

K^+ production by neutrinos at MINERvA

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Fermilab Wine and Cheese
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ROCHESTER





The big picture



- Motivation for studying K^+ production by neutrinos
- Identifying K^+ in MINERvA
- Differential cross section measurements:
 - Charged-current K^+ production
 - Neutral-current K^+ production
- Search for charged-current coherent K^+ production



The big picture

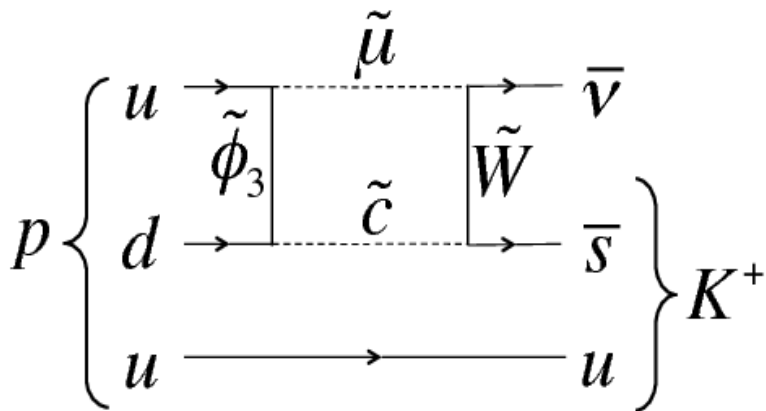


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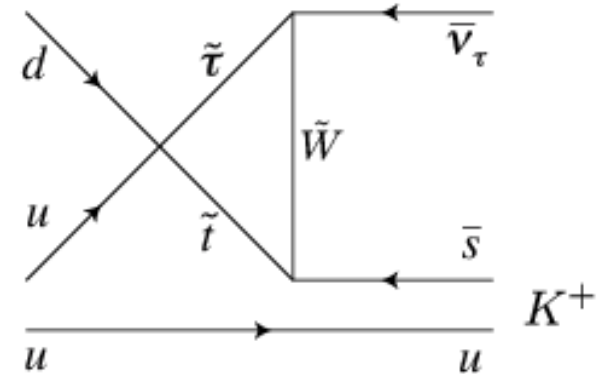
Why study K^+ production?



- K^+ production by atmospheric neutrinos, especially by the neutral current, is a background in searches for the proton decay $p \rightarrow K^+ \nu$



Abe, K. et al. arXiv:1109.3262



Hewett, J.L. et al. arXiv:1401.6077 [hep-ex]
FERMILAB-CONF-14-019-CH02



Why study K^+ production?



- K^+ production by atmospheric neutrinos, especially by the neutral current, is a background in searches for the proton decay $p \rightarrow K^+ \nu$
- K^+ production complements measurements of π^+ production as a probe of hadron interactions inside the nucleus



Why study K^+ production?



**105 MeV kinetic energy
for proton at rest**

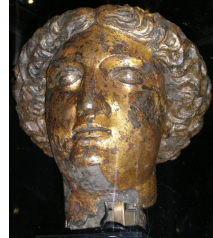
$\bar{\nu}$

K^+

Big detector



Why study K^+ production?



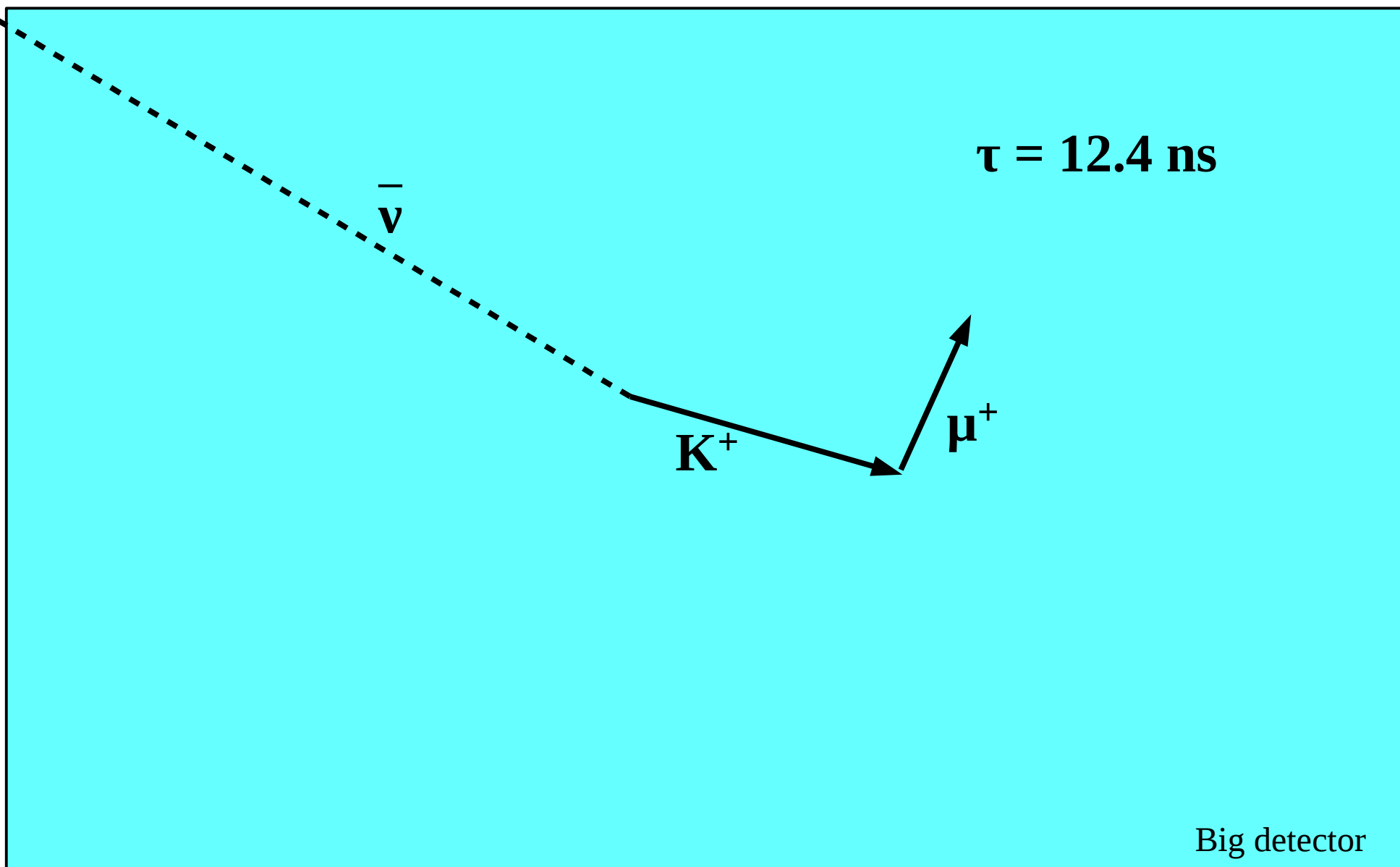
**105 MeV kinetic energy
for proton at rest**

**Water Cherenkov
threshold = 252 MeV**

Big detector

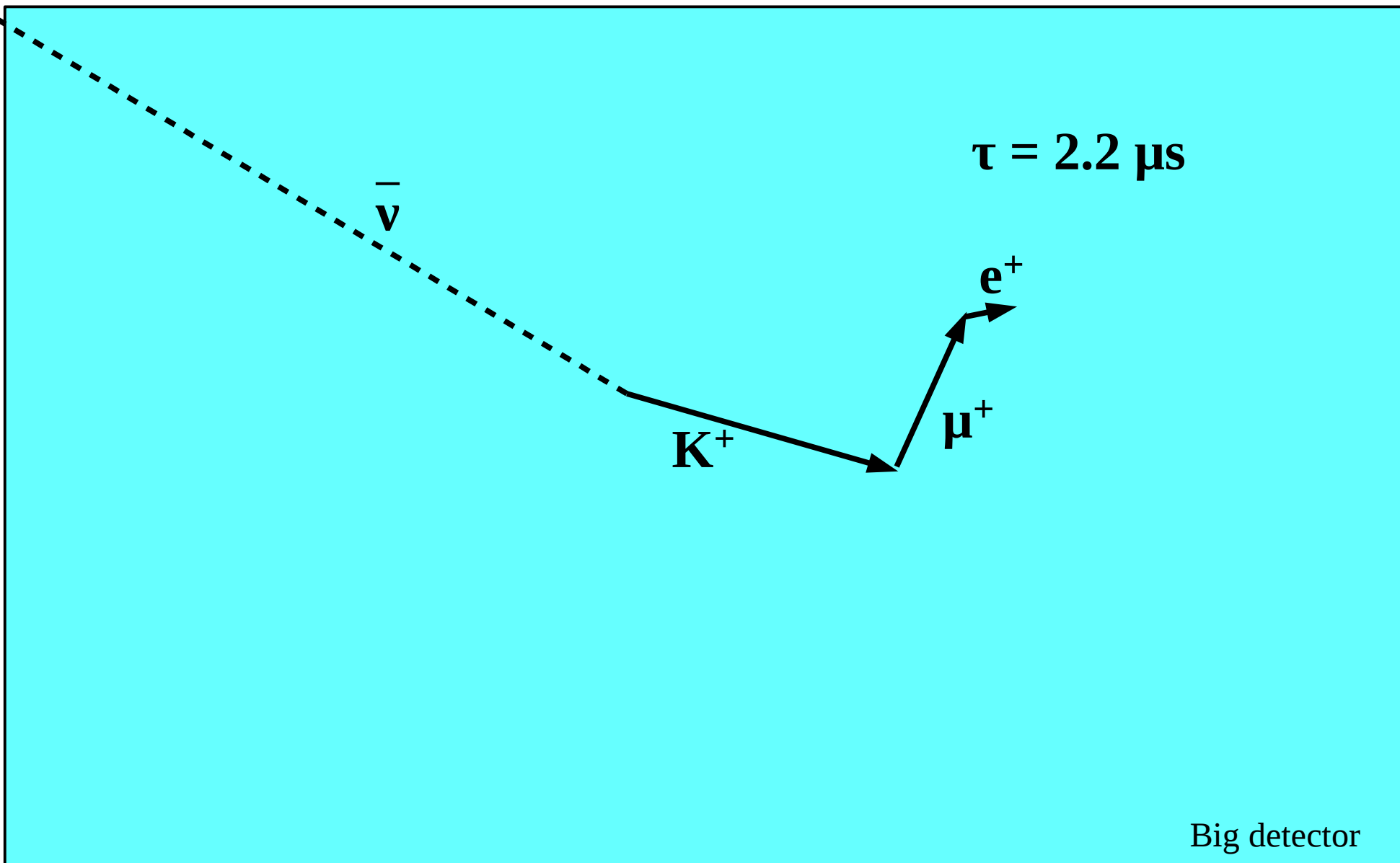
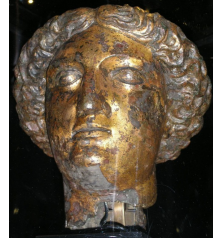


Why study K^+ production?



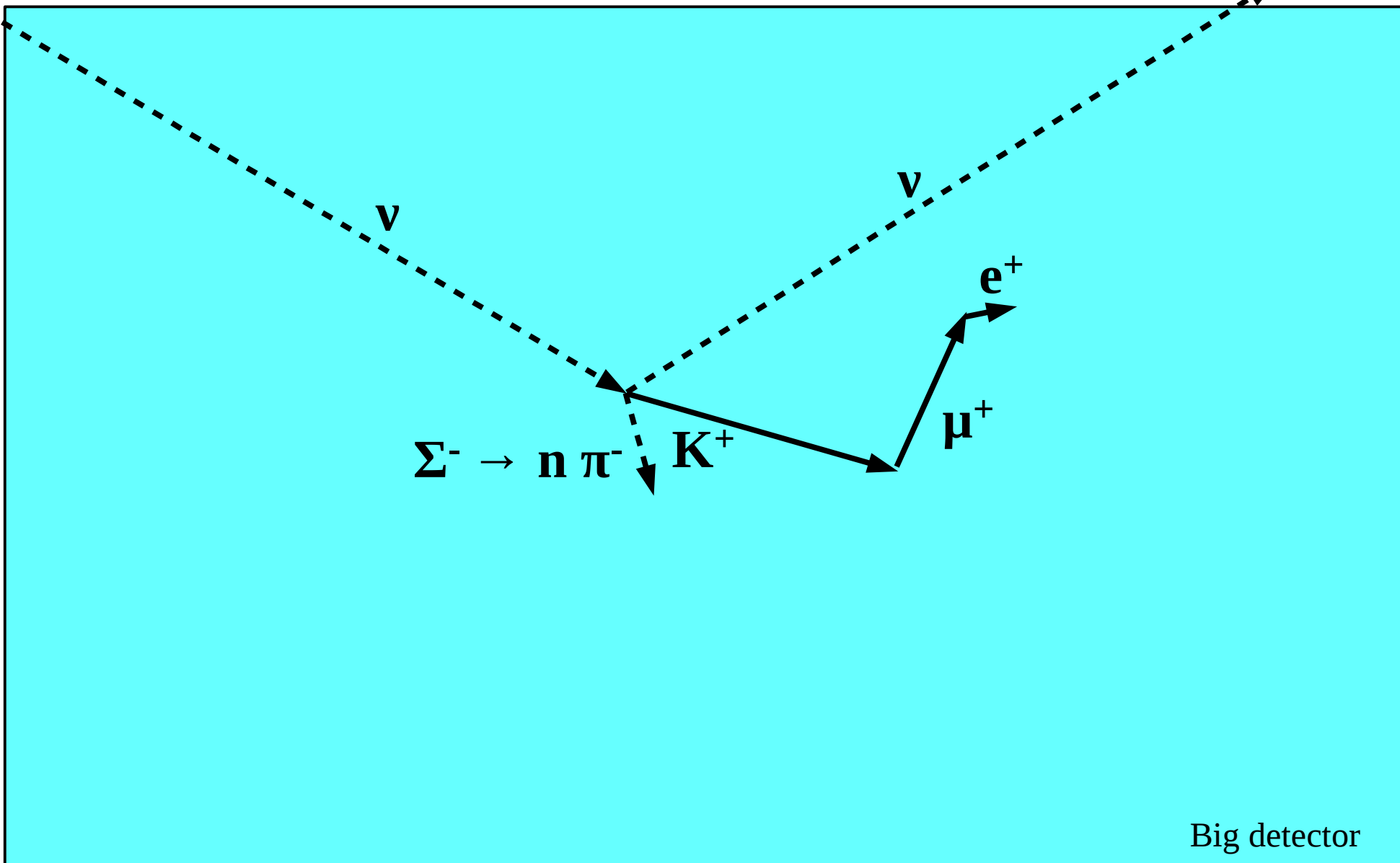
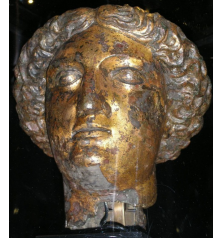


Why study K^+ production?





Why study K^+ production?

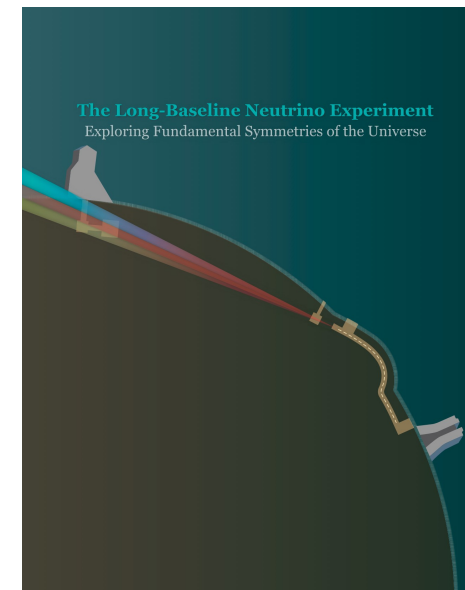


DUNE background prediction

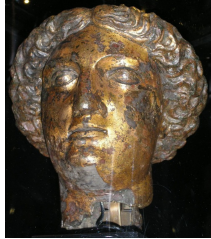


1 event per Mton-year JHEP **0704** 041 (2007)

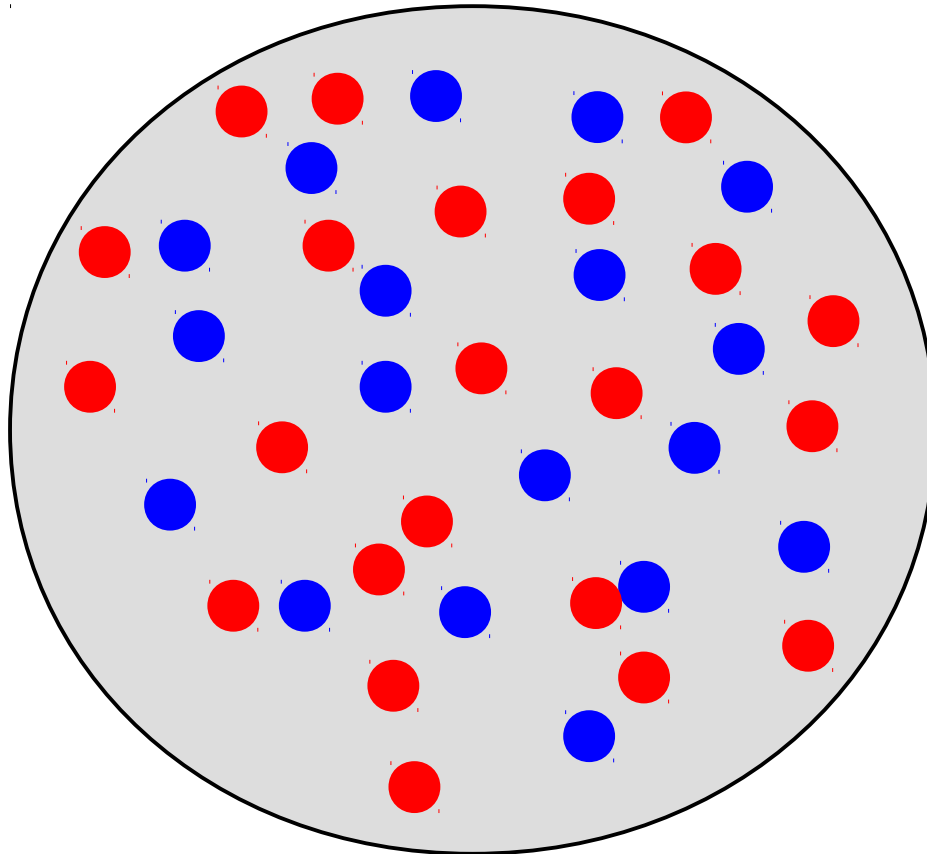
“It is natural to ask to what extent simulations are capable of providing reliable estimates for such rare processes. What if the actual rate for single-kaon atmospheric-neutrino events is higher by a factor of ten or more? Is that even conceivable?”



Zoom in on the nucleus



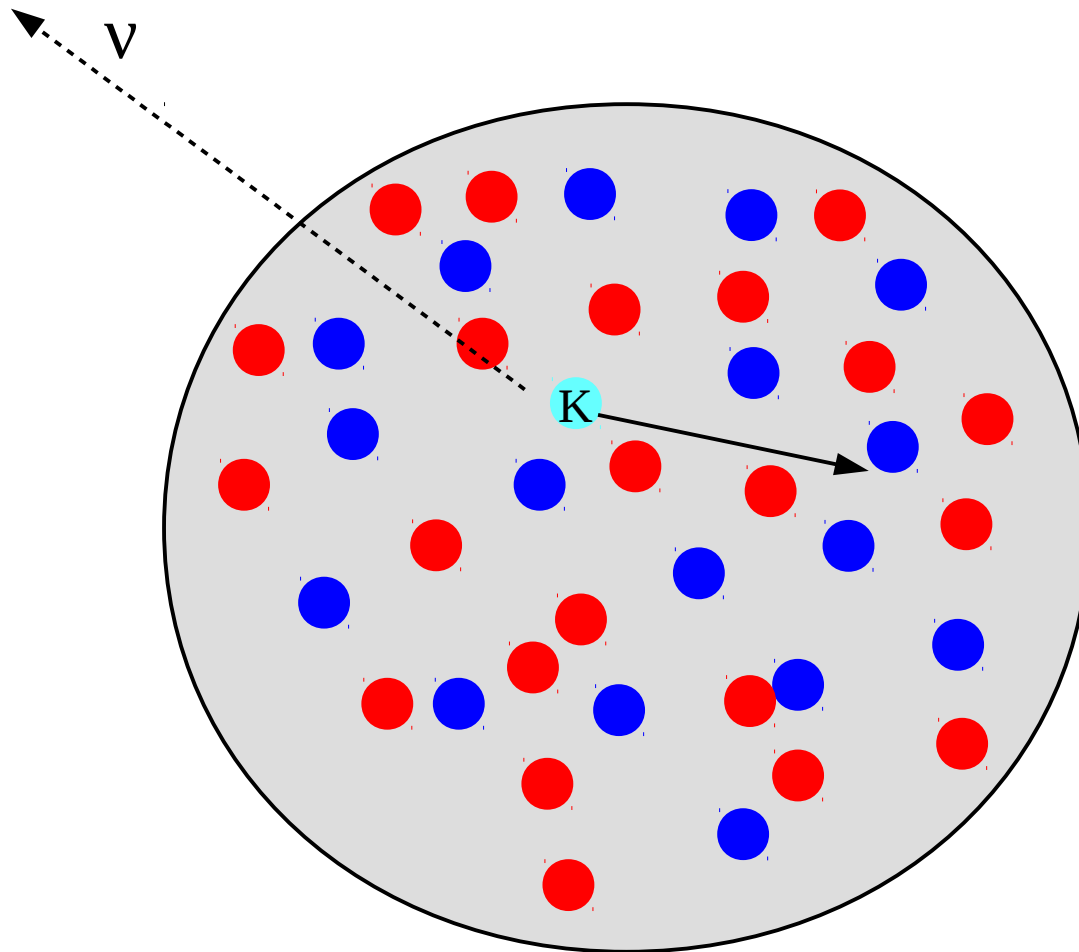
A proton is about to decay!



Argon nucleus
not to scale



Zoom in on the nucleus

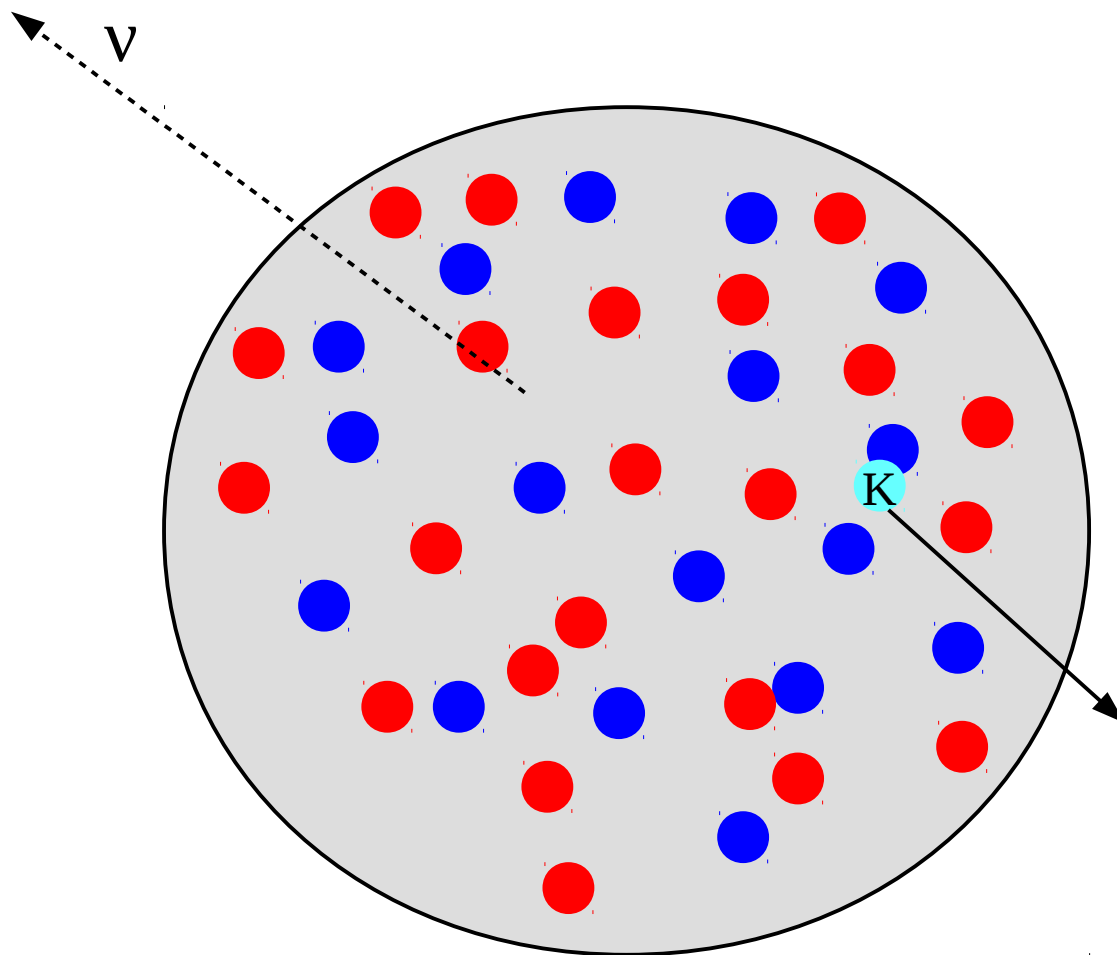


The kaon must get out of the nucleus, and may undergo final-state interactions (FSI)

Argon nucleus
not to scale



Zoom in on the nucleus

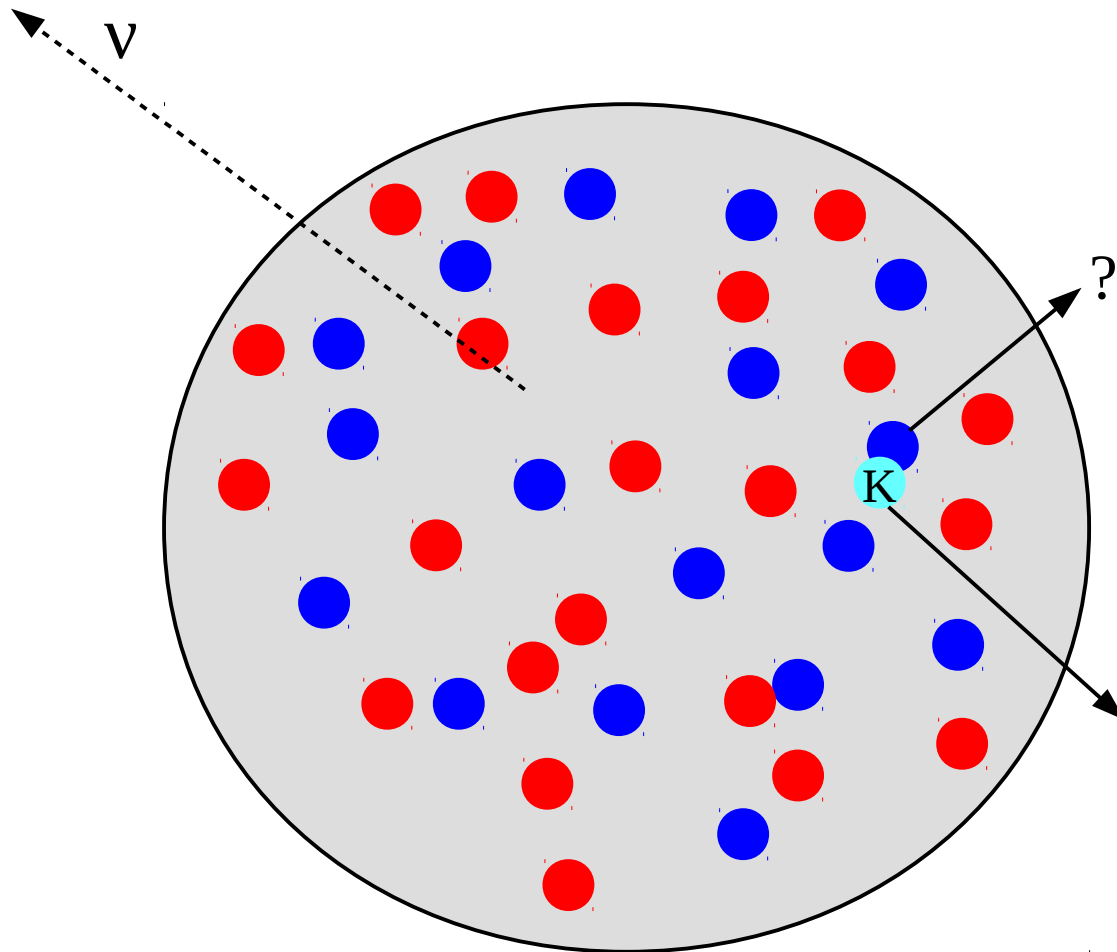
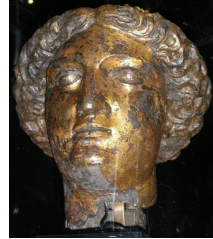


Momentum spectrum is smeared by FSI

Argon nucleus
not to scale



Zoom in on the nucleus

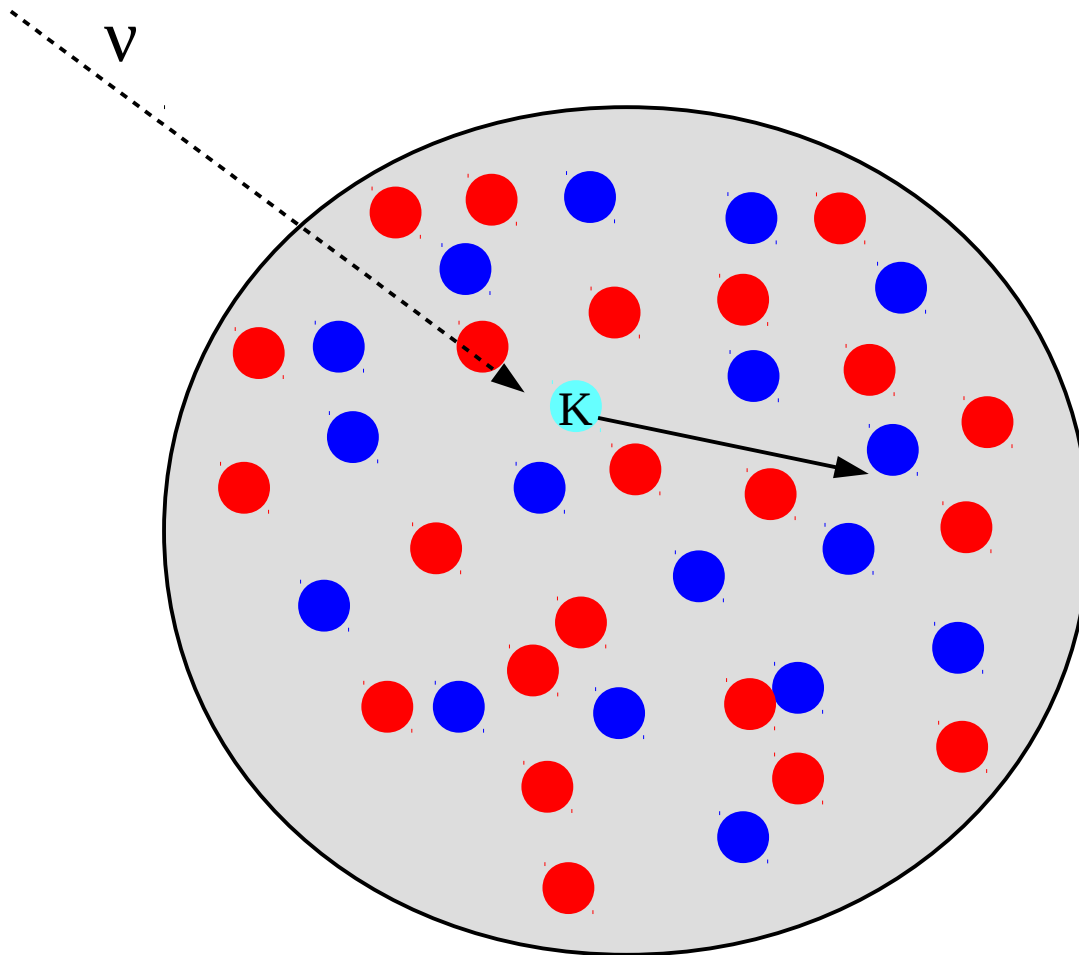


And other nucleons could be knocked out

Argon nucleus
not to scale



We can study this with neutrinos



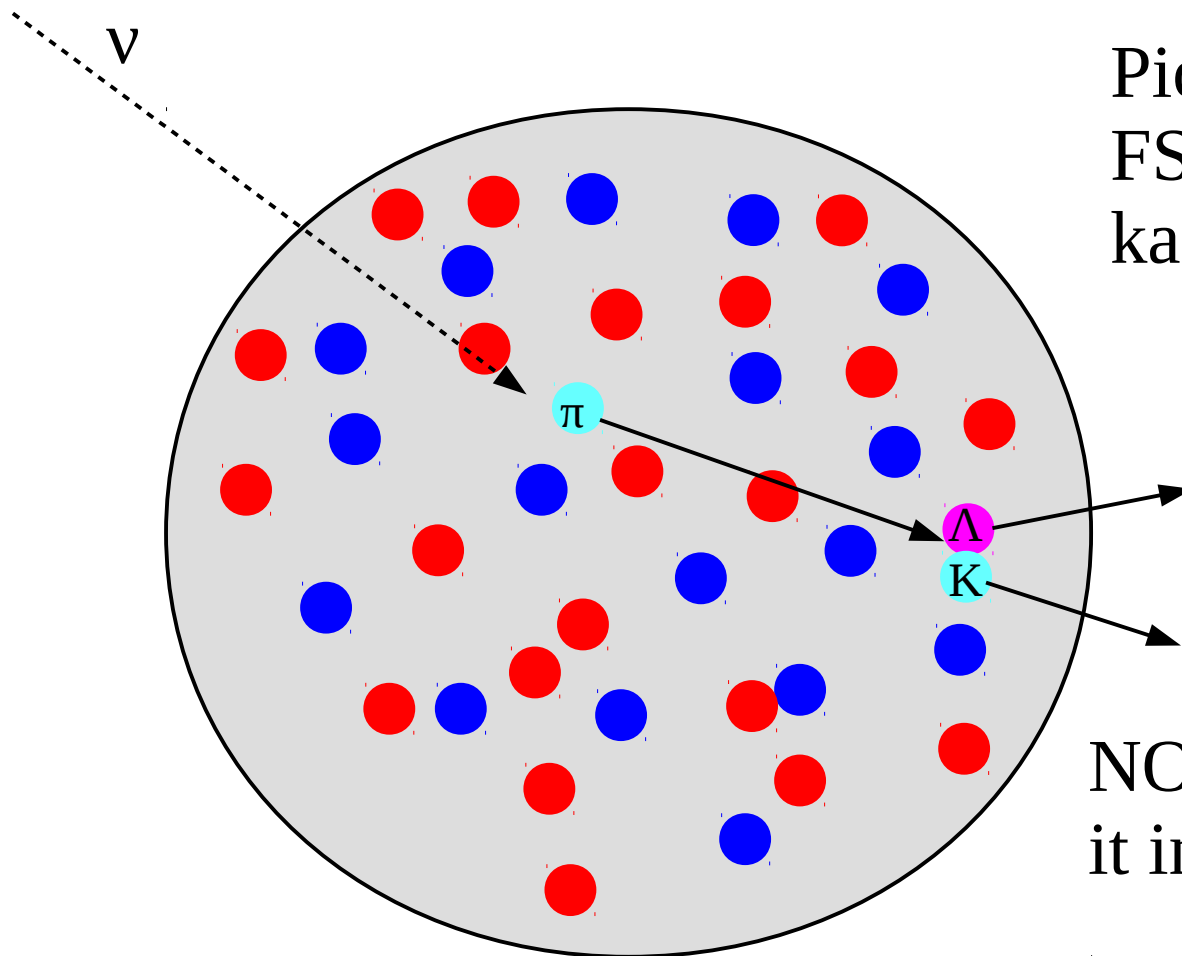
FSI affects kaons produced in neutrino reactions

Does our nuclear model (kaon spectrum) agree with the data?

Argon nucleus
not to scale



Kaon production via FSI



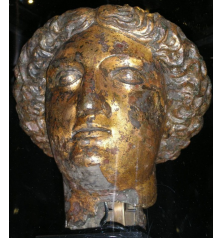
Pion production +
FSI can produce
kaons

NOT in GENIE...is
it in the data?

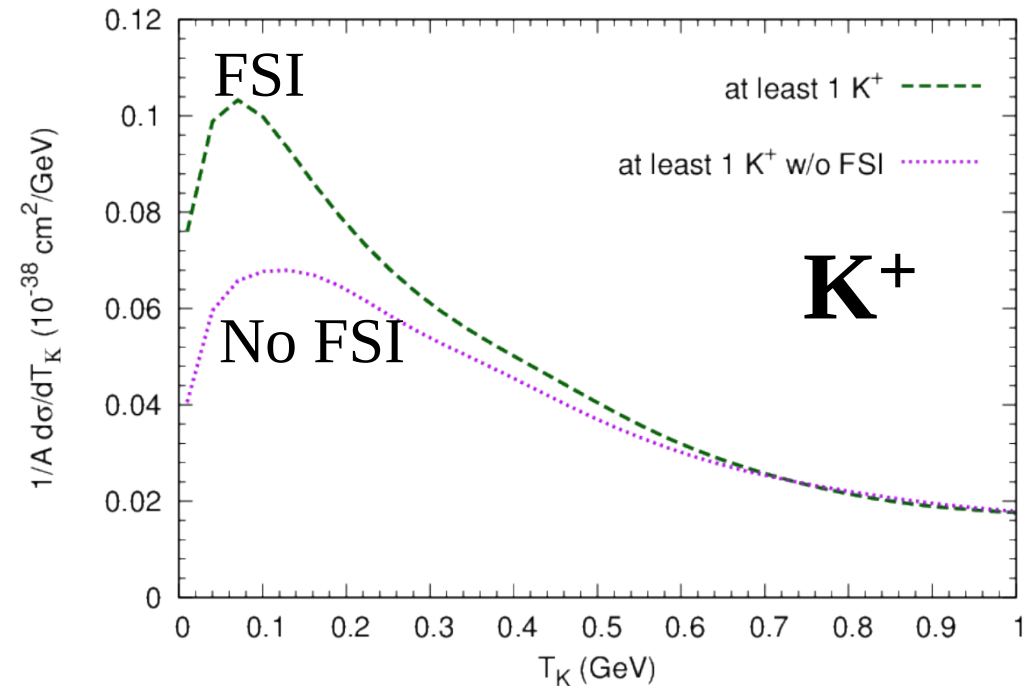
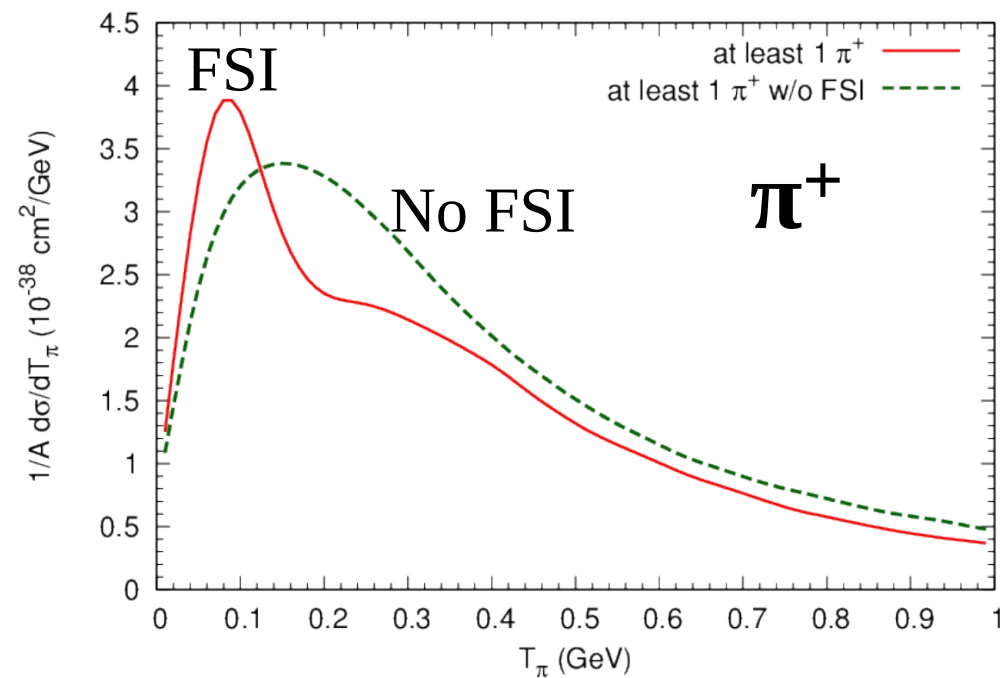
Argon nucleus
not to scale



Pion and kaon production as probes of FSI

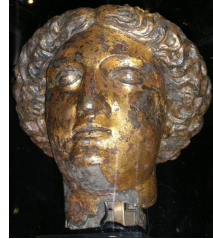


ν_μ CC GiBUU event generator predictions,
MINER ν A LE flux, carbon target

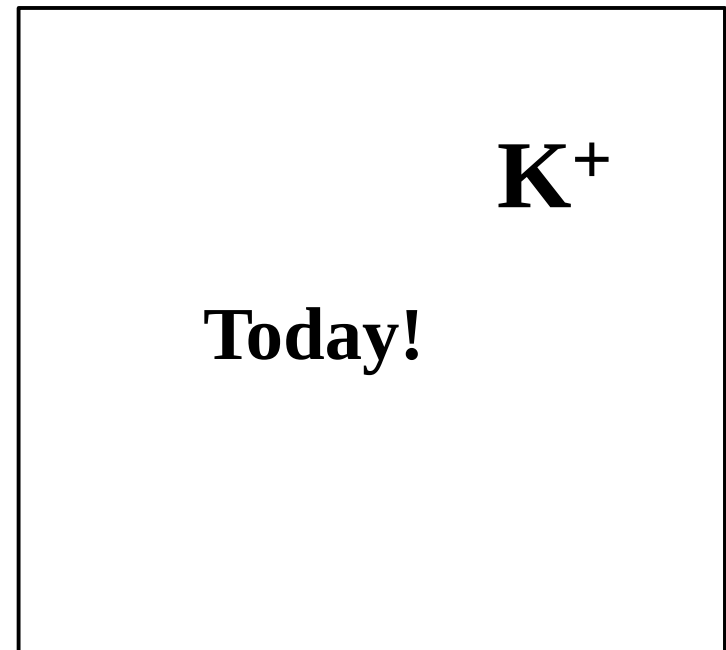
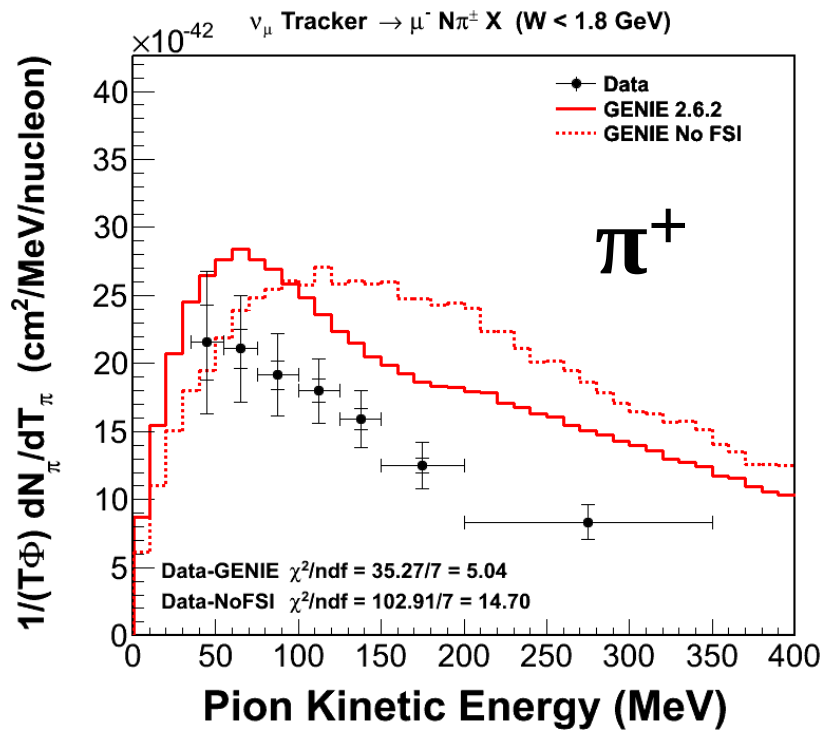


Mosel, Lalakulich, Gallmeister, Phys. Rev. D 89, 093003

Pion and kaon production as probes of FSI



ν_μ CC MINERvA data



Phys. Rev. D 92, 092008 (2015)
 Wine & Cheese 7 February 2014

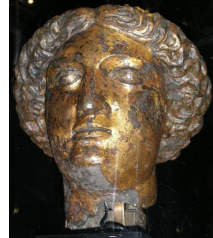
What can MINERvA do?



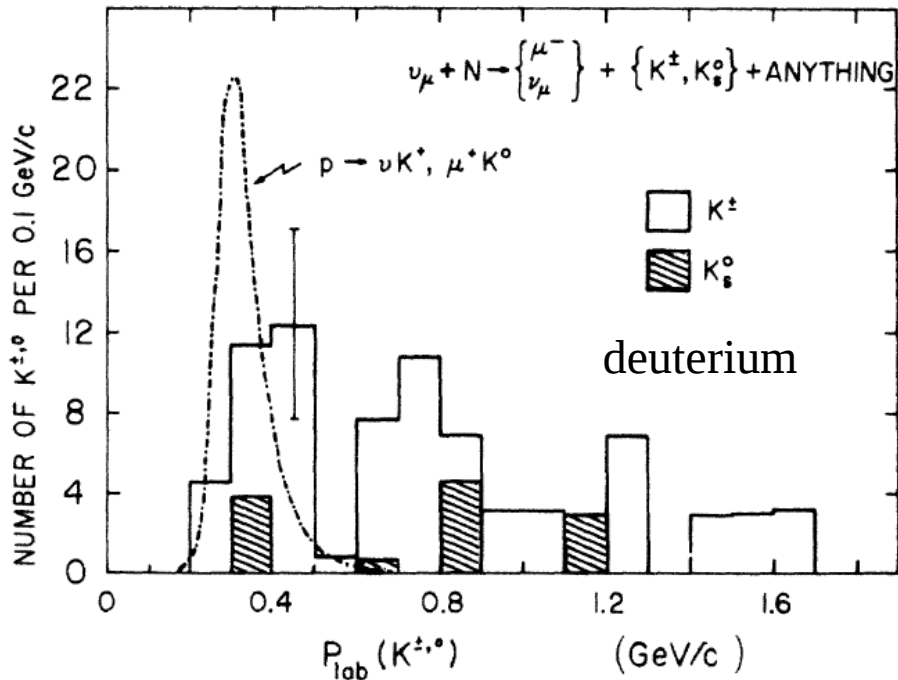
- Measure K^+ production cross sections on CH
- Benchmark Monte Carlo generators
- Measure kaon spectrum sensitive to FSI



Existing K^+ neutrino data

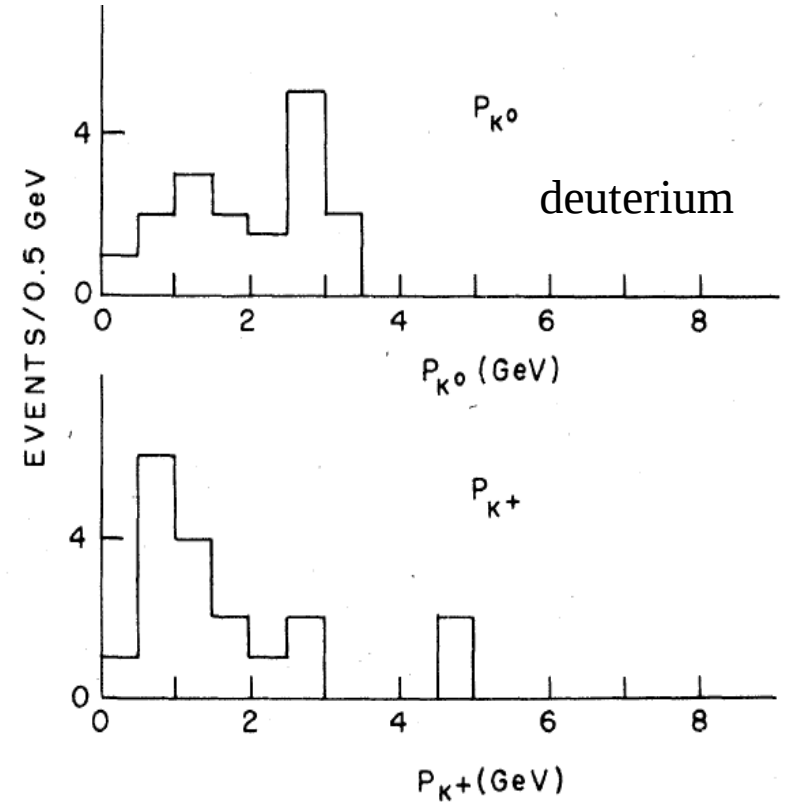


W. A. Mann et al., Phys.Rev. D34, 2545 (1986)



ANL 12' bubble chamber

N. J. Baker et al., Phys.Rev. D24, 2779 (1981)



BNL 7' bubble chamber

Also Gargamelle: Physics Letters B 73 4-5 (1978)



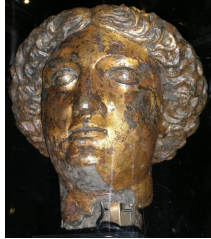
Types of reactions



- “Associated production”, “ $\Delta S = 0$ ”: pairs of strange particles in final state
 - $\nu_{\mu} n \rightarrow \mu^{-} K^{+} \Lambda$
 - $\nu_{\mu} n \rightarrow \mu^{-} K^{+} K^{-} p$
 - $\nu_{\mu} n \rightarrow \nu_{\mu} K^{+} \Sigma^{-}$



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- “Single kaon production”, “ $\Delta S = 1$ ”: Cabibbo-suppressed, single kaon final state
 - $\nu_{\mu} N \rightarrow \mu^{-} K^{+} N$



Types of reactions



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- “Single kaon production”, “ $\Delta S = 1$ ”: Cabibbo-suppressed, single kaon final state
 - $\nu_{\mu} N \rightarrow \mu^{-} K^{+} N$
- “Coherent kaon production”: nucleus remains in ground state
 - $\nu_{\mu} A \rightarrow \mu^{-} K^{+} A$



Meet the generator

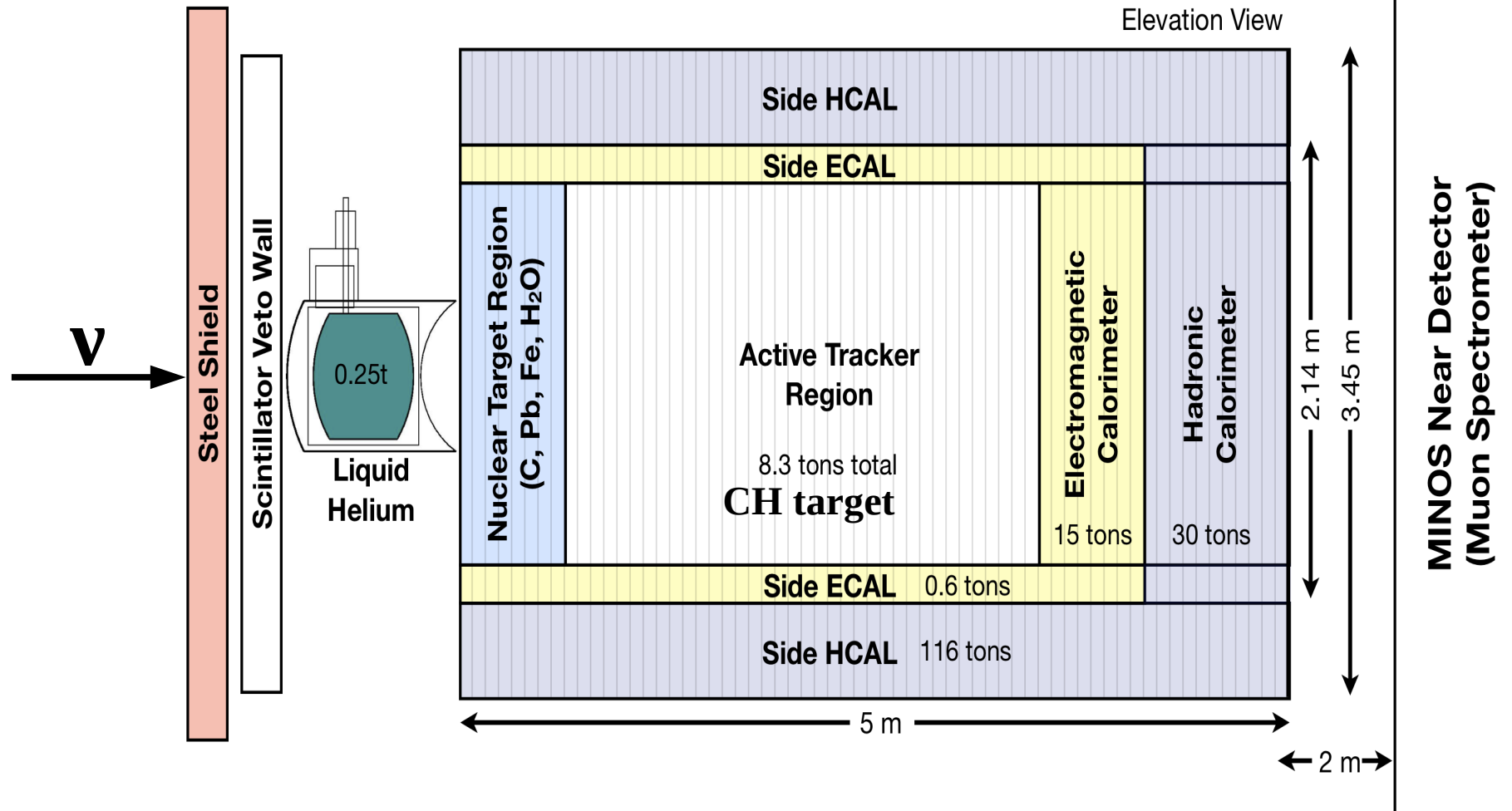
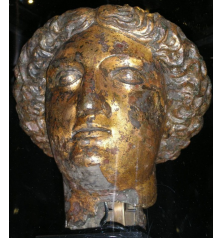


- GENIE version 2.8.4
 - Also used by NOvA, DUNE, MicroBooNE, others
- Kaons are generated in the hadronization model:
 - KNO for $1.7 < W / \text{GeV} < 2.3$
 - AGKY for $2.3 < W / \text{GeV} < 3.0$
 - PYTHIA for $W > 3 \text{ GeV}$
- Rate of strange production is tuned to Λ and K^0_S data on deuterium from BEBC and FNAL 15' bubble chambers
- Single kaon production not in default model, but introduced in 2.10 based on Alam et al. Phys.Rev. **D82** 033001 (2010)
- No coherent K^+ production





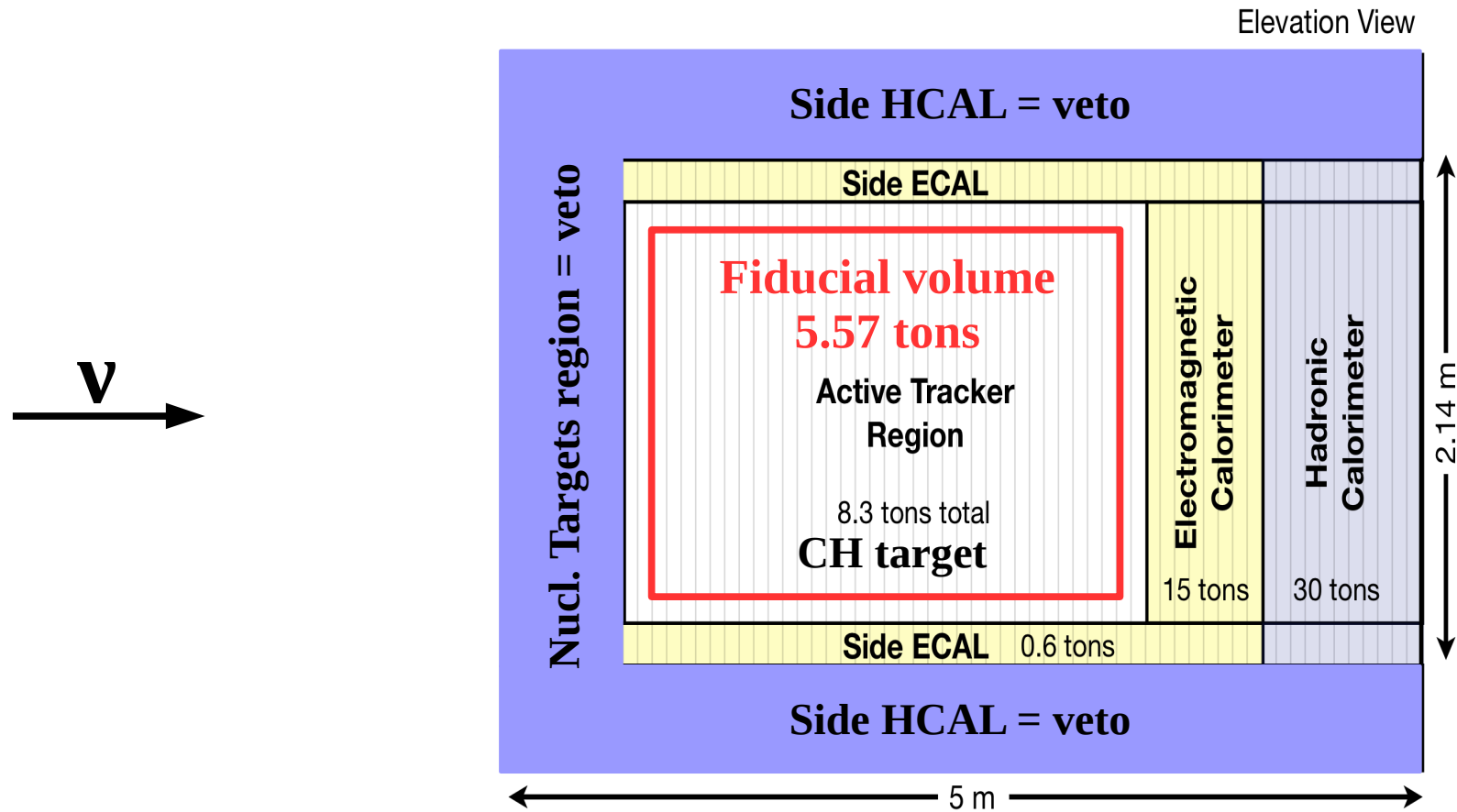
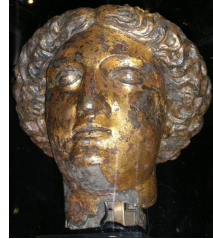
The MINERvA detector



Nucl. Inst. and Meth. A743 (2014) 130
arXiv:1305.5199



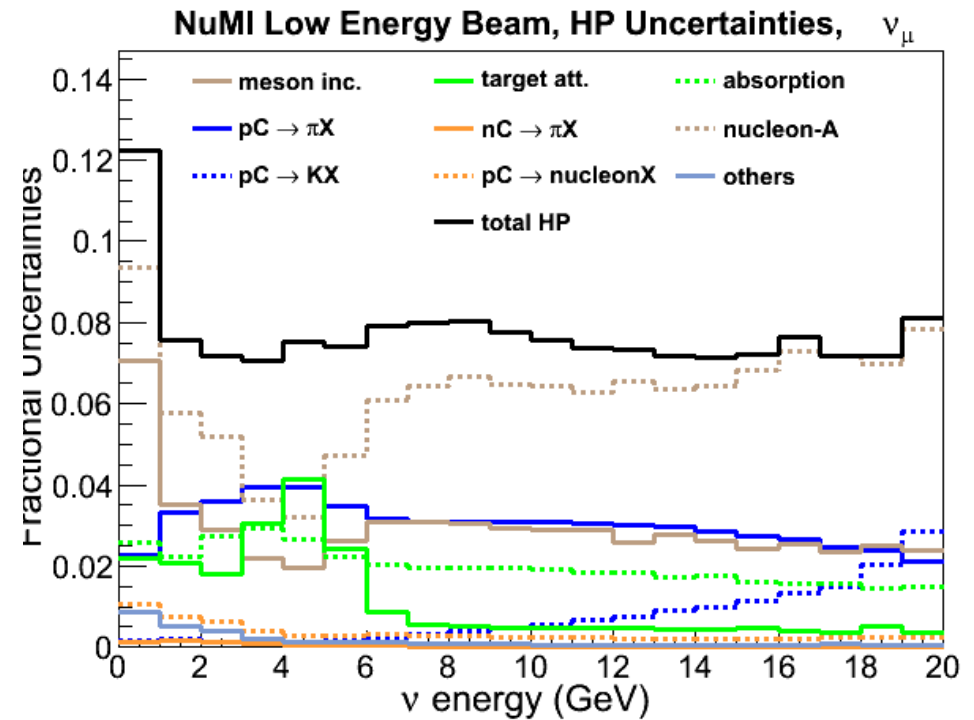
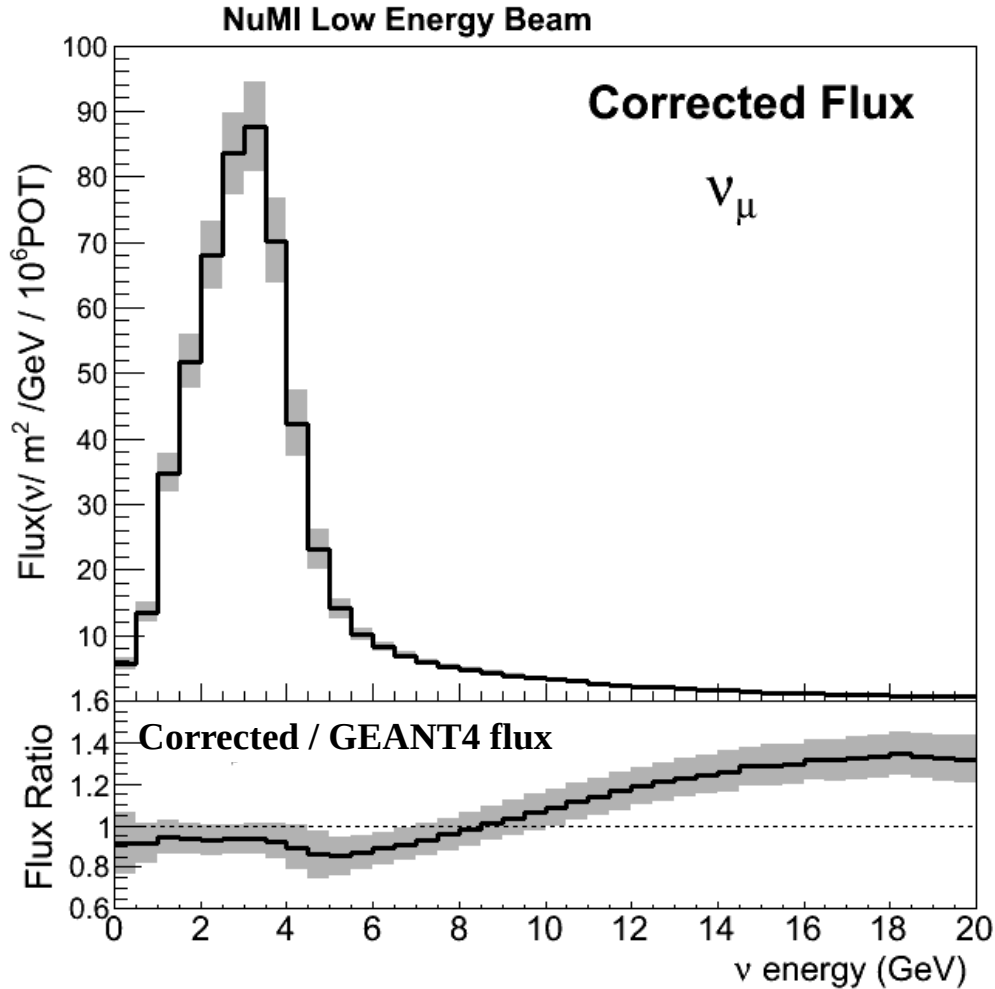
The MINERvA detector for this analysis



Nucl. Inst. and Meth. A743 (2014) 130
arXiv:1305.5199

Neutrino flux

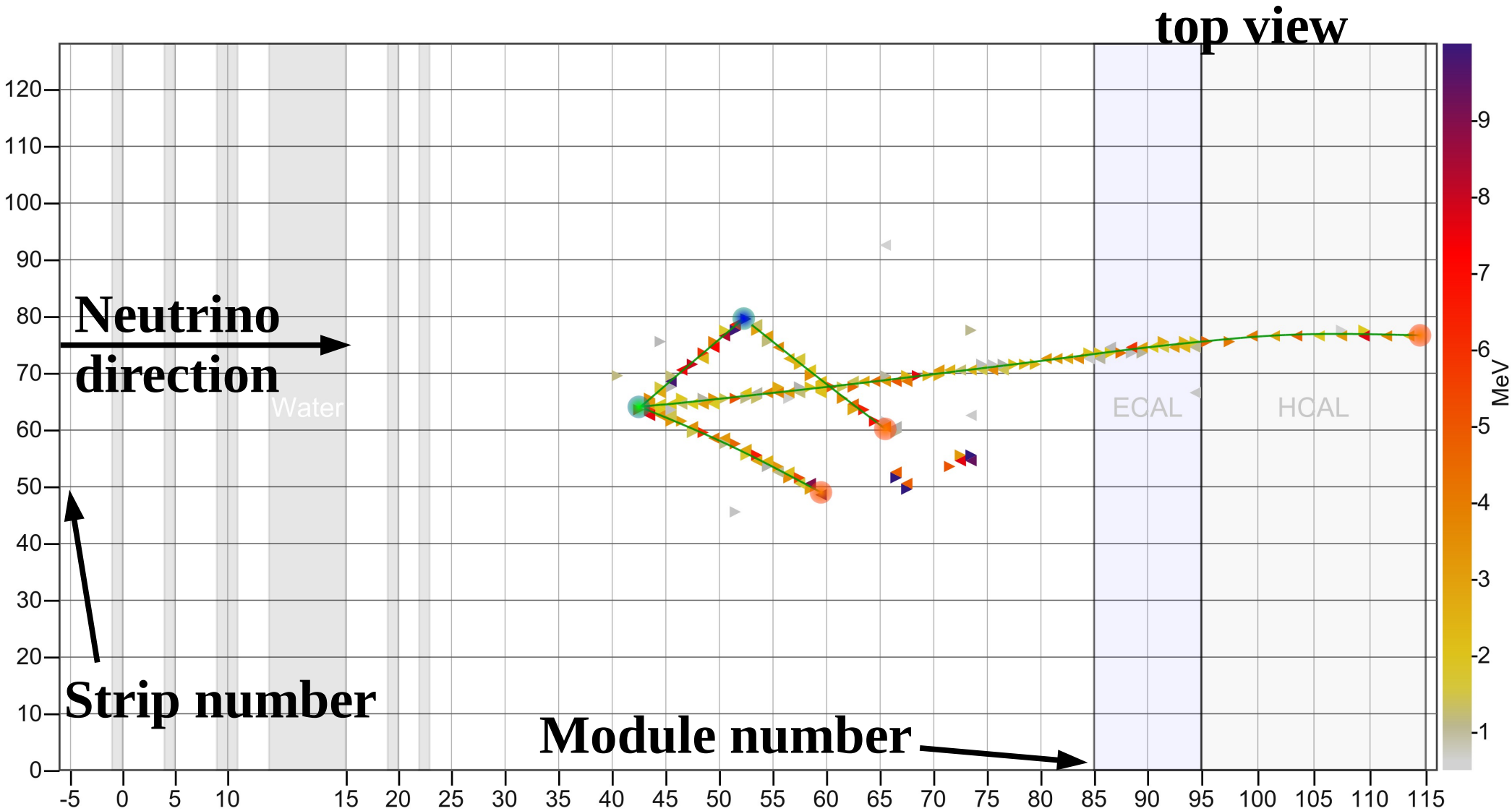
Leo Aliaga Wine & Cheese, 18 December 2015



NuMI “low energy” beam tune, ~ 3.5 GeV peak energy, with $\sim 8\%$ uncertainty dominated by hadron production

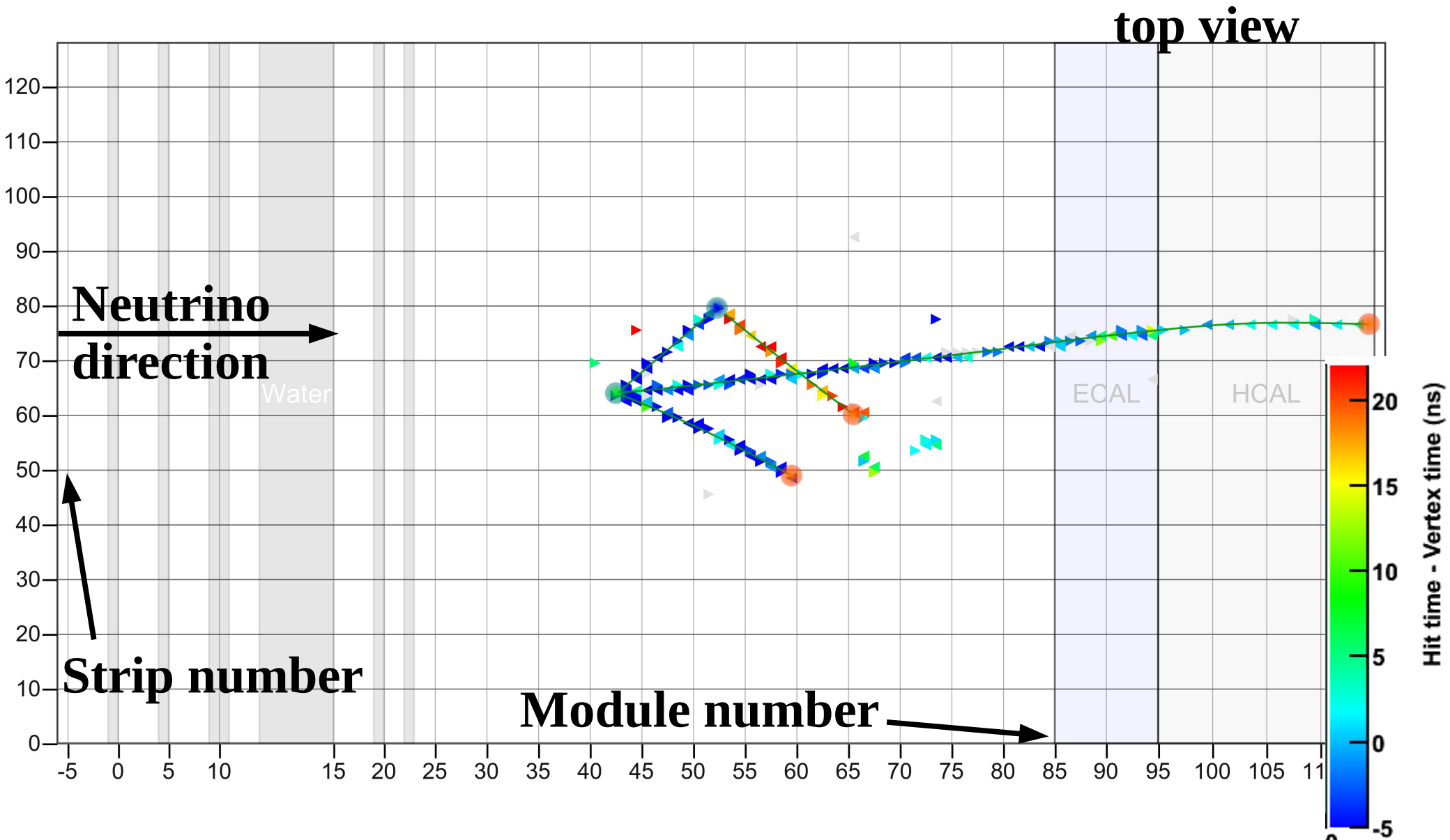
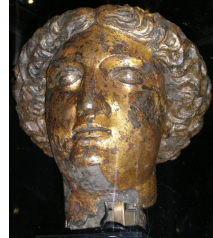


Kaon candidate event display



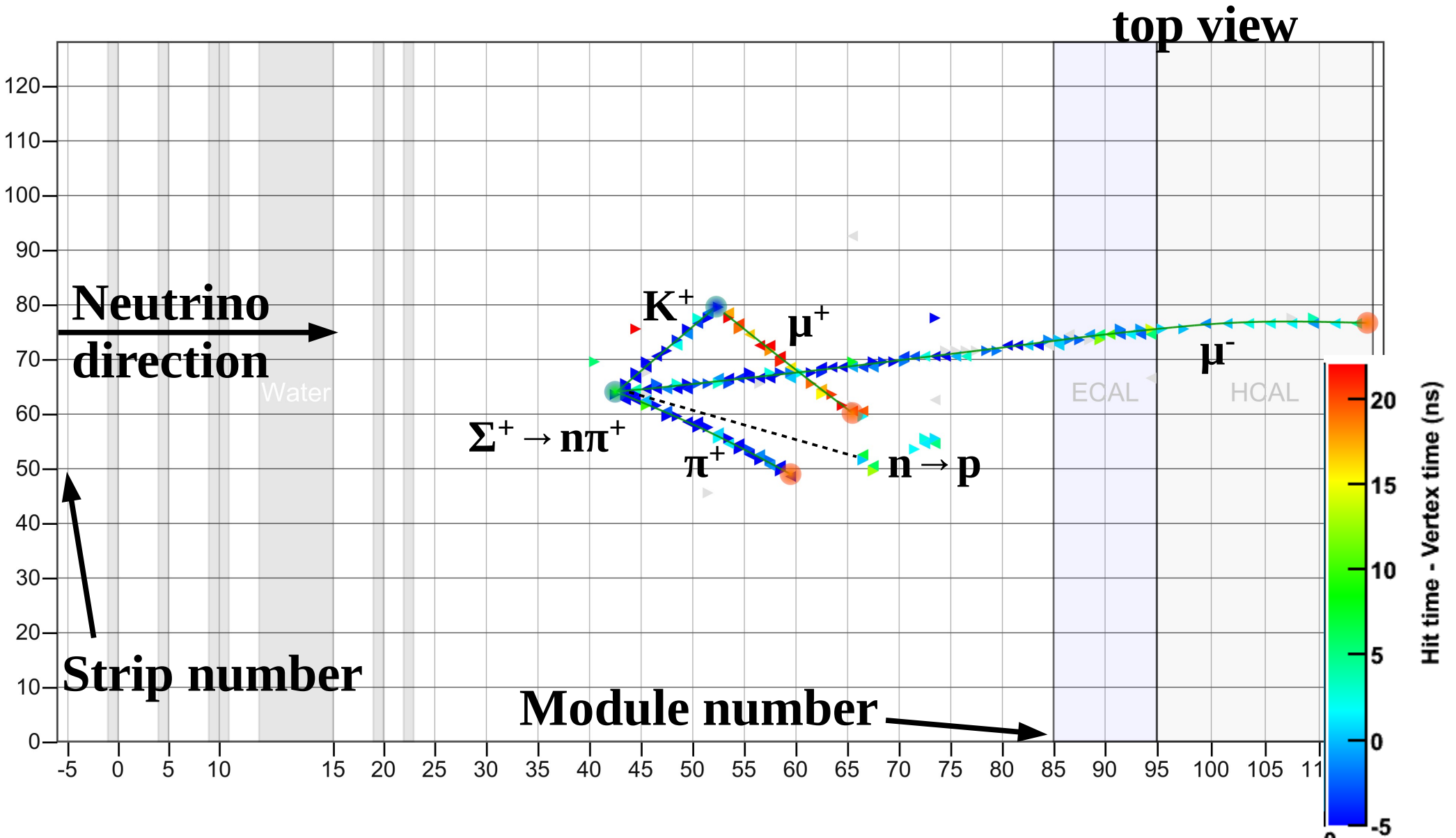


Kaon candidate event display



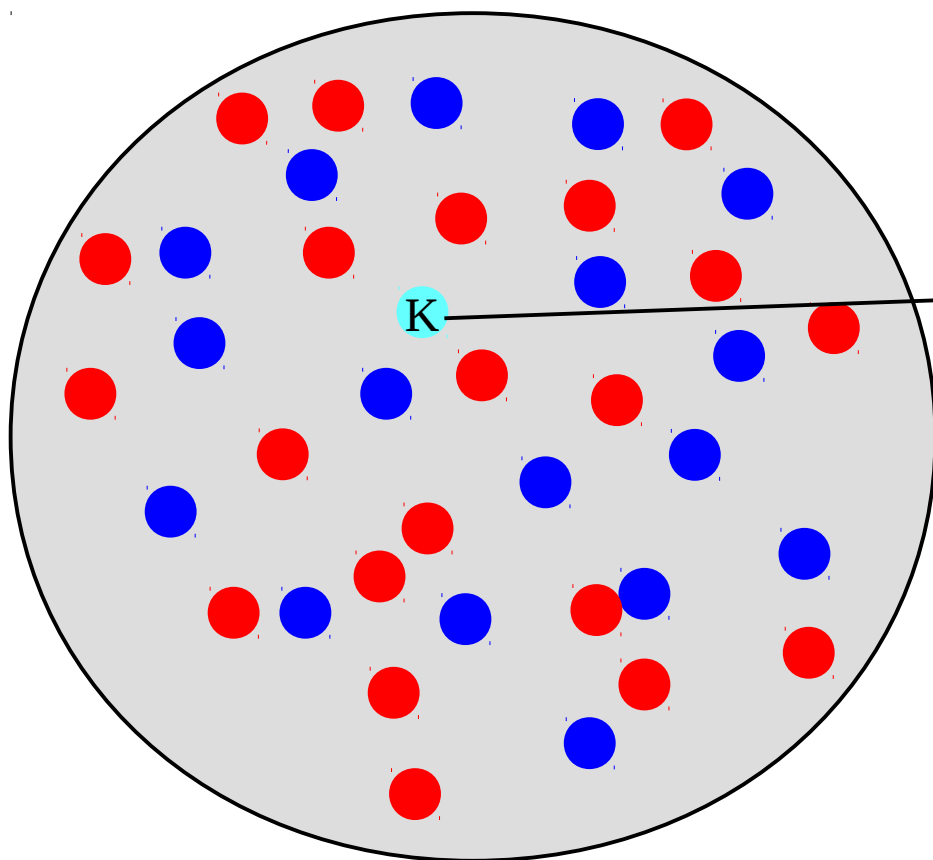


My guess: $\nu_{\mu}p \rightarrow \mu^{-}K^{+}\Sigma^{+}$





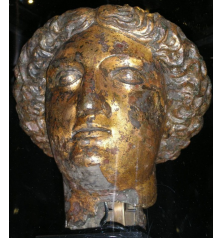
Signal definition



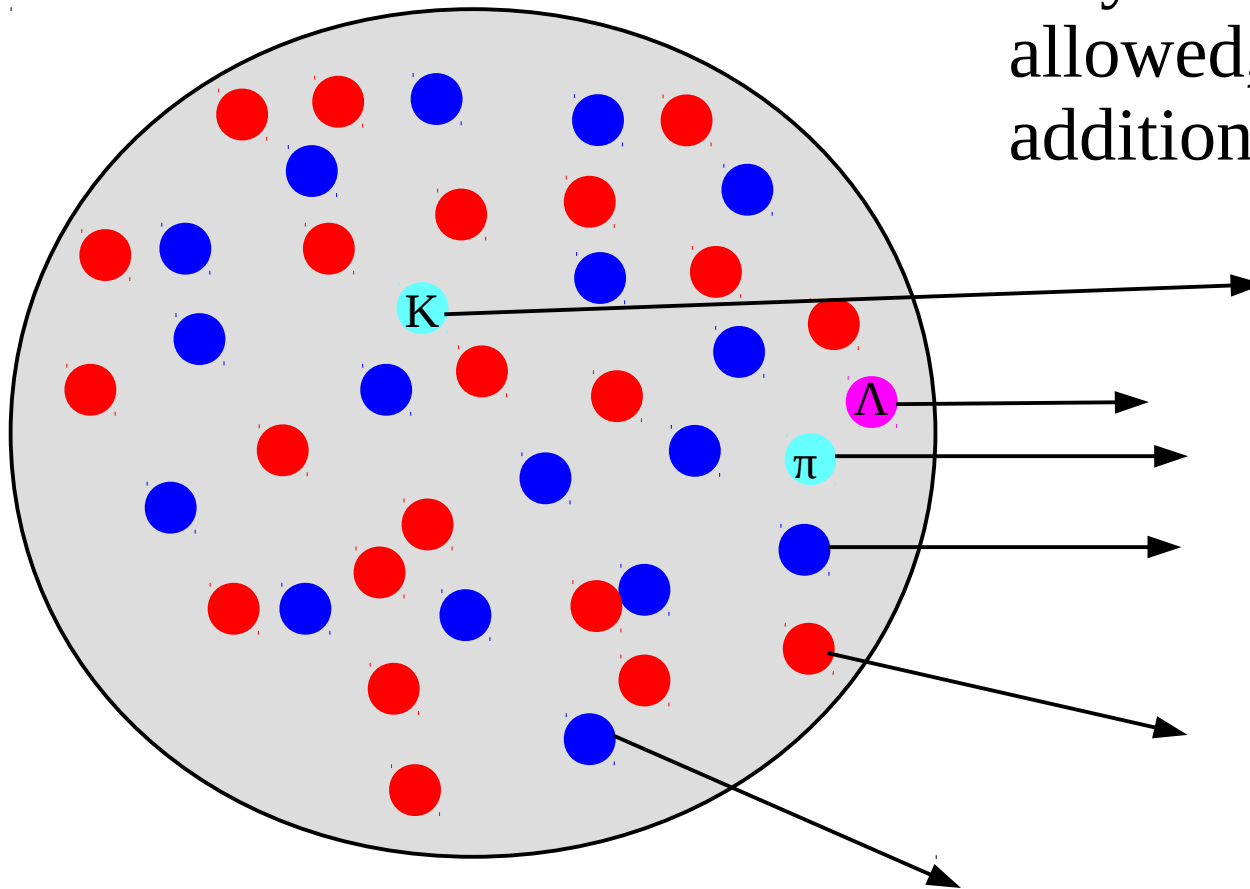
At least one K^+
exiting the nucleus



Signal definition



Any other particles are allowed, including additional kaons



CC and NC sample definitions



For CC analysis, require μ^- in the final state

For NC analysis, require zero charged leptons at neutrino interaction vertex





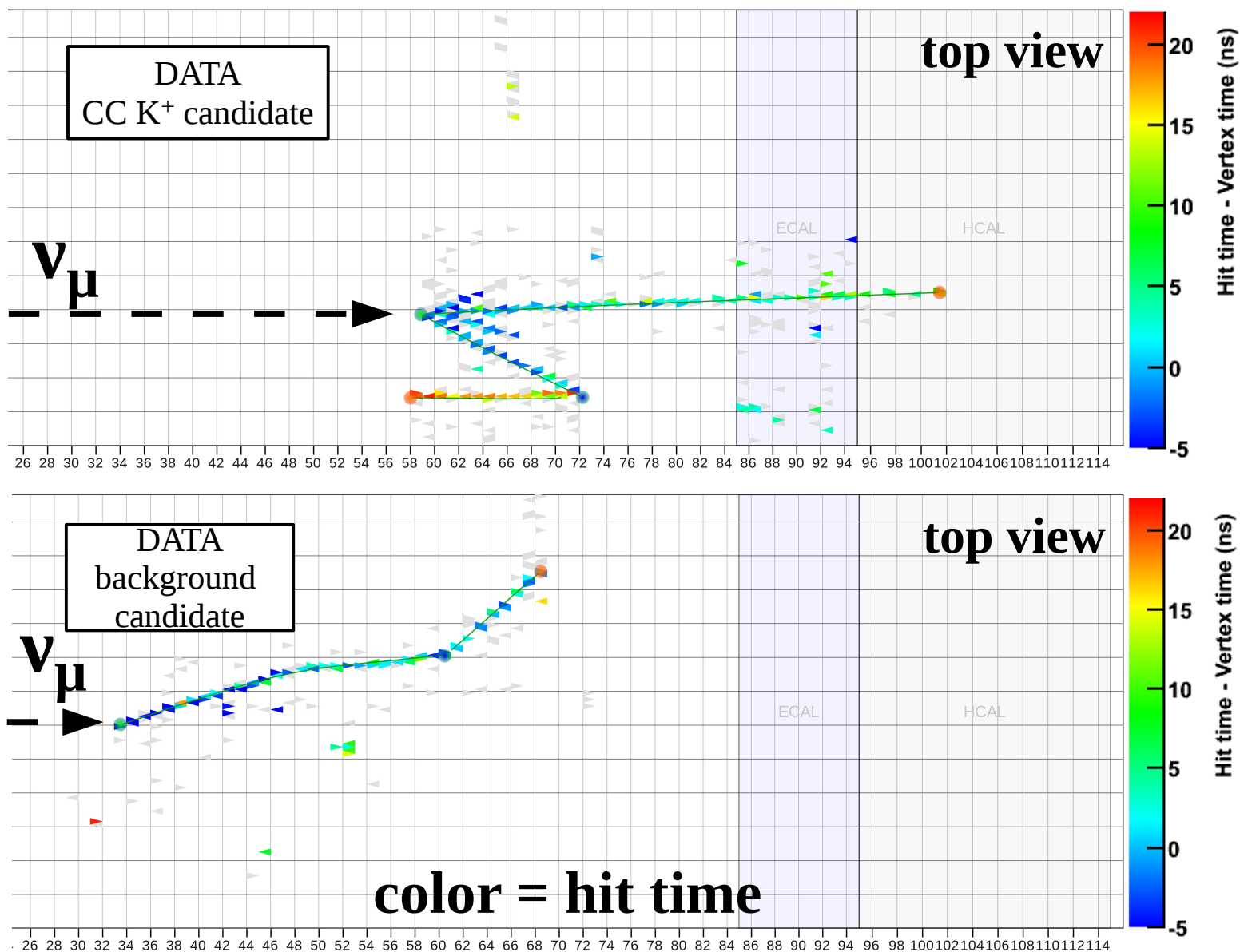
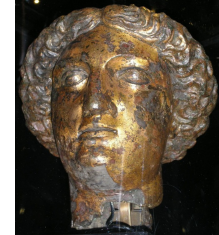
The big picture



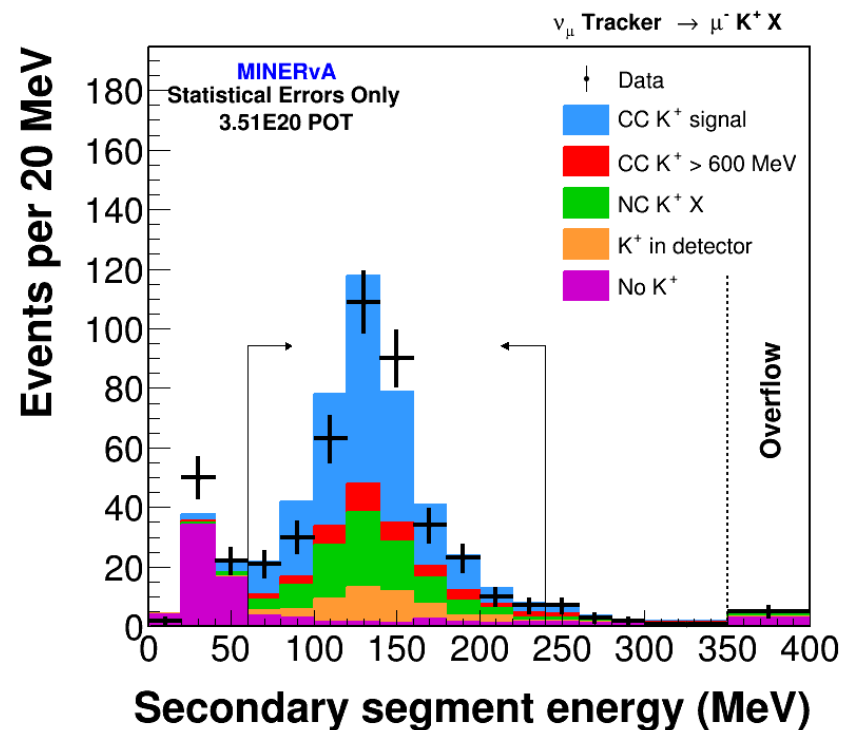
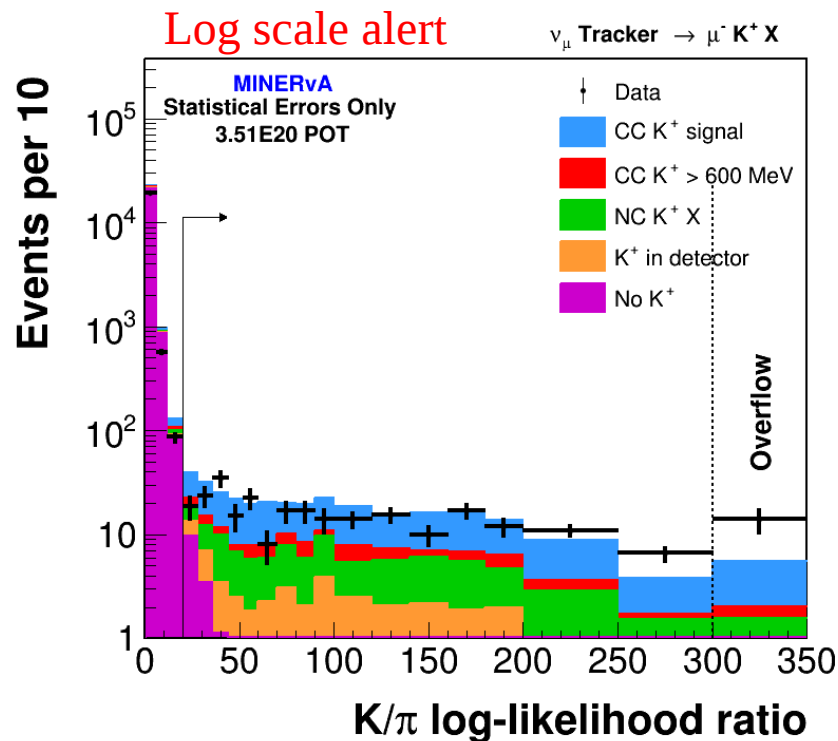
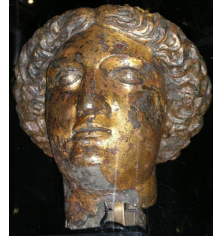
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Identifying K^+ by timing



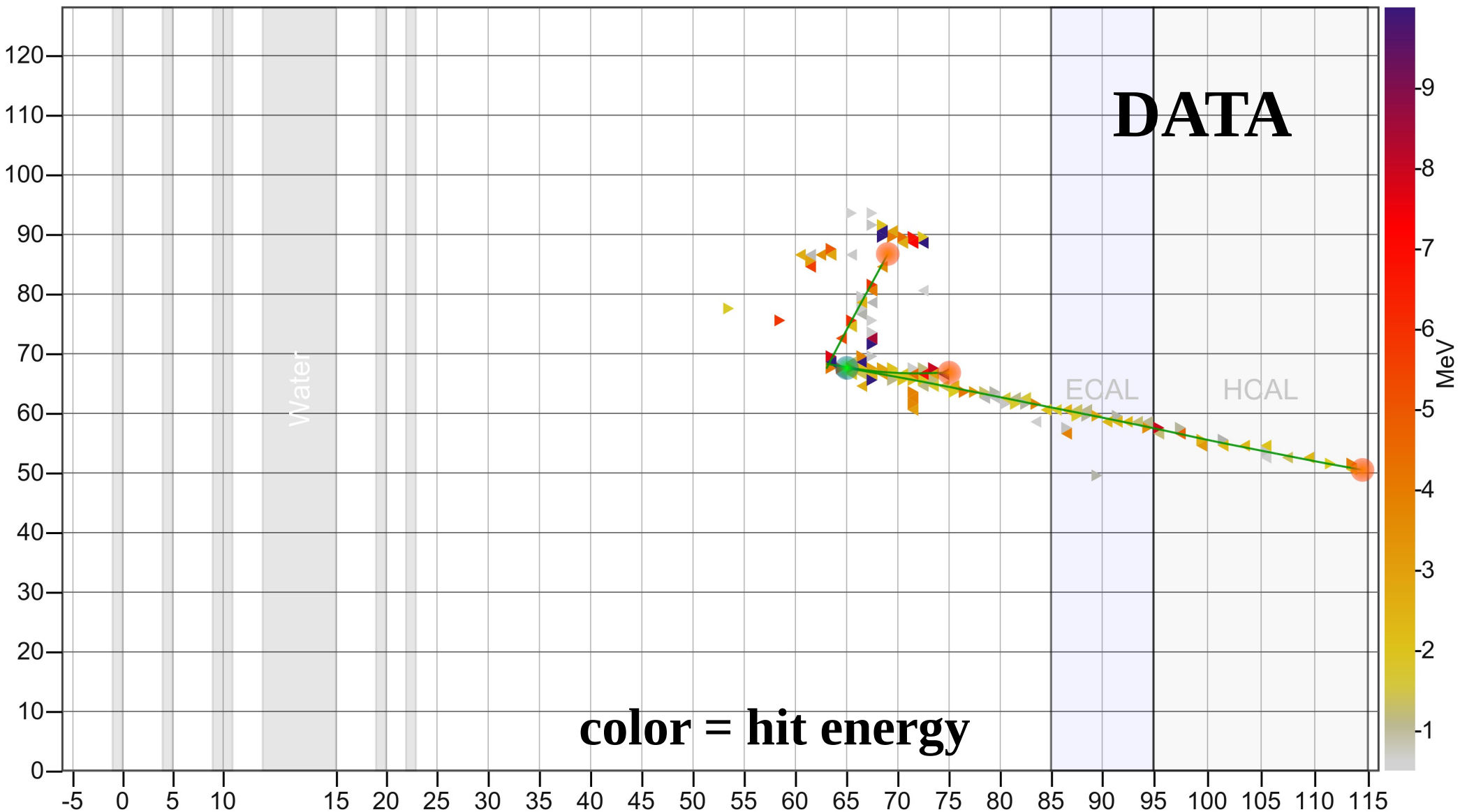
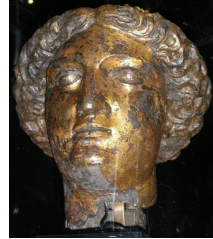
Kinked track selection



- Fit timing profile with two hypotheses, cut on log-likelihood ratio to select kaon-like events
- All from $K^+ \rightarrow \mu^+ \nu$ decays, muon is monoenergetic

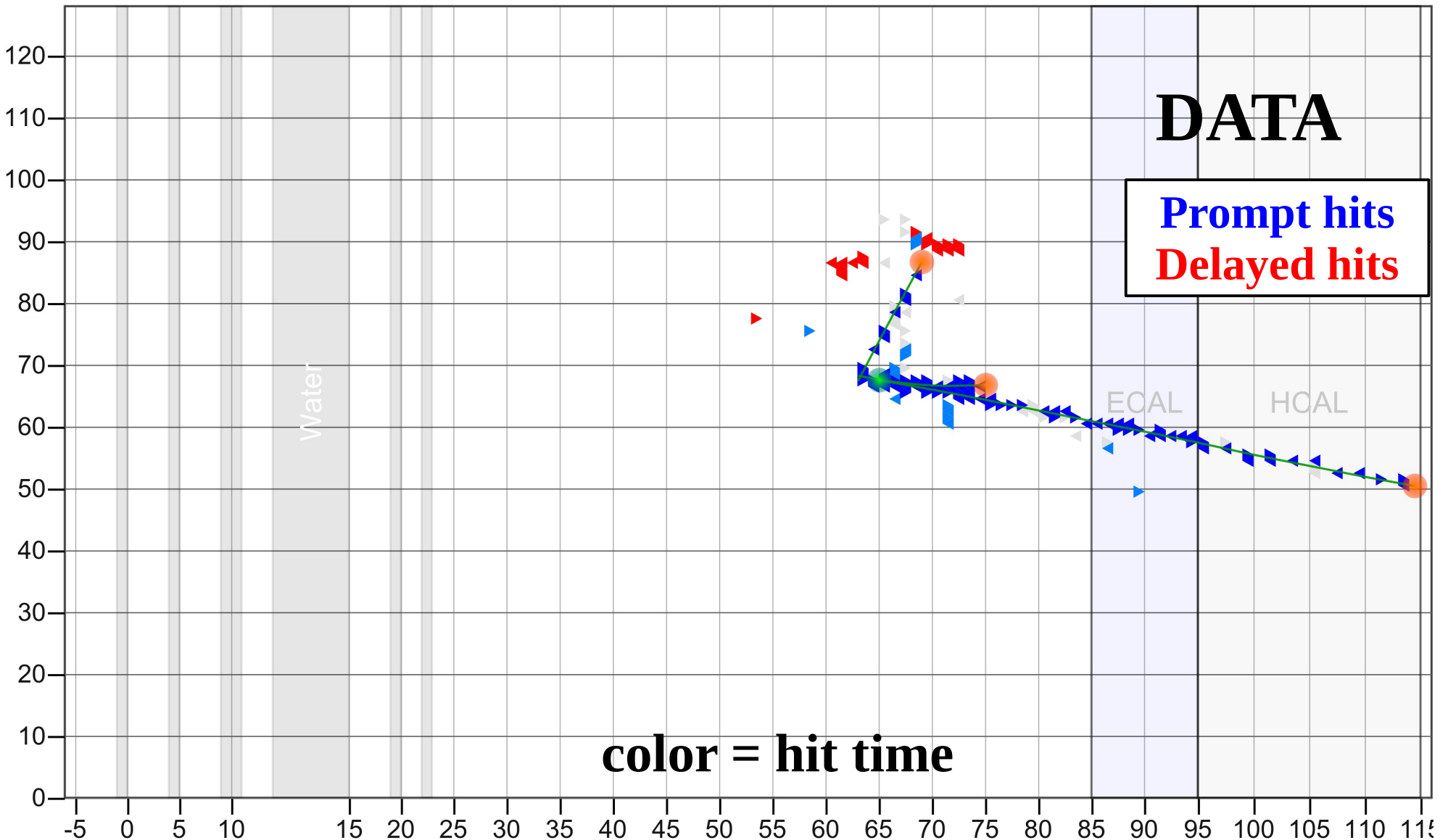
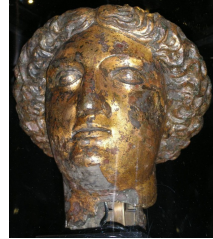


Reconstructing events without kinked tracks



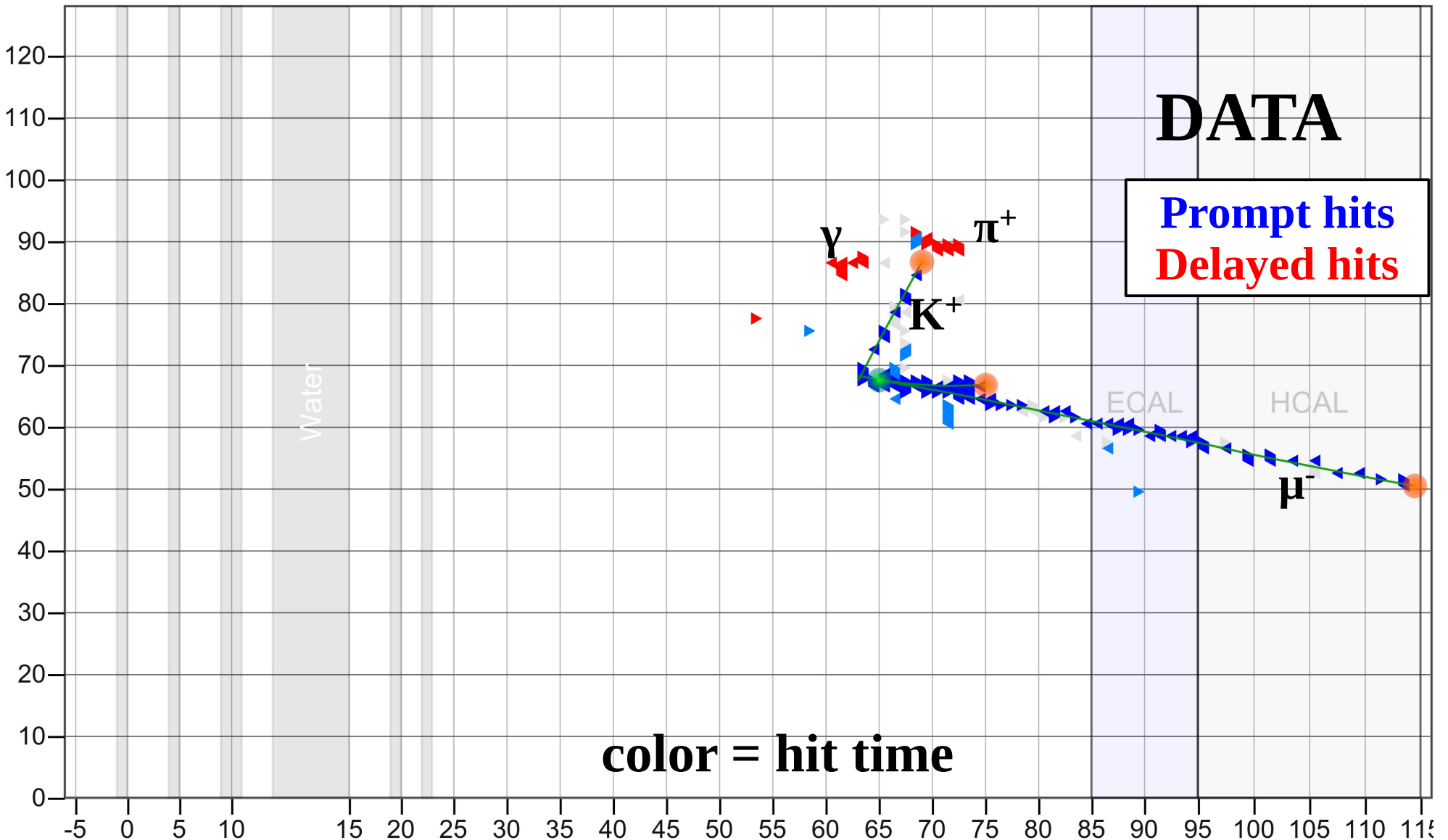
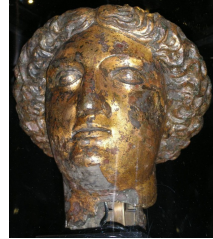


Hits are grouped into narrow bunches in time: “time slivers”



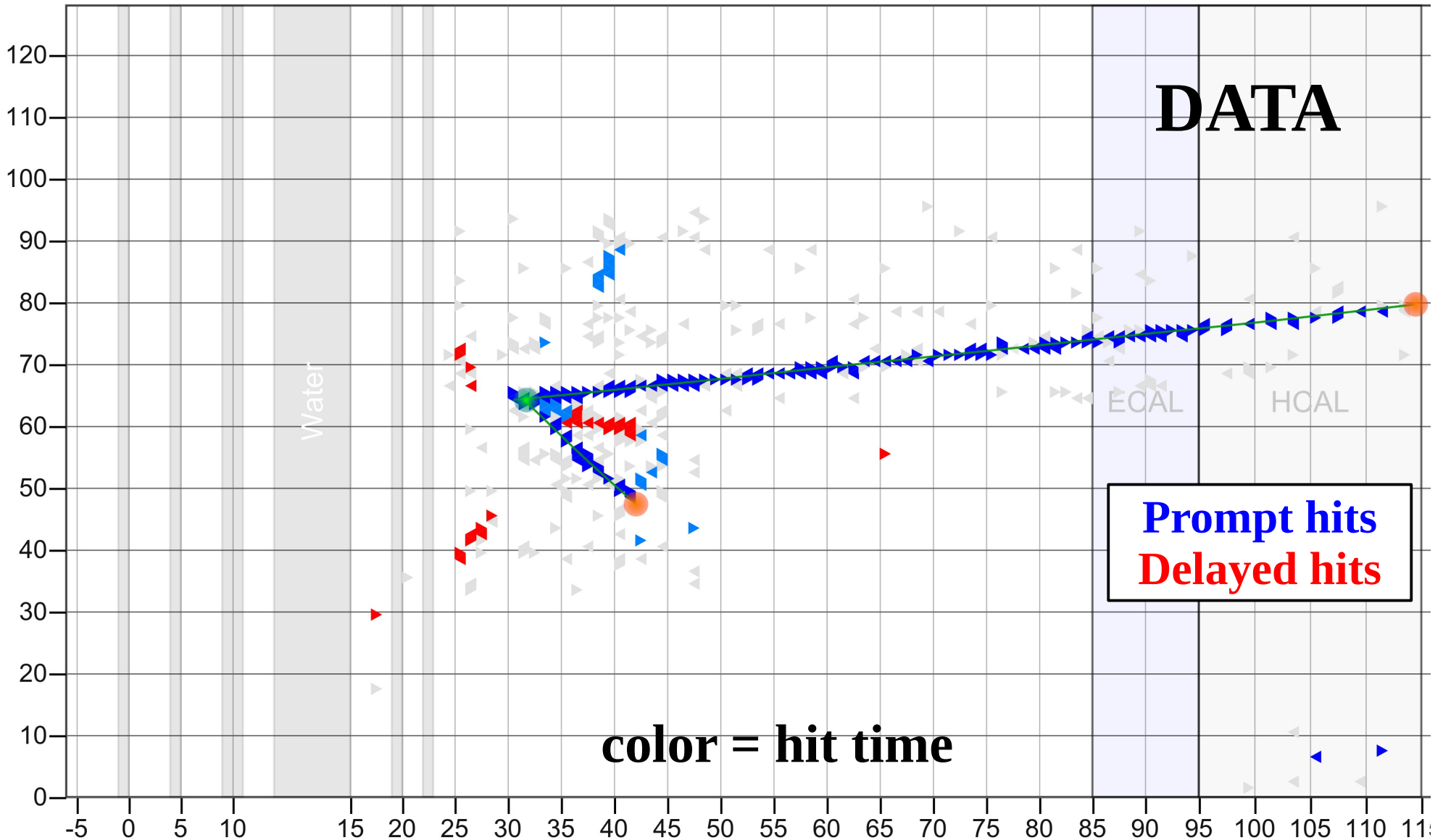
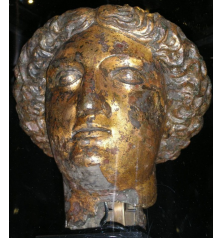


My guess



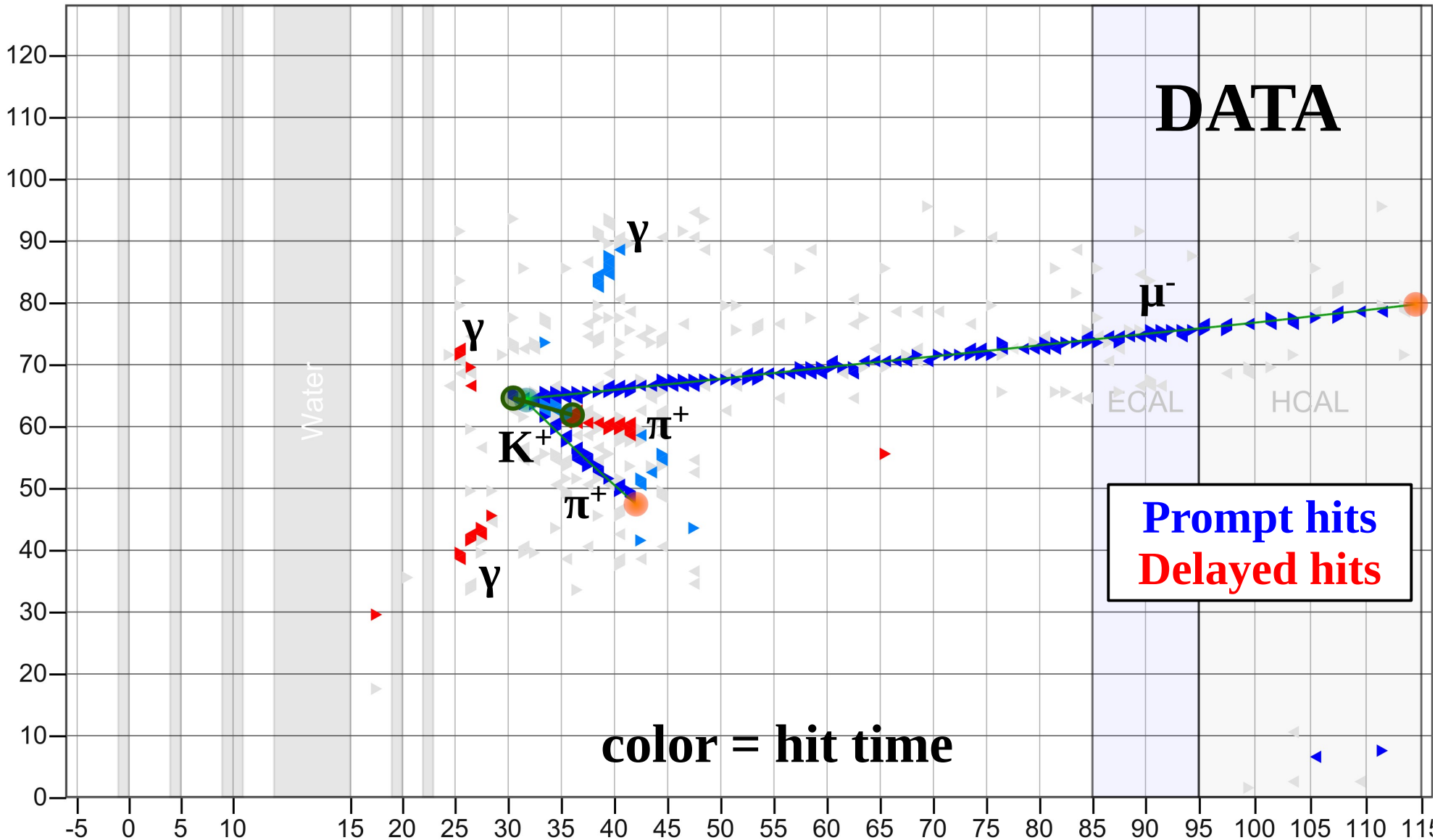
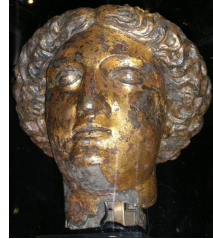


Reconstructing events with K^+ below tracking threshold



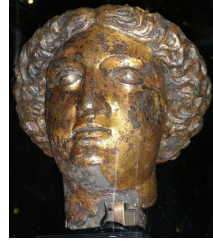


Reconstructing events with K^+ below tracking threshold

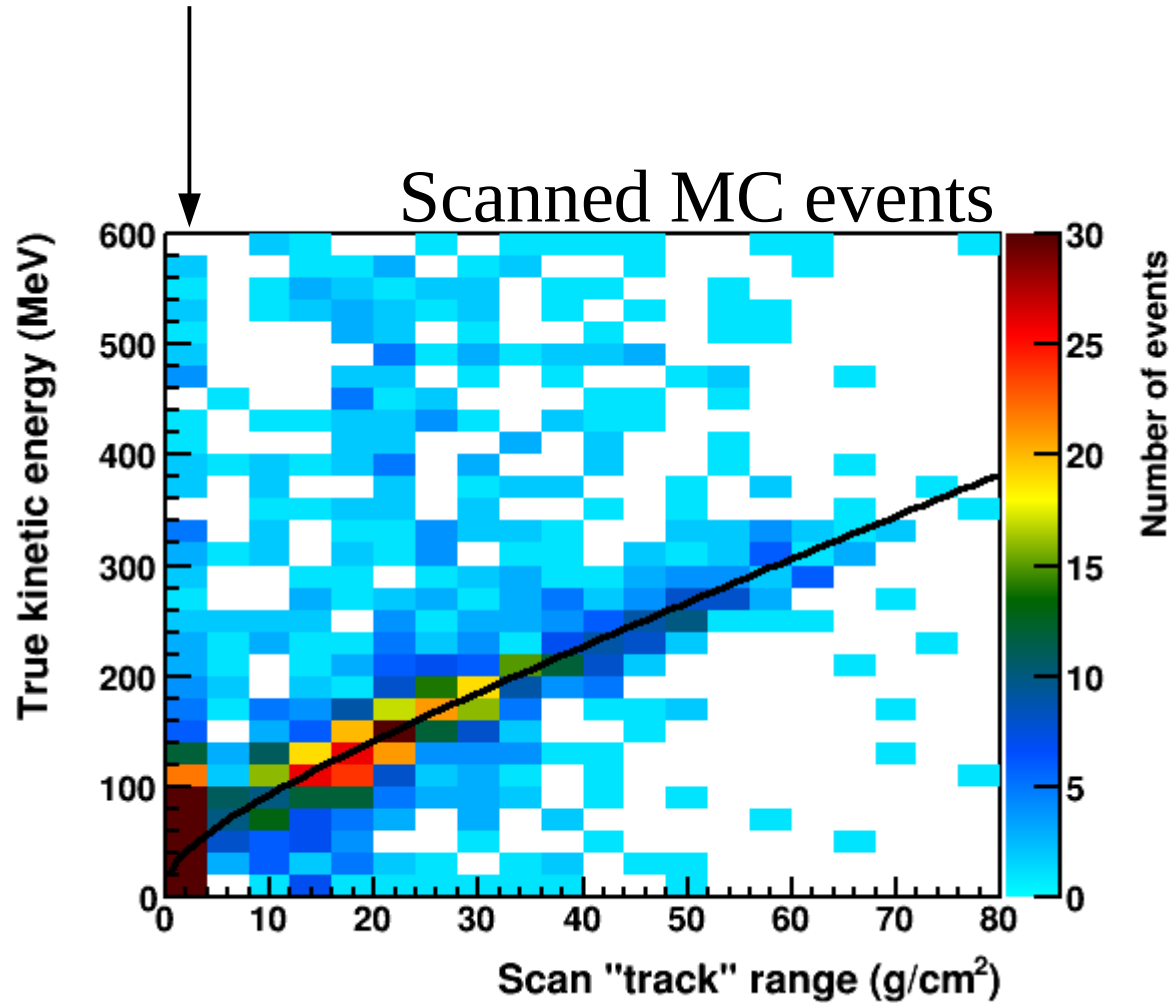




Use MC to convert range to kaon kinetic energy

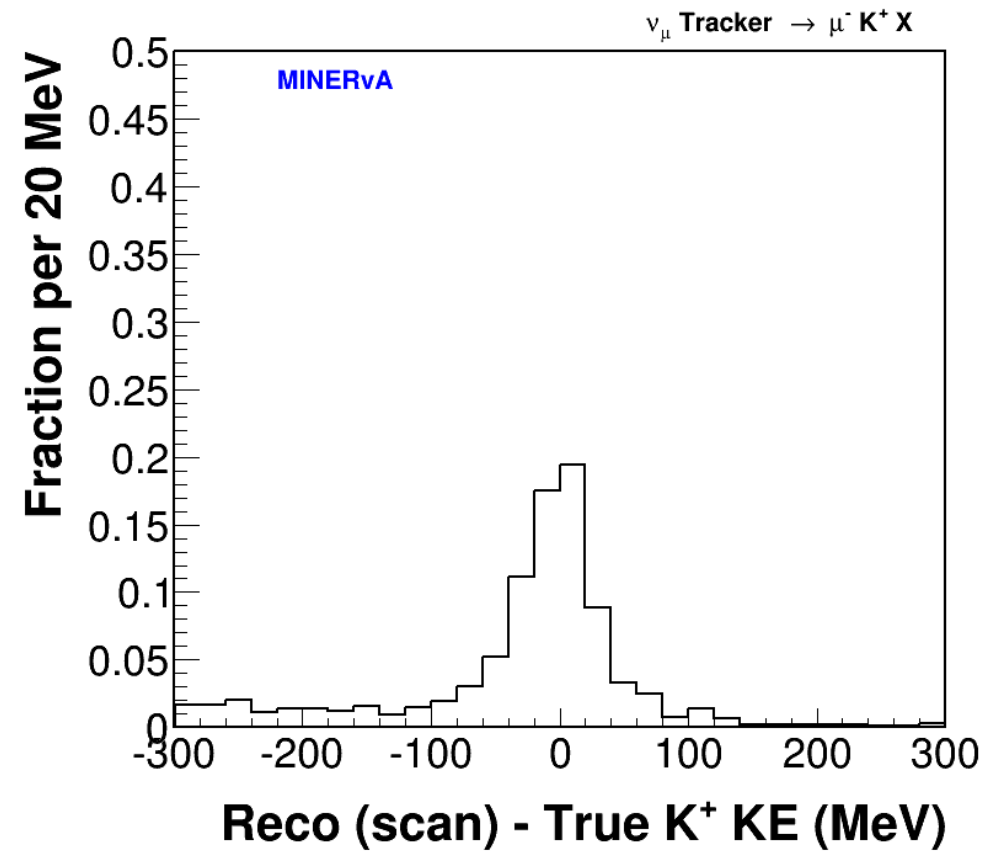
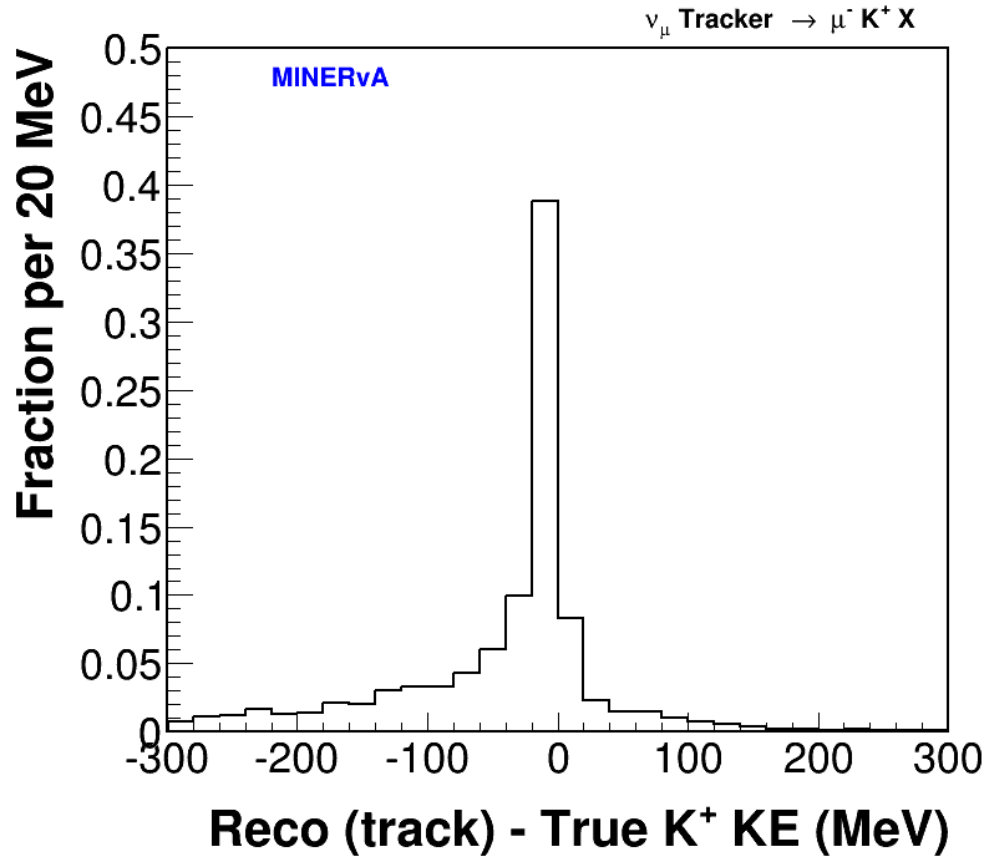
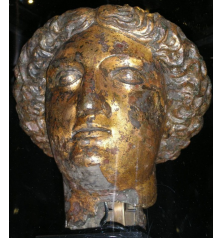


Too short to make a "User track"

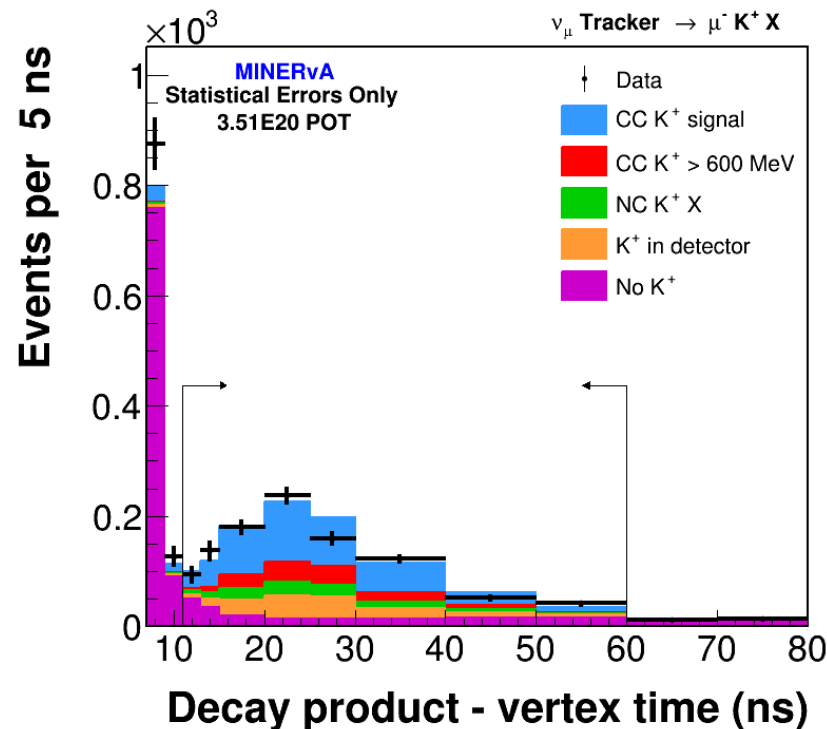
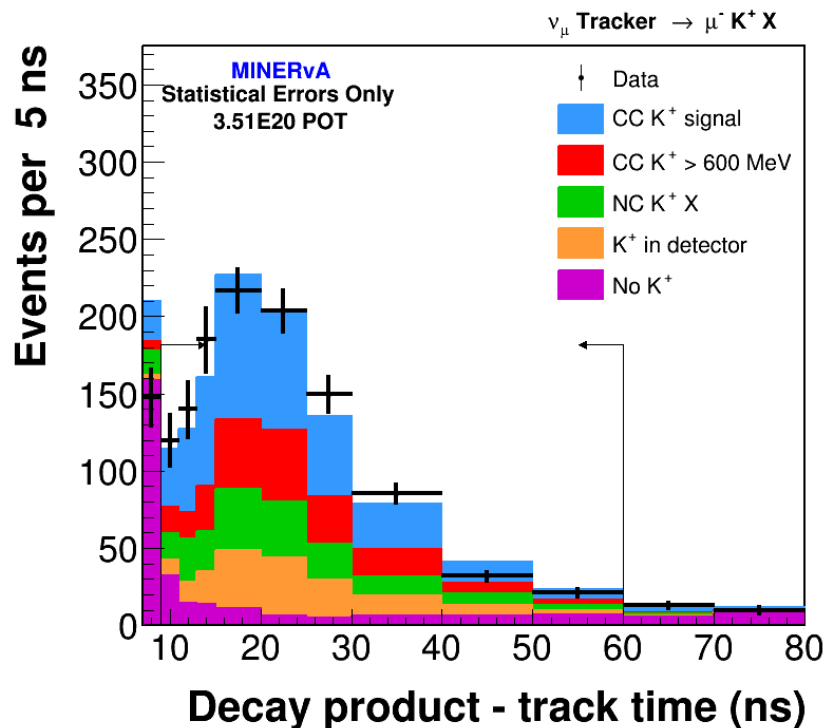
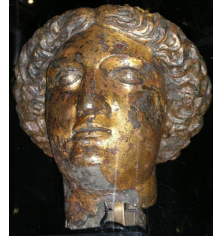




Kaon kinetic energy residuals

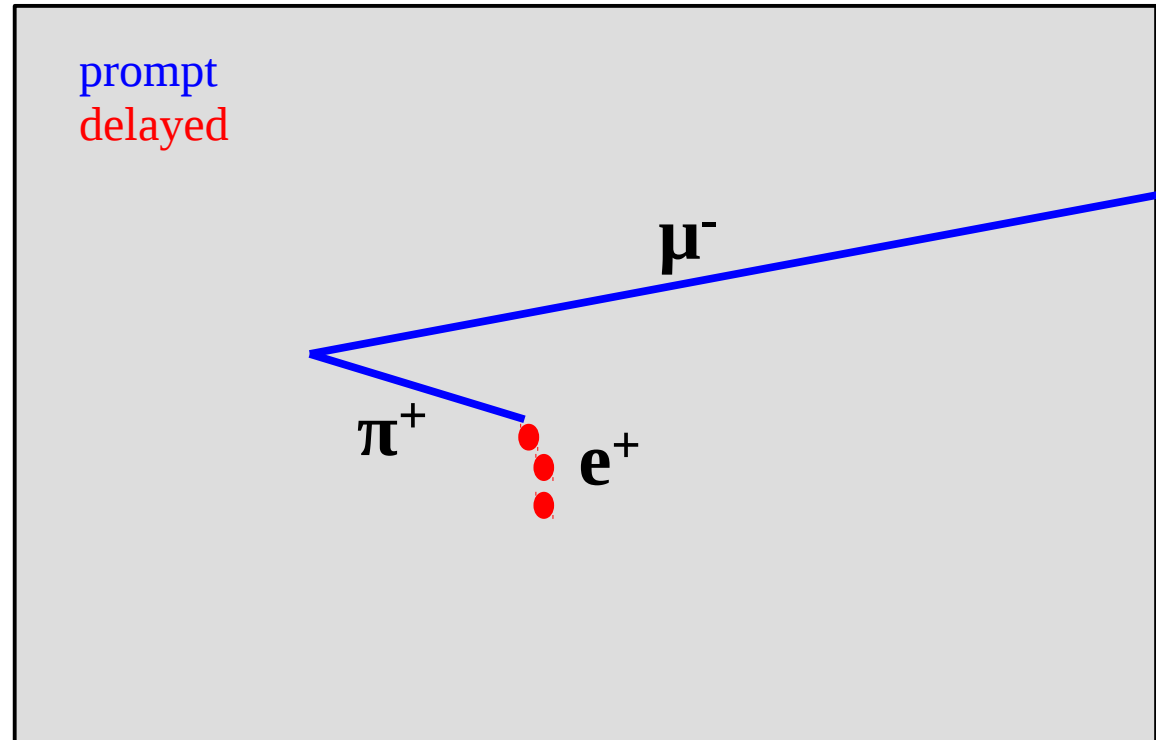
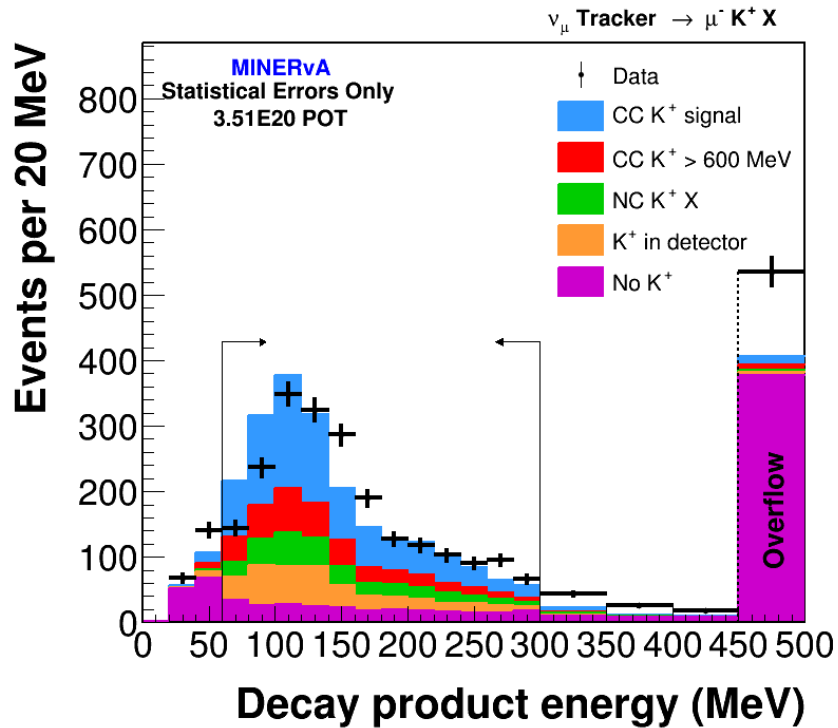
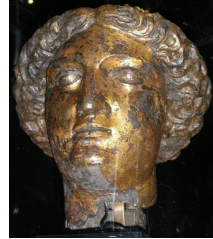


Time difference to decay



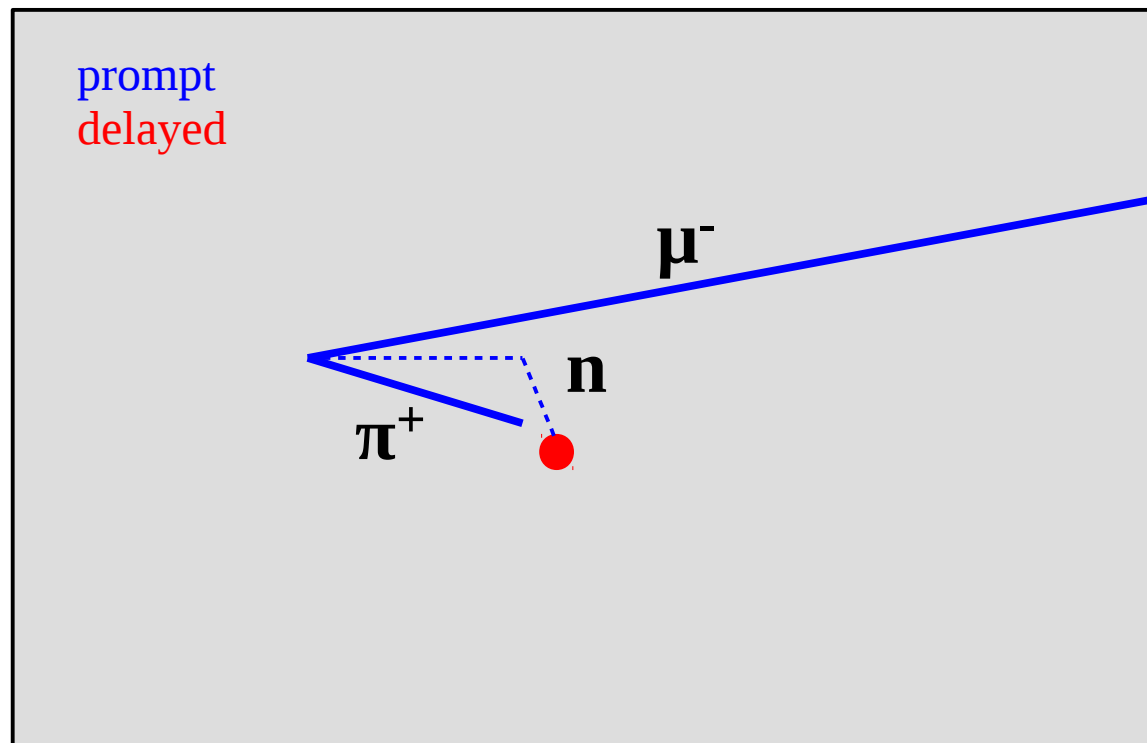
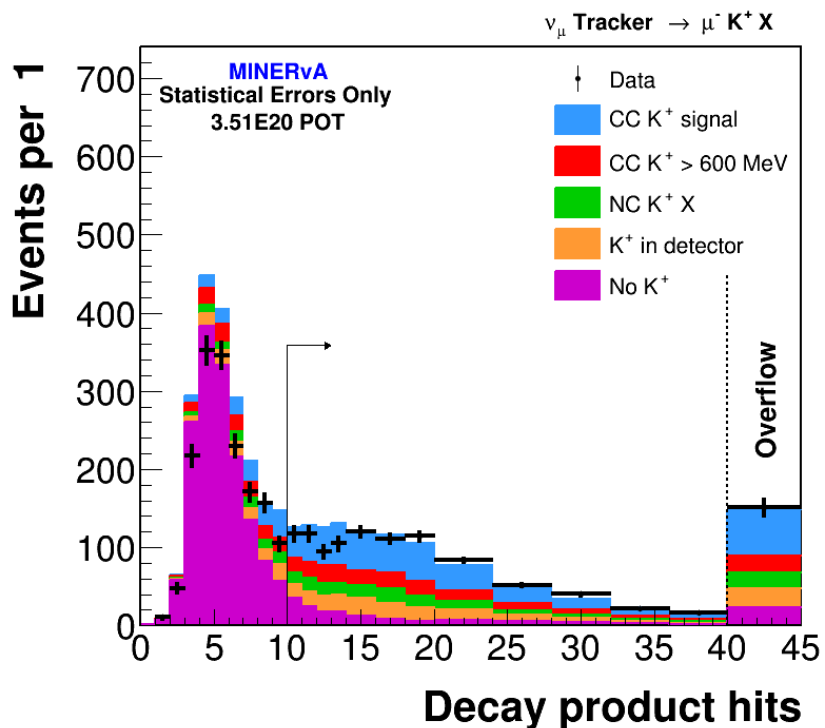
- Suppressing an enormous number of background events below 7 ns time gap

Decay candidate energy



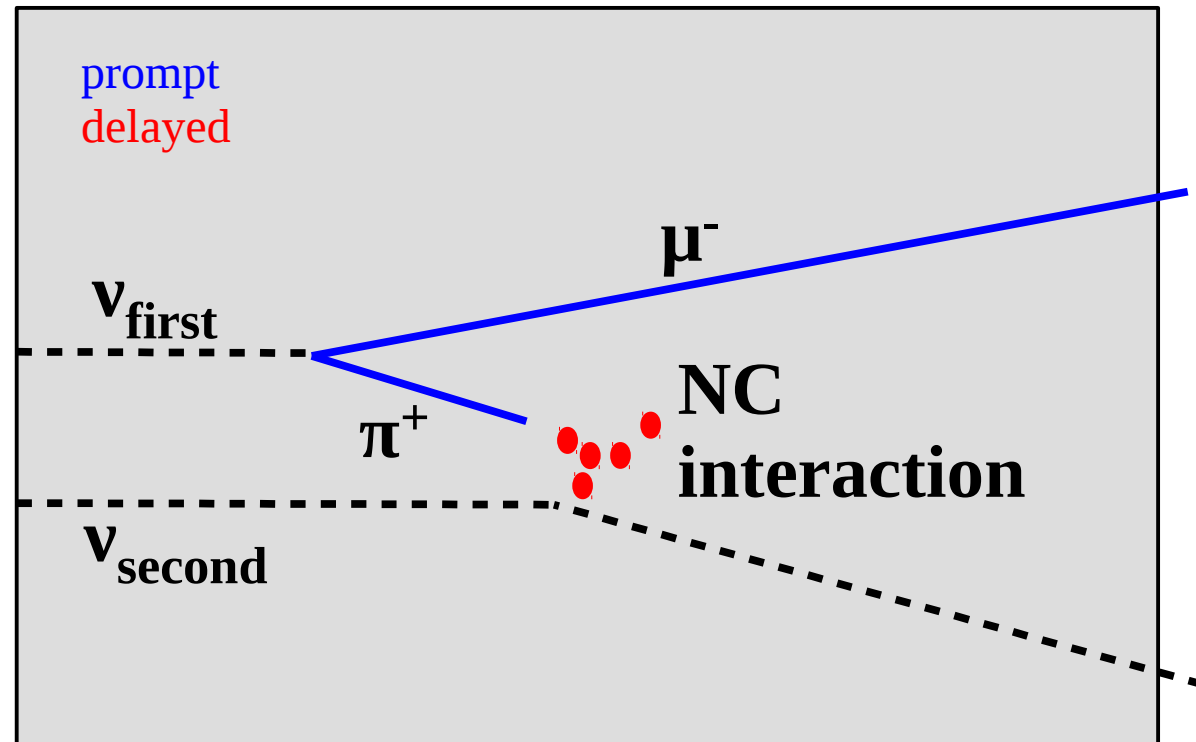
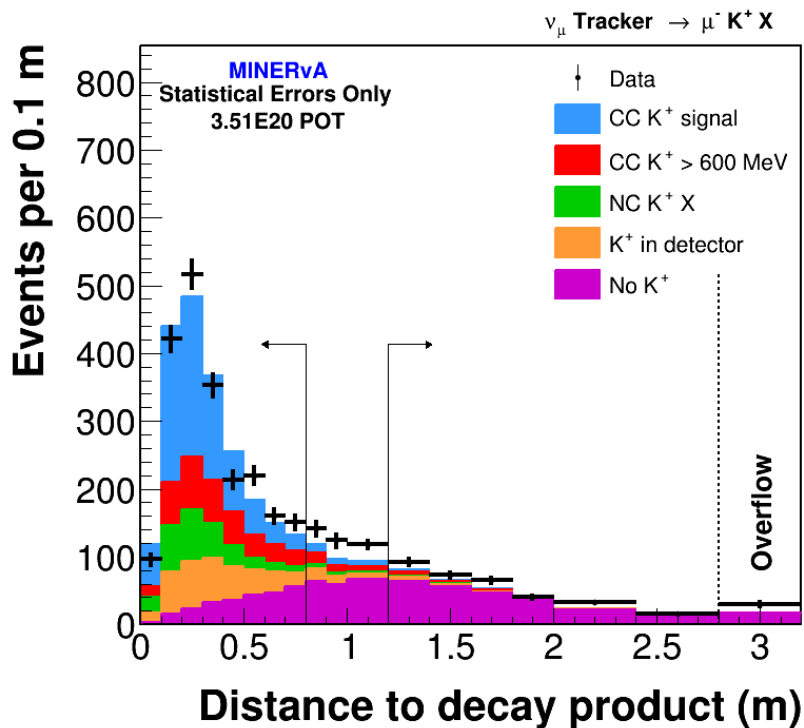
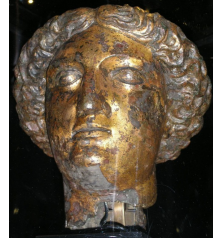
- Require energy to be consistent with $K^+ \rightarrow \mu^+ \nu$ or $K^+ \rightarrow \pi^+ \pi^0$

Decay number of hits



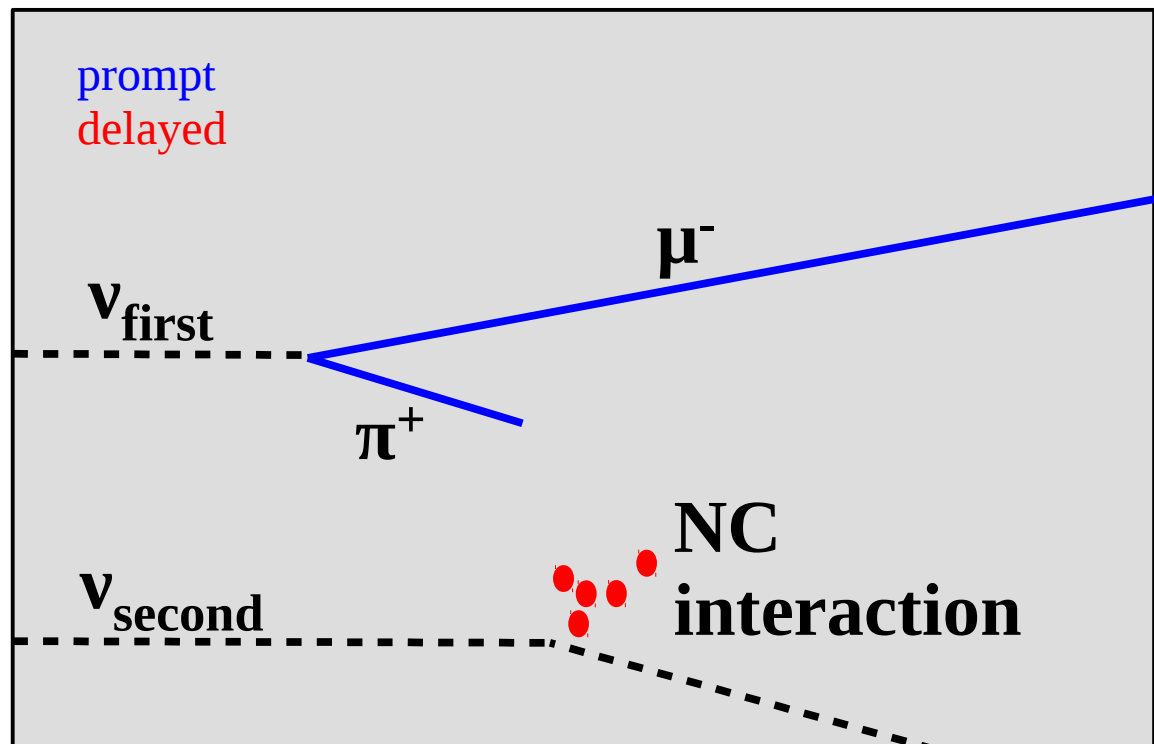
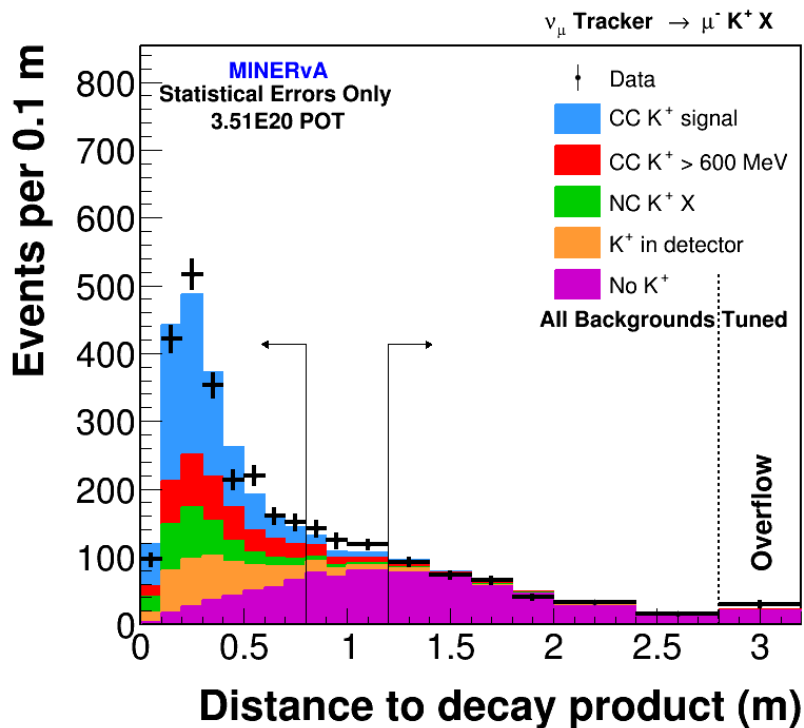
- Require at least 10 energy deposits (hits); neutron interaction will typically produce fewer

Distance to decay product



- Require decay product candidate to be spatially near the kaon track candidate

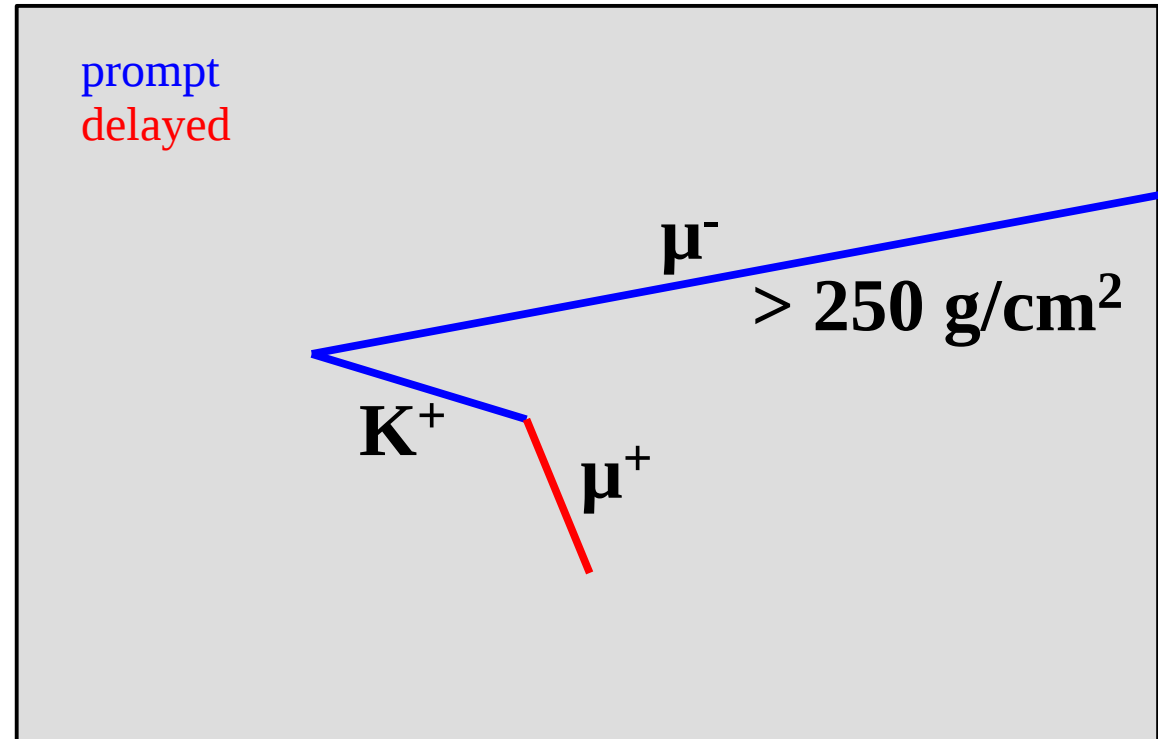
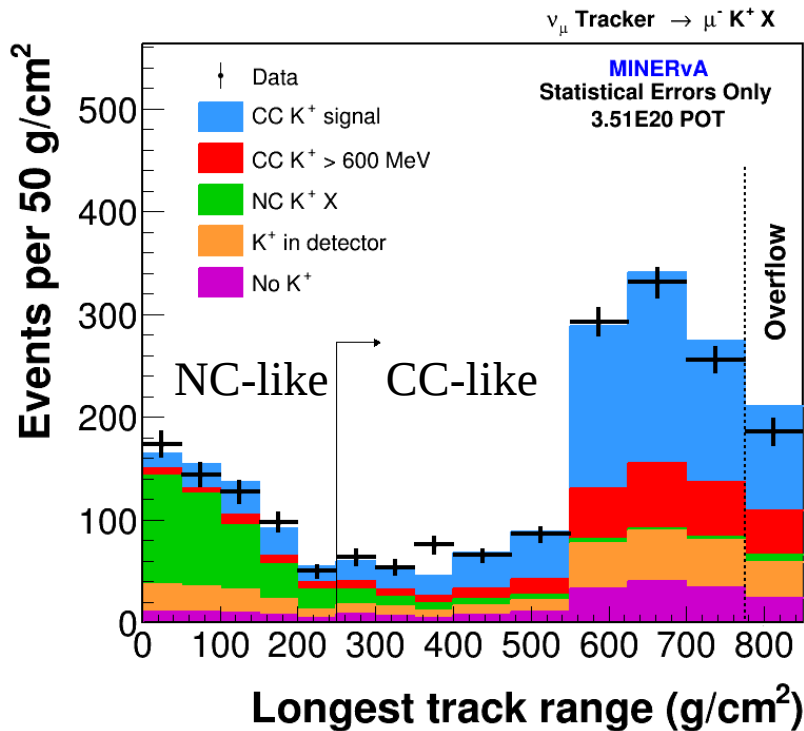
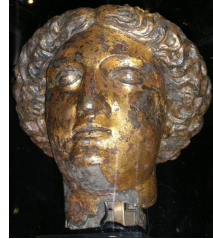
Tune the pile-up background



- Use events where the late activity is far from the kaon candidate to measure the pile-up background in data



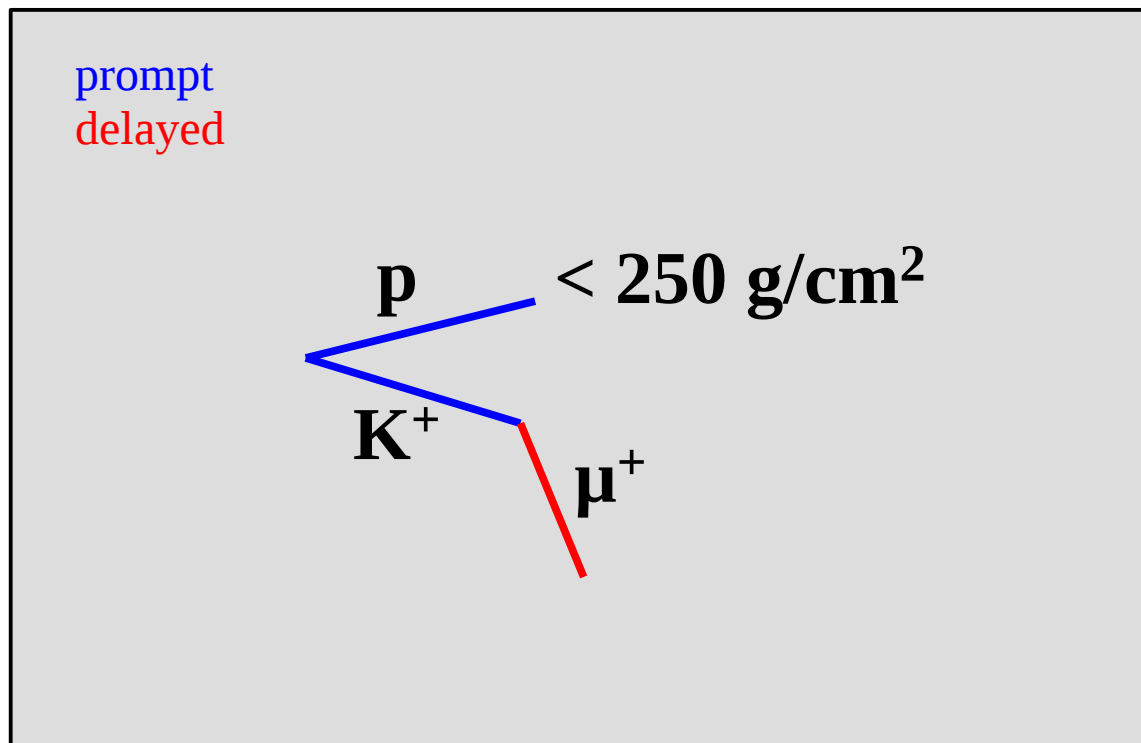
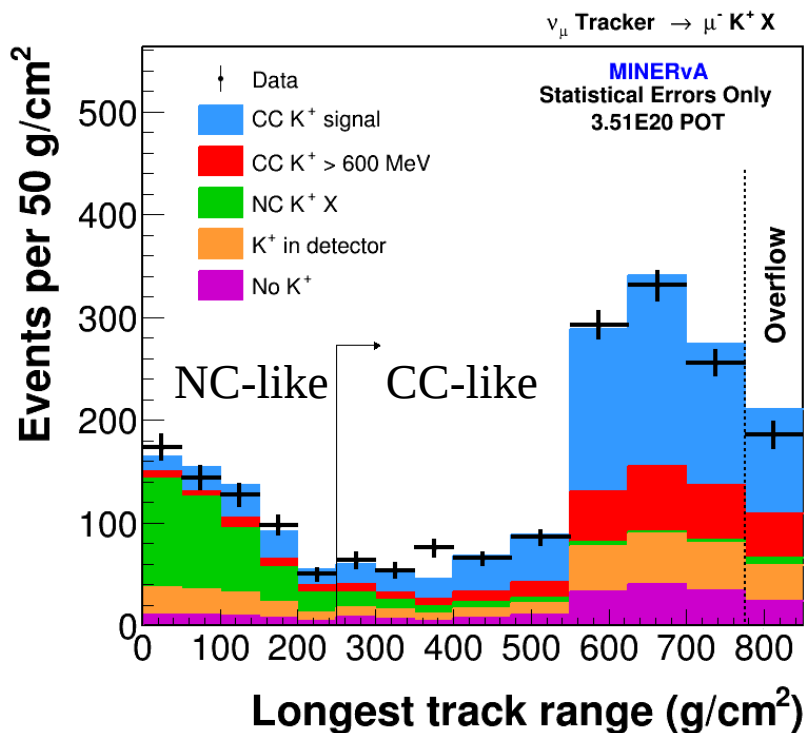
CC/NC separation



- For CC event, require a track to travel $> 250 \text{ g/cm}^2$



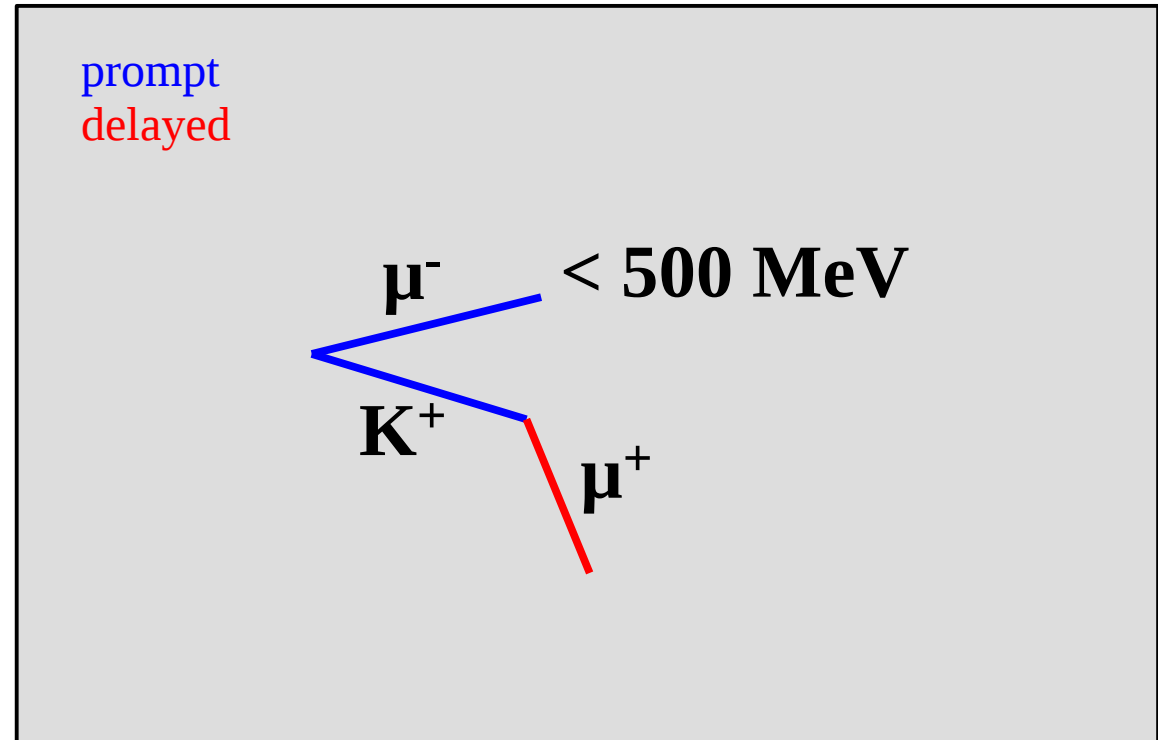
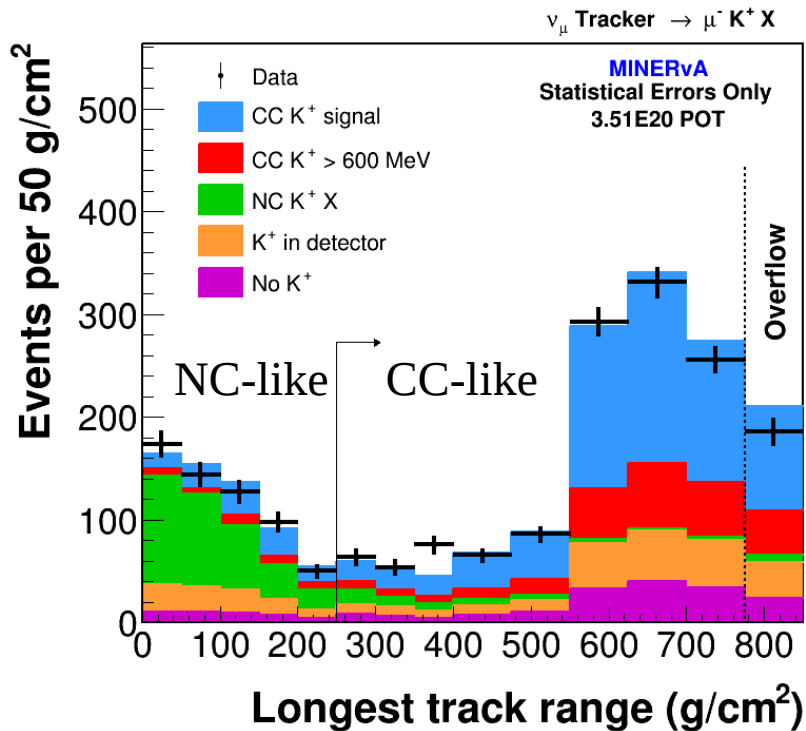
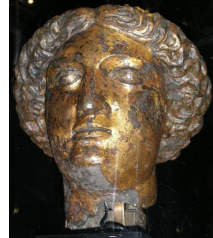
CC/NC separation



- Cut corresponds to ~ 3.1 nuclear interaction lengths
- Back of F.V. through calorimeters $\sim 550 \text{ g/cm}^2$



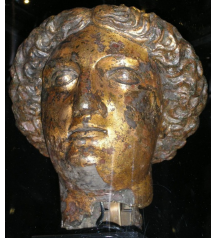
CC/NC separation



- Implicit cut on muon energy > 500 MeV for CC analysis
- Muon/pion separation at these energies is poor



We have come to a fork in the road



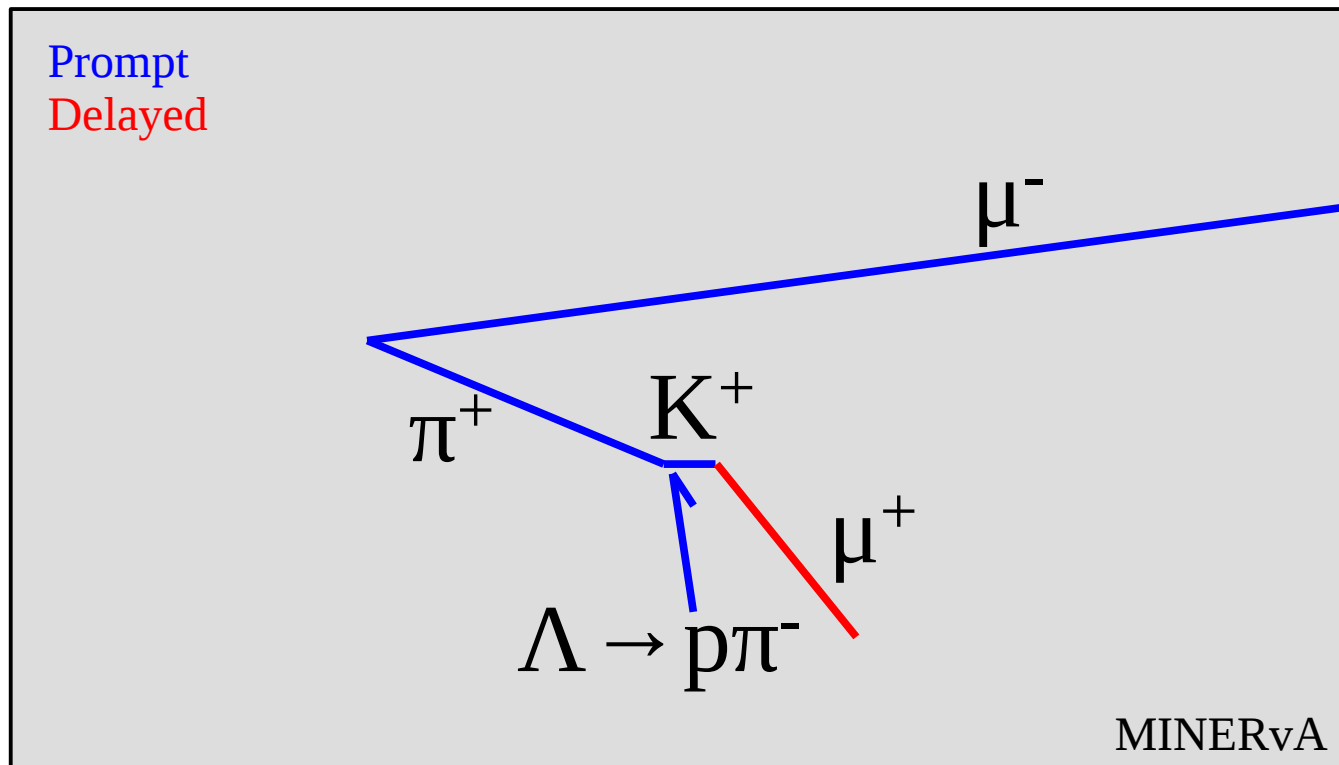
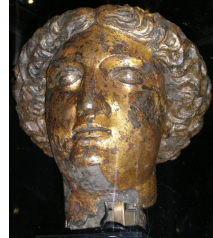
Now we have selected events with K^+

Cross section extraction is qualitatively similar for CC
and NC analyses:

We will follow the CC “path”



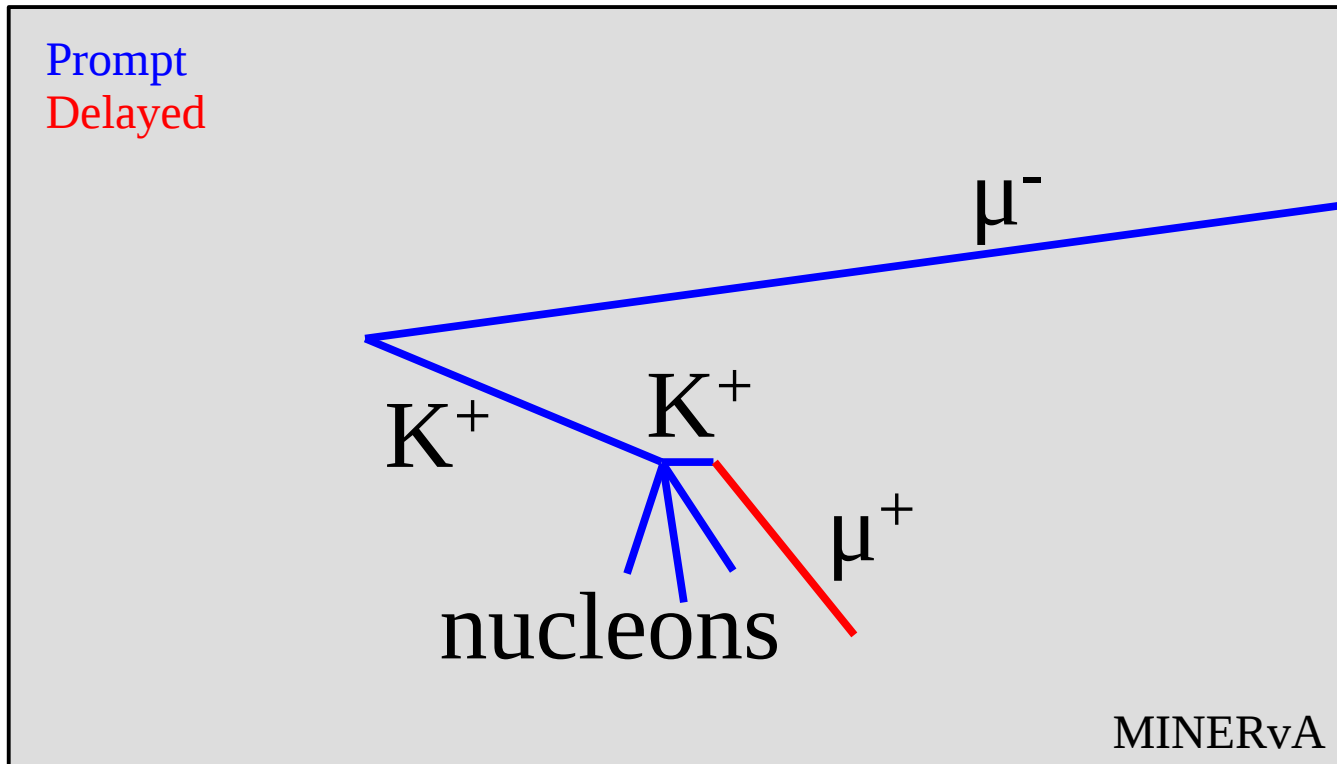
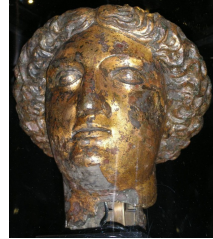
Troublesome event #1



- Pion interactions that produce kaons inside the detector, but outside the target nucleus, are a background

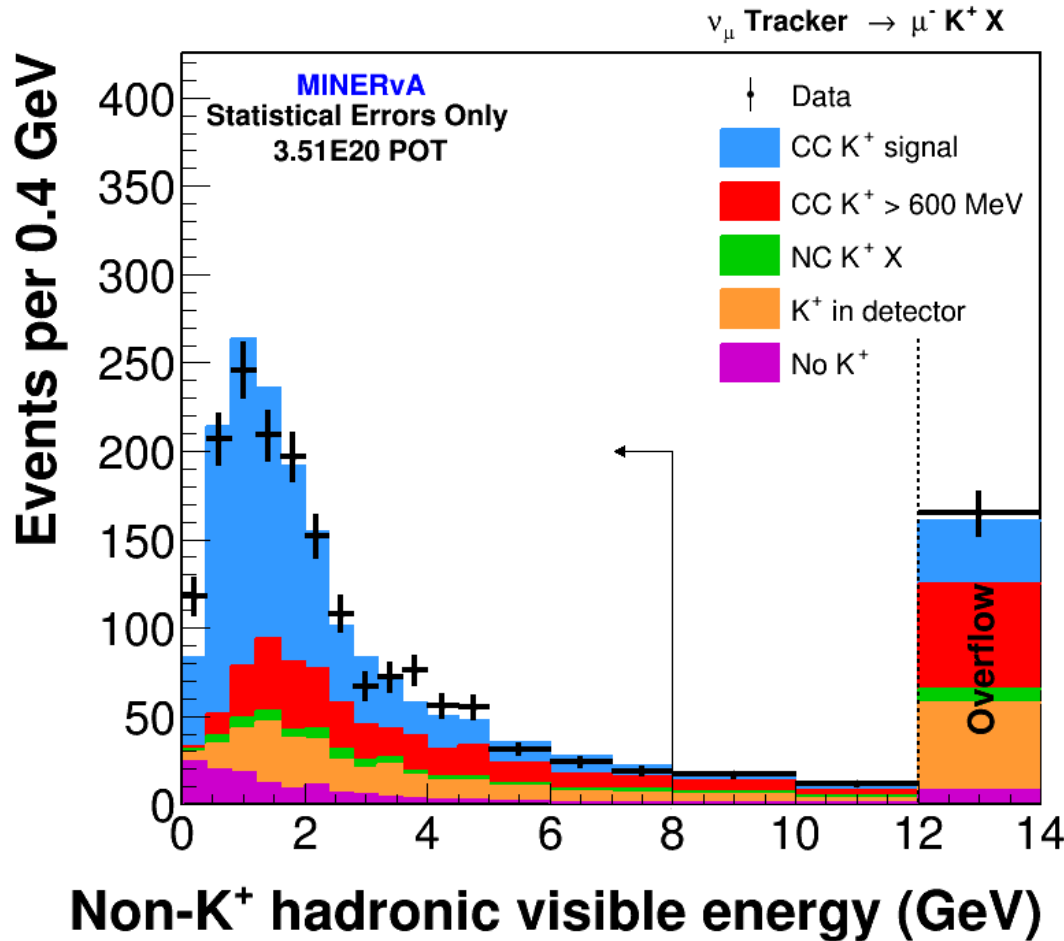
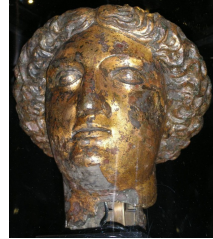


Troublesome event #2



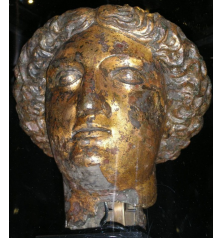
- High-energy kaons ($KE > 0.6 \text{ GeV}$) that interact in the detector have badly misreconstructed energies

Constraining high-energy kaons and $\pi \rightarrow K$ in detector events

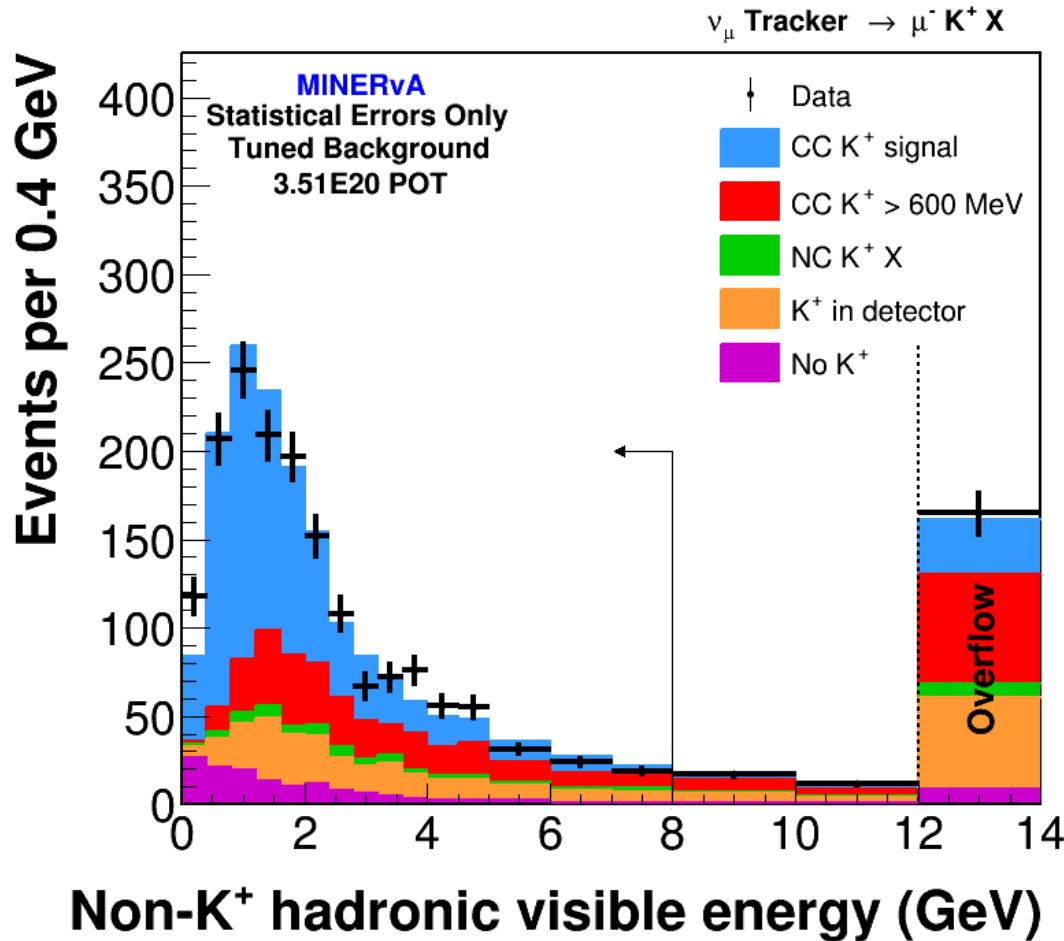


- Events with interactions have high visible energy in the detector
- Use sideband of very high hadronic visible energy

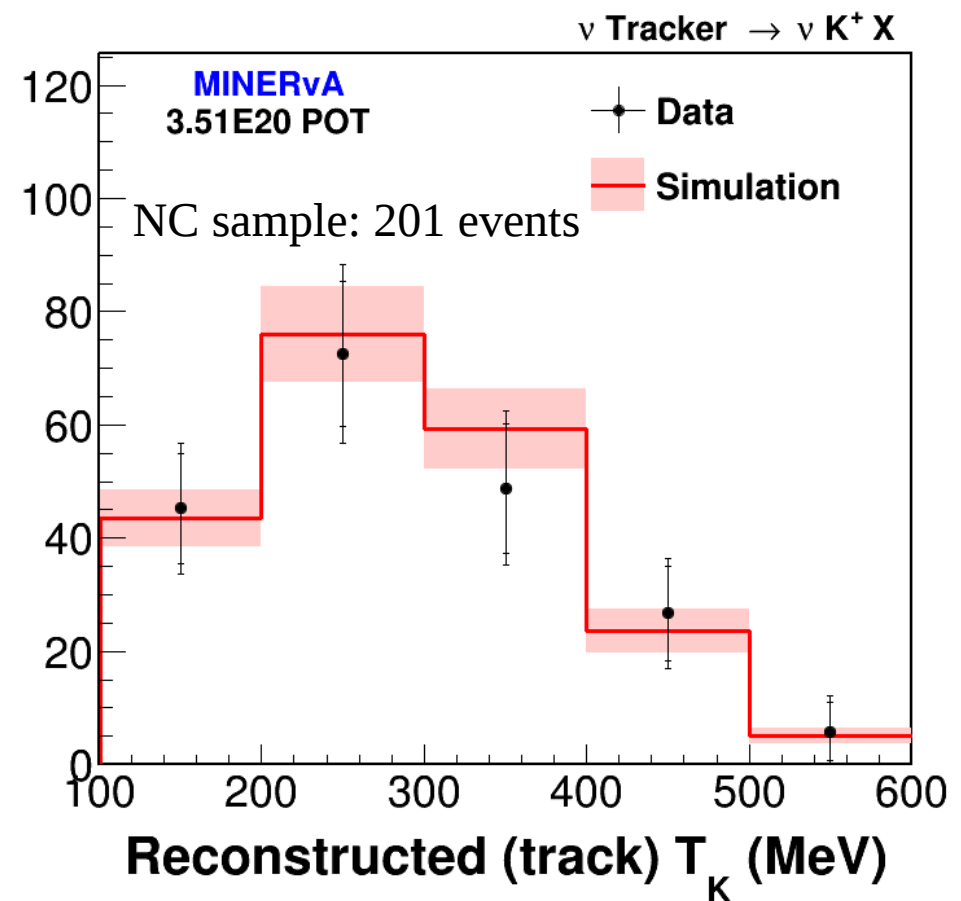
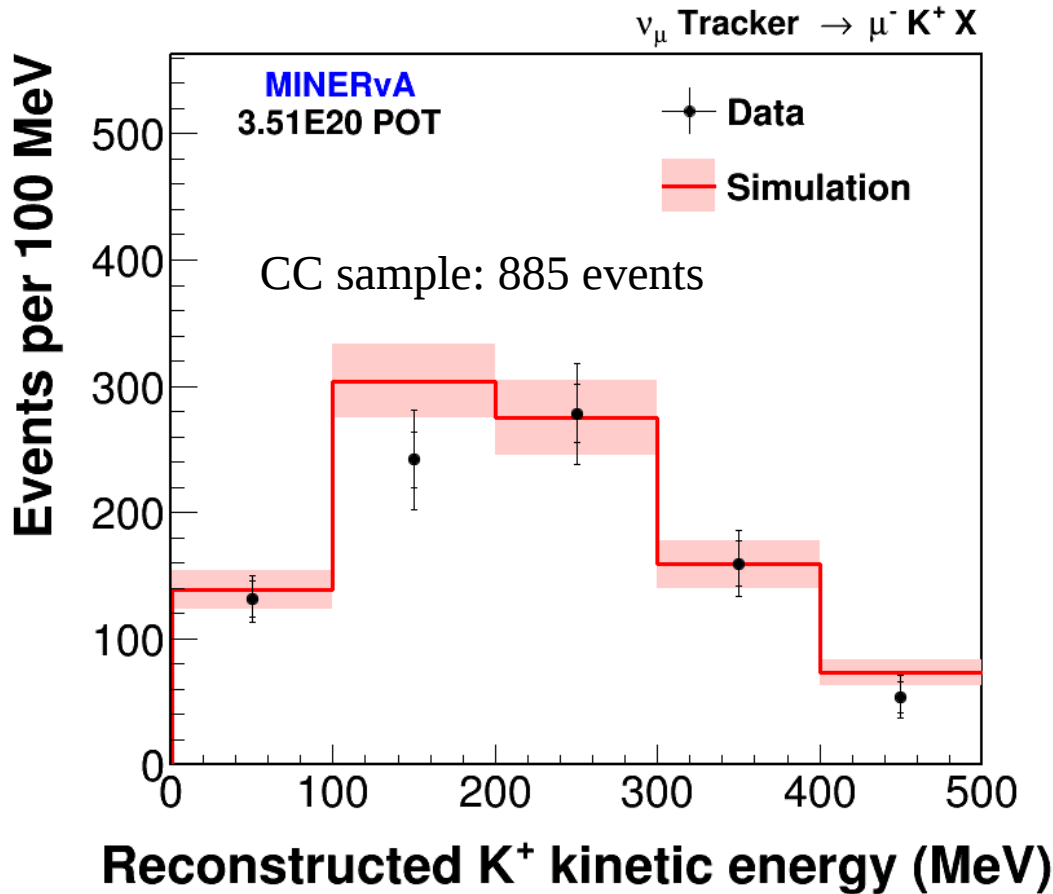
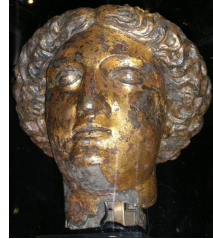
Tune the background



- Constrain the high-energy kaons, and kaons from pion interactions together



Sample sizes after background subtraction



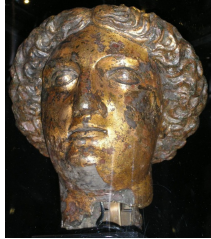


The big picture



- Motivation for studying K^+ production by neutrinos
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Extracting a cross section



differential cross section in true bin i

unsmearing matrix

observed events in reconstructed bin j

$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

integrated flux

number of targets

bin width

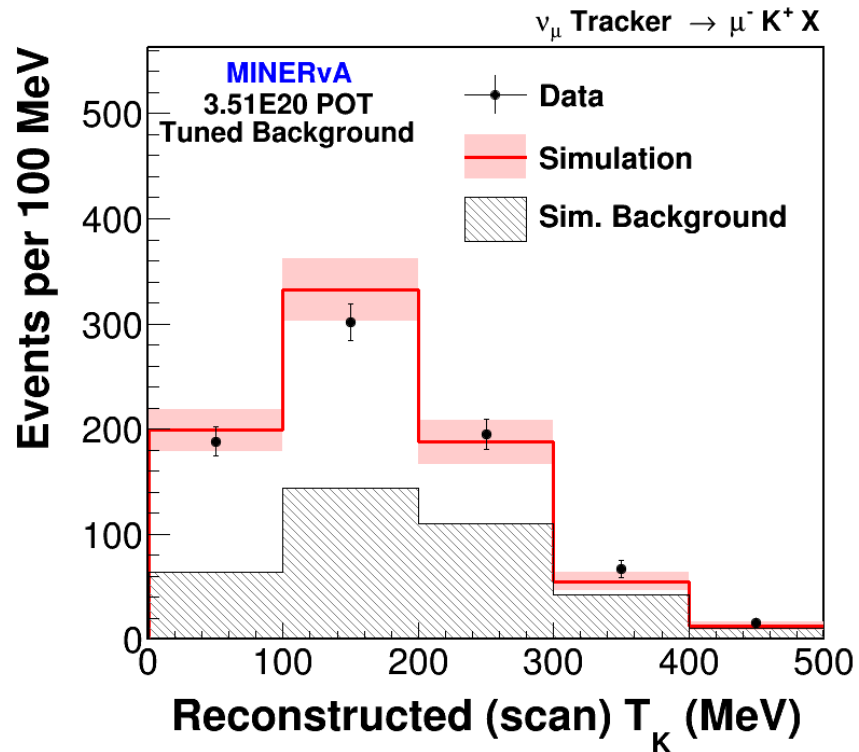
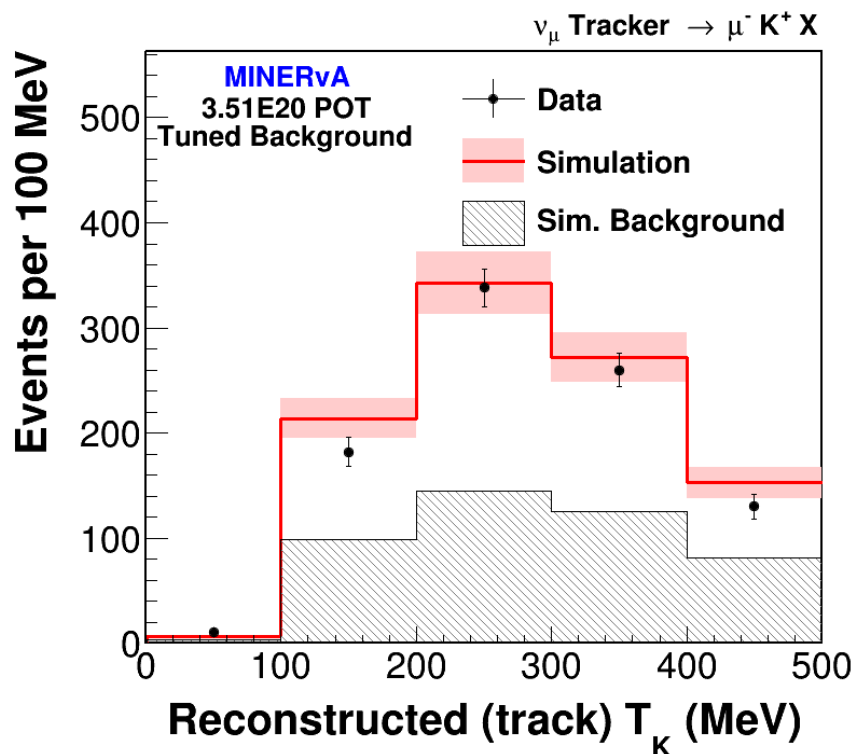
efficiency

predicted background

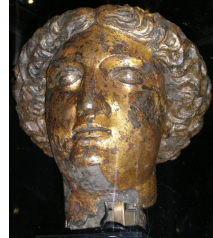
Extracting a cross section



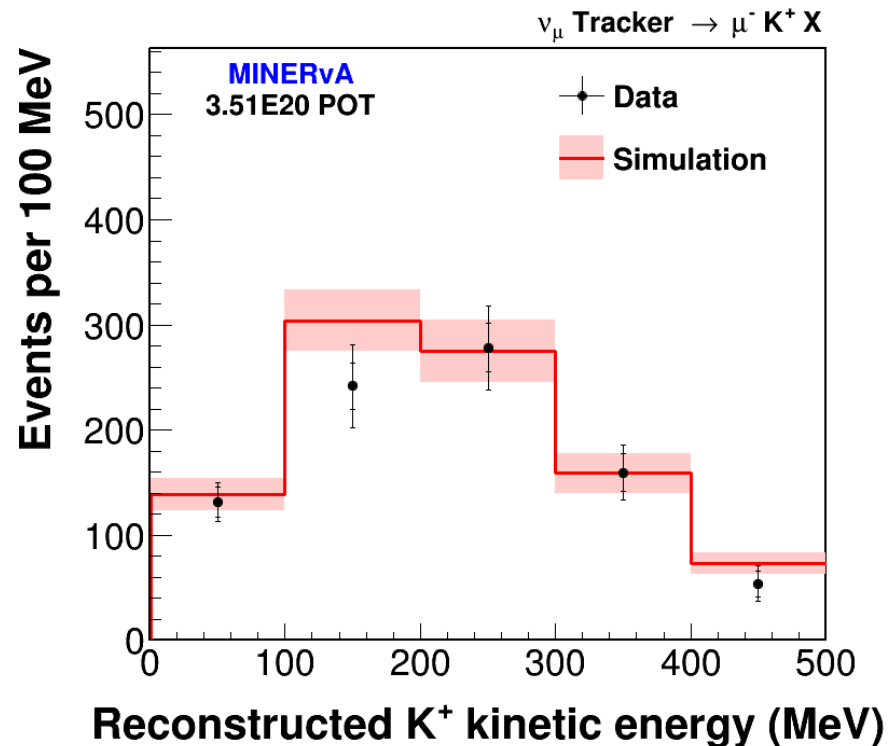
$$\left(\frac{d\sigma}{d\xi} \right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$



Extracting a cross section



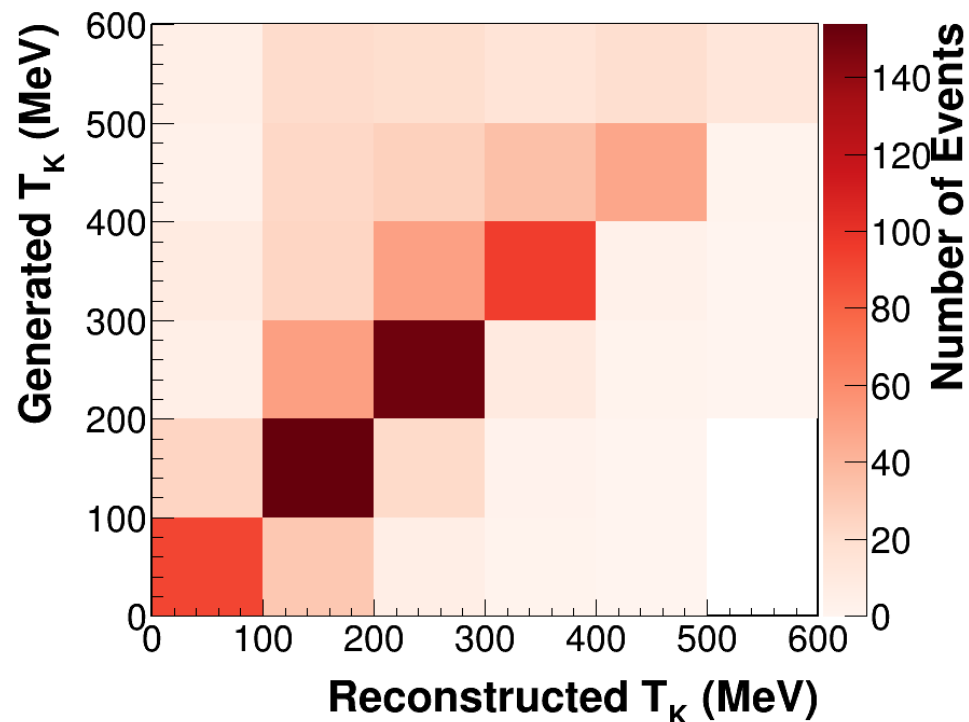
$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$



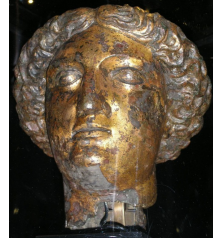
Extracting a cross section



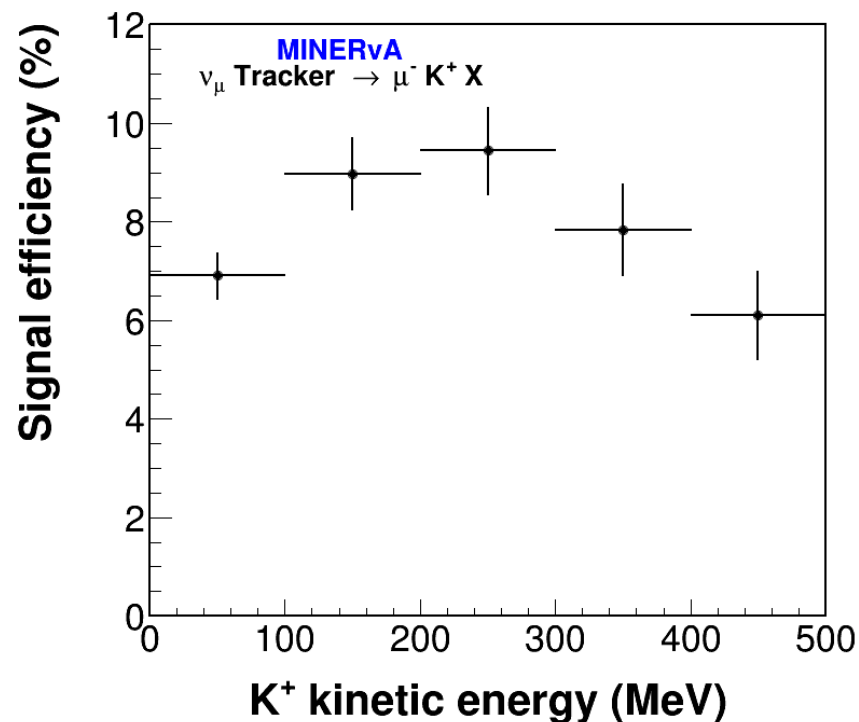
$$\left(\frac{d\sigma}{d\xi} \right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$



Extracting a cross section

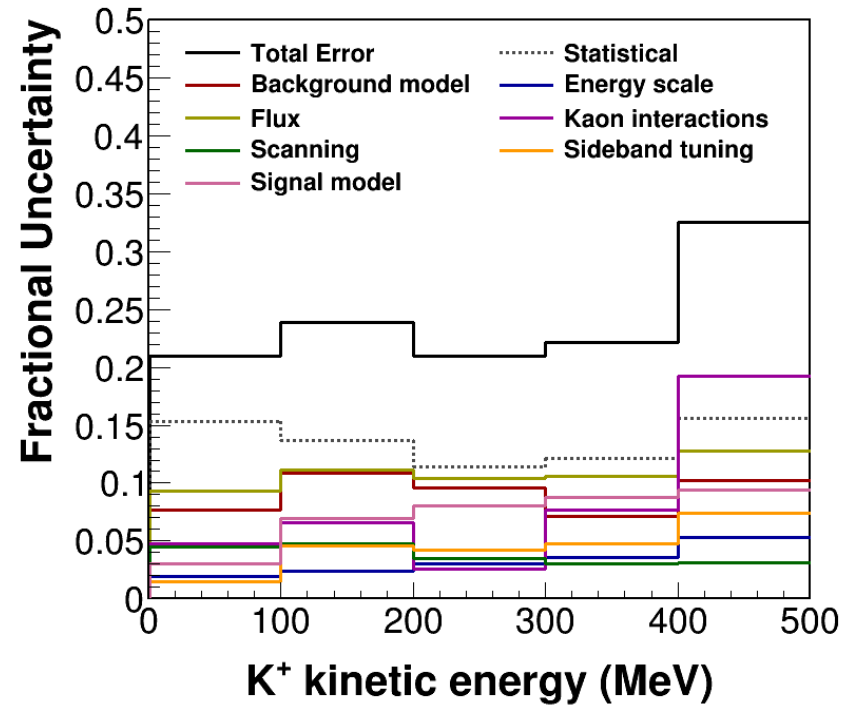
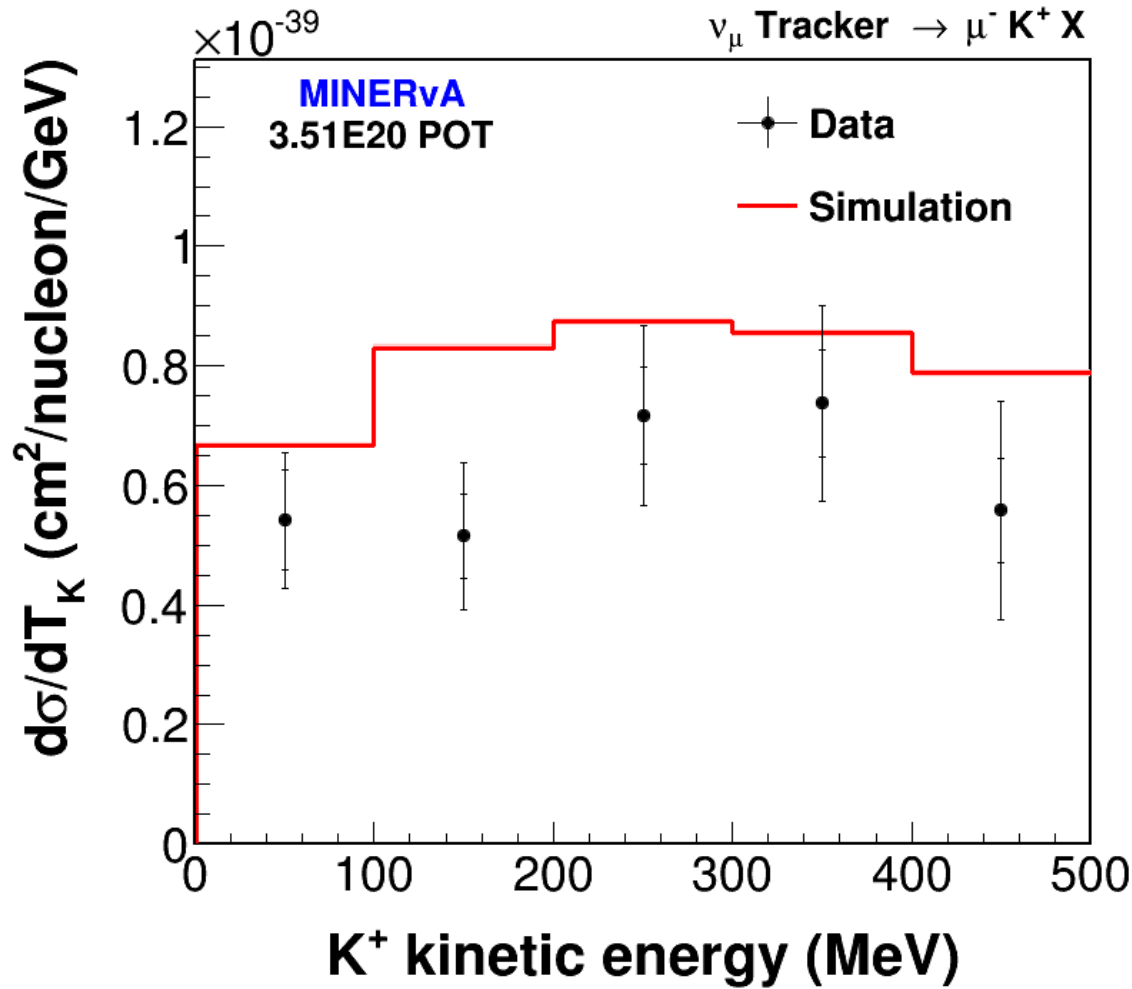
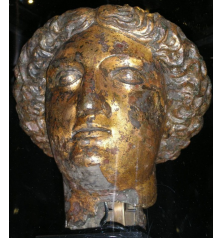


$$\left(\frac{d\sigma}{d\xi} \right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

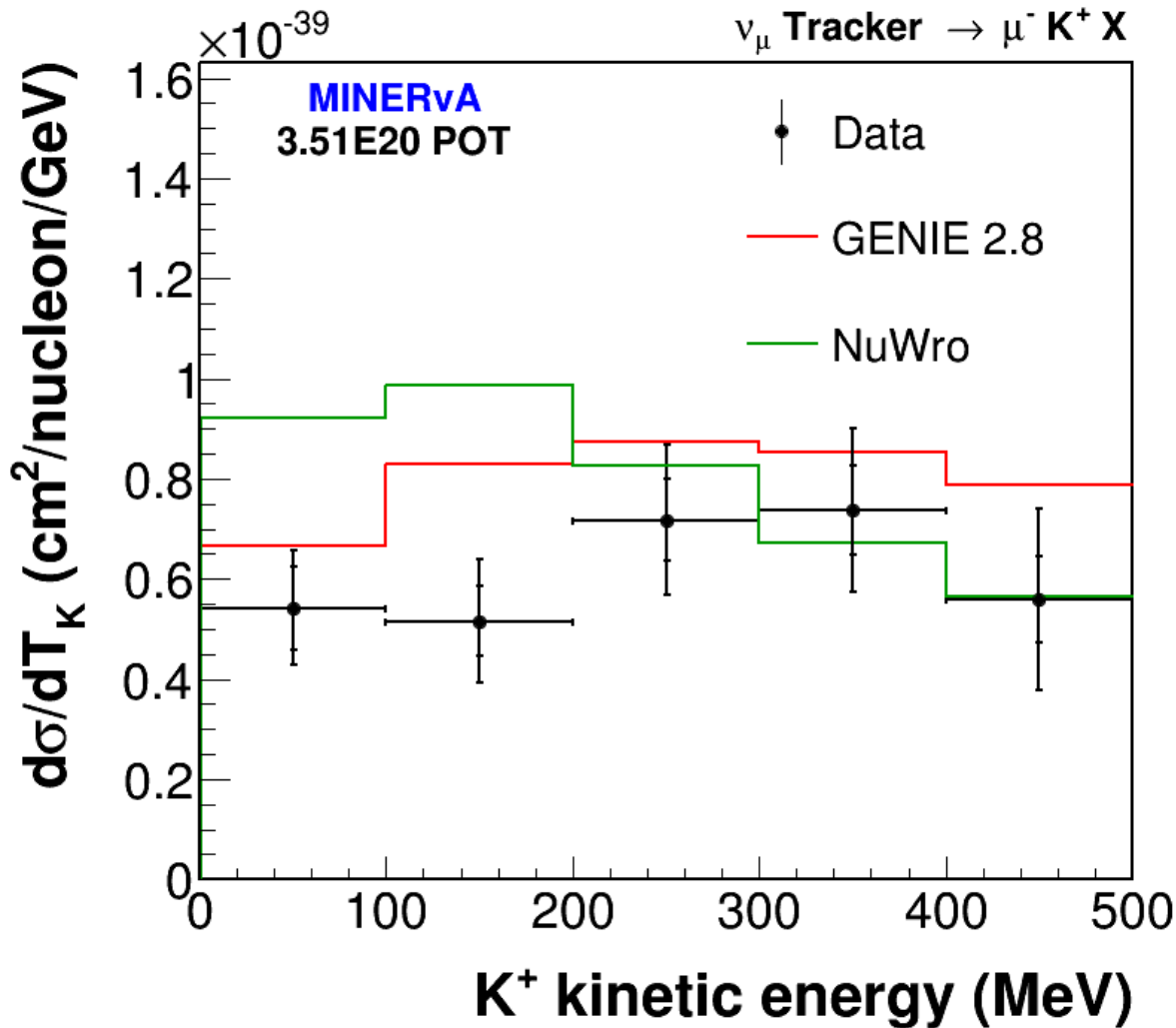
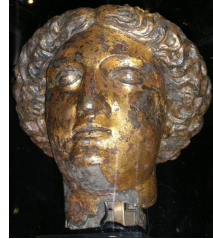




Cross section: good agreement with GENIE



Data disfavors NuWro



- Kaons in NuWro come only from hadronization (PYTHIA)
- Shape is inconsistent with NuWro at low energy

Go back to the fork



NC cross section extraction is qualitatively similar

Skip to the results instead



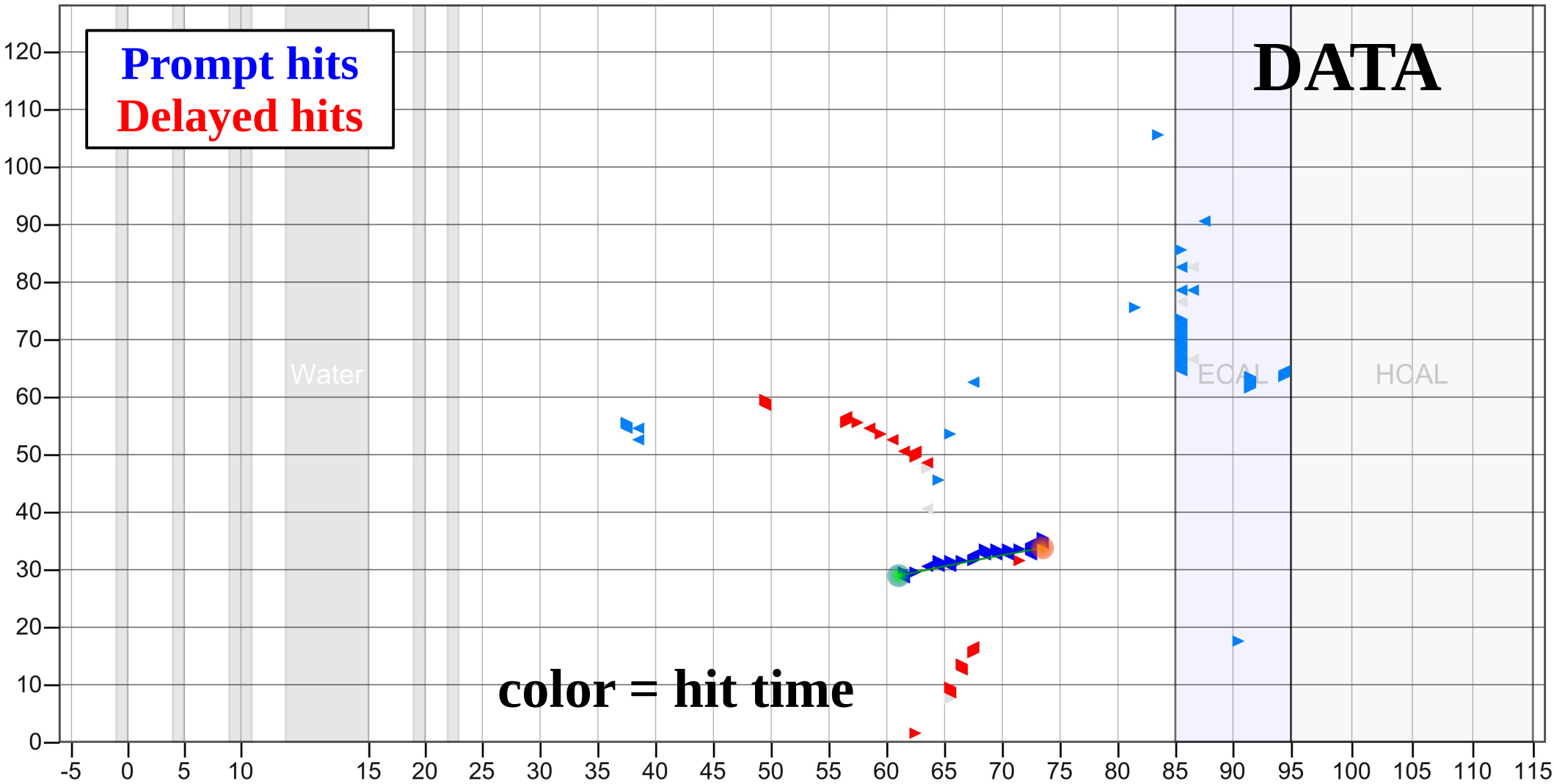
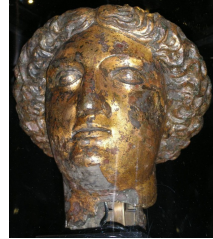
The big picture



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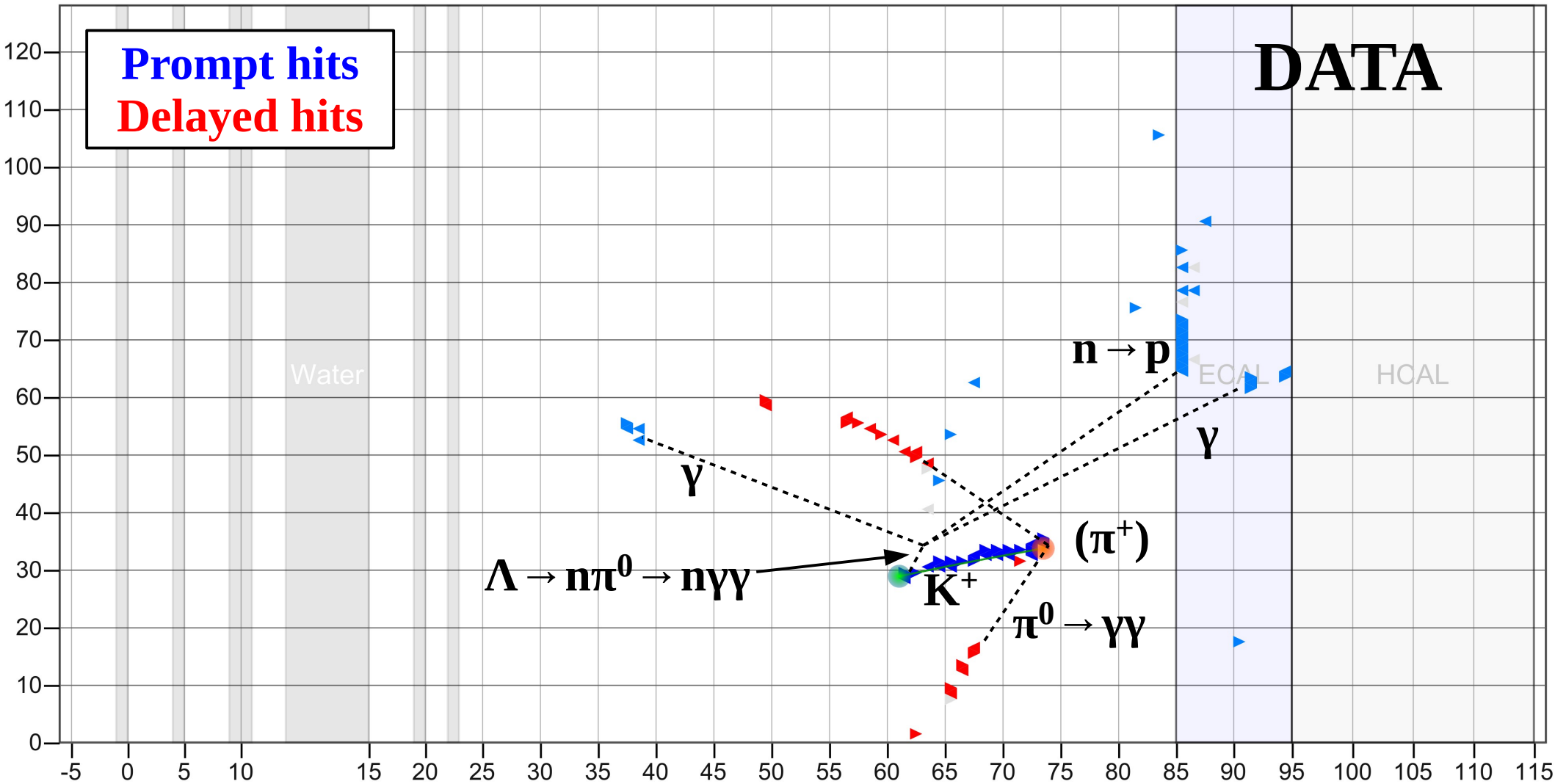
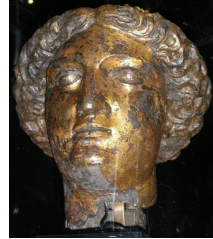


Neutral current event



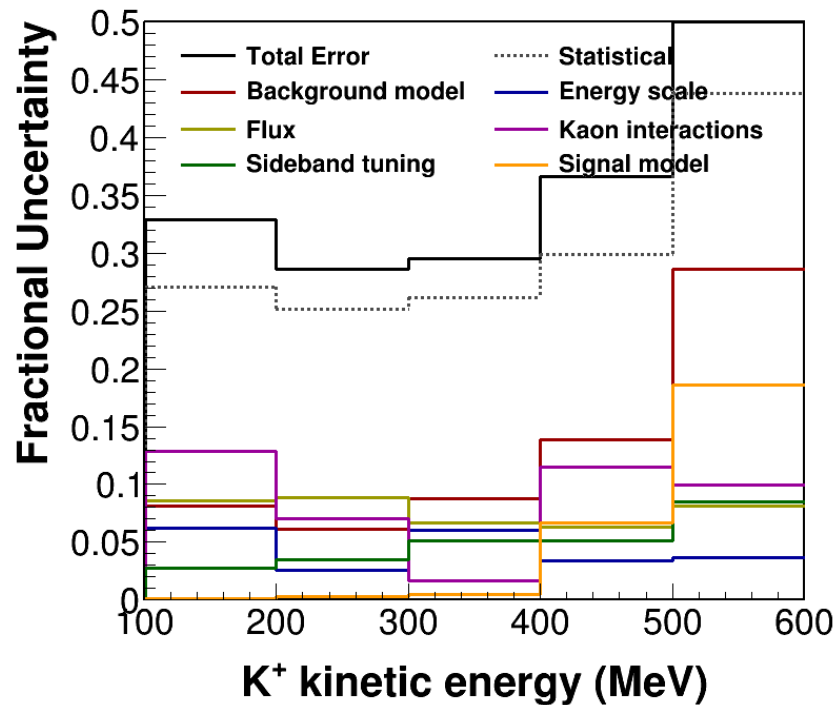
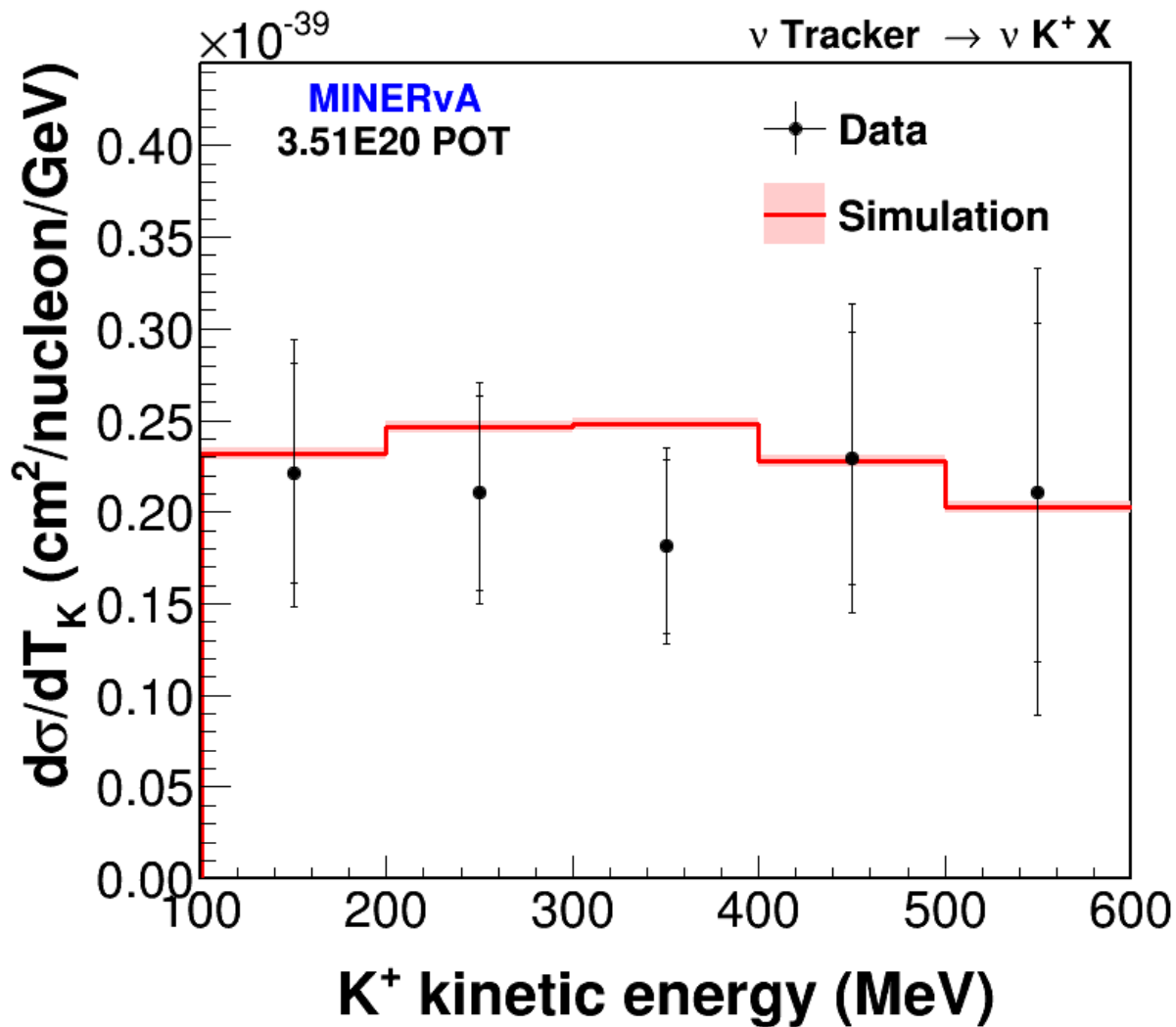


My guess



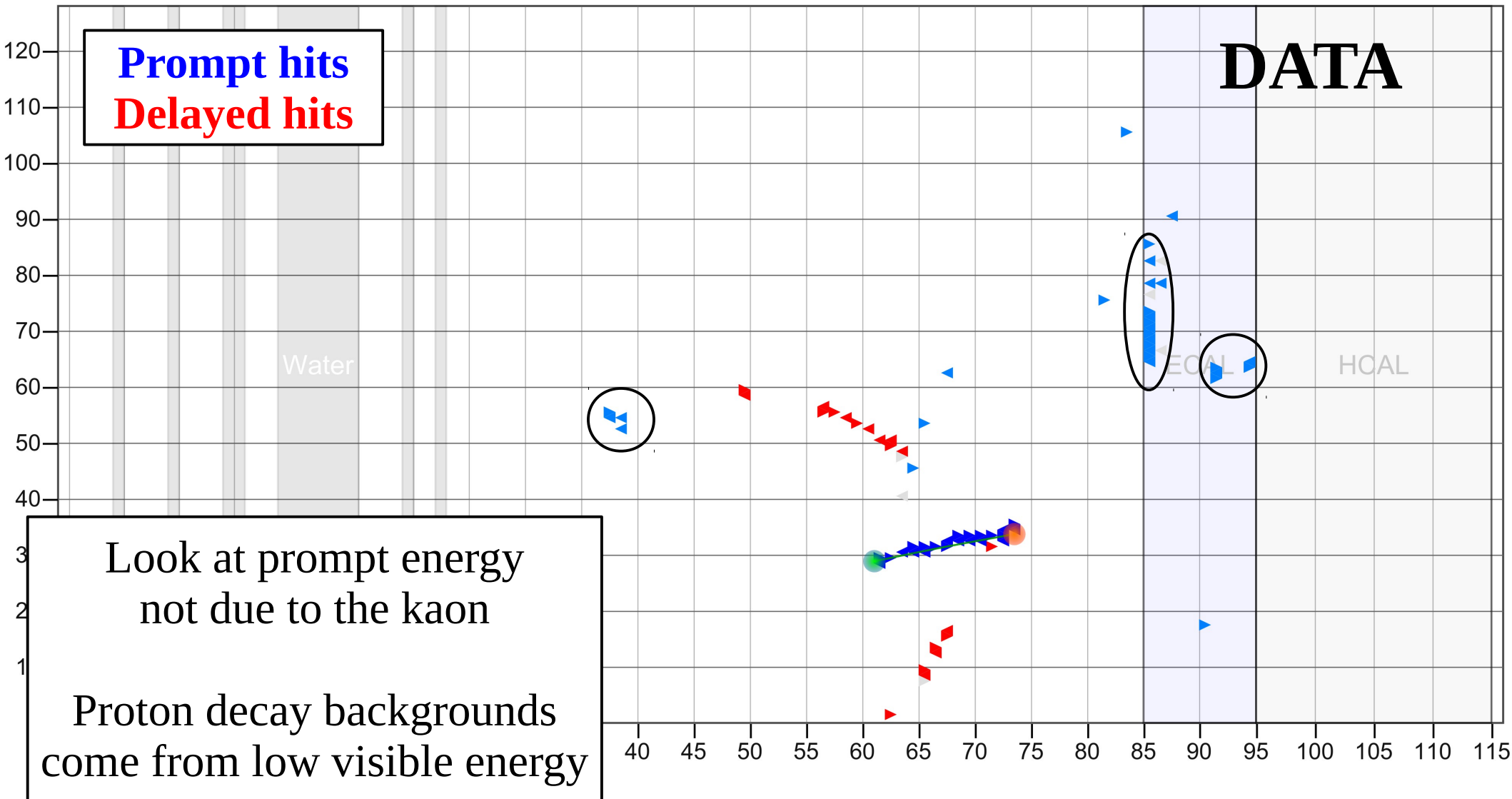
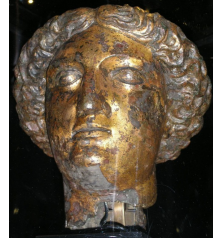


Cross section: good agreement with GENIE





Additional measurement: non-kaon visible energy



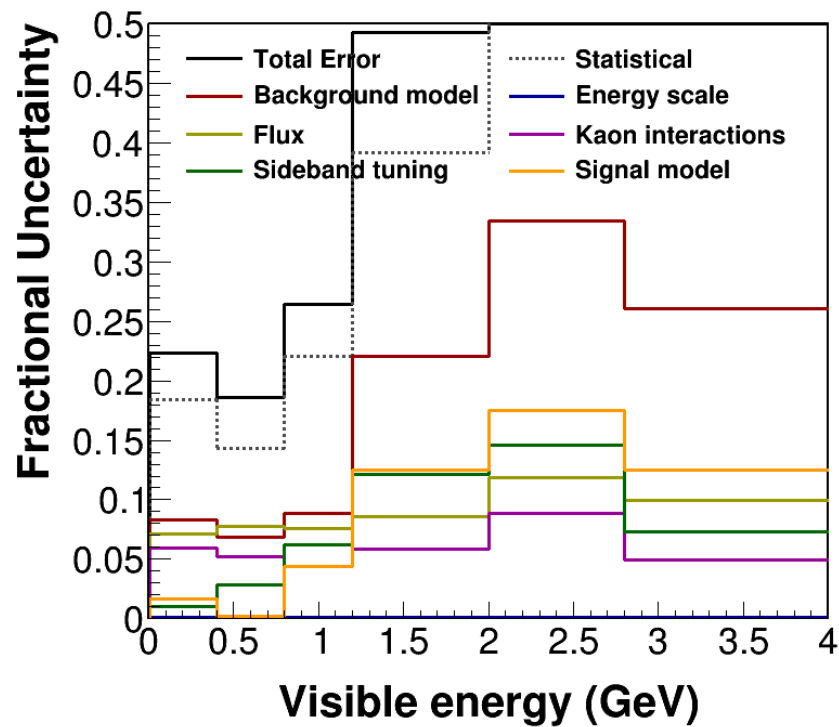
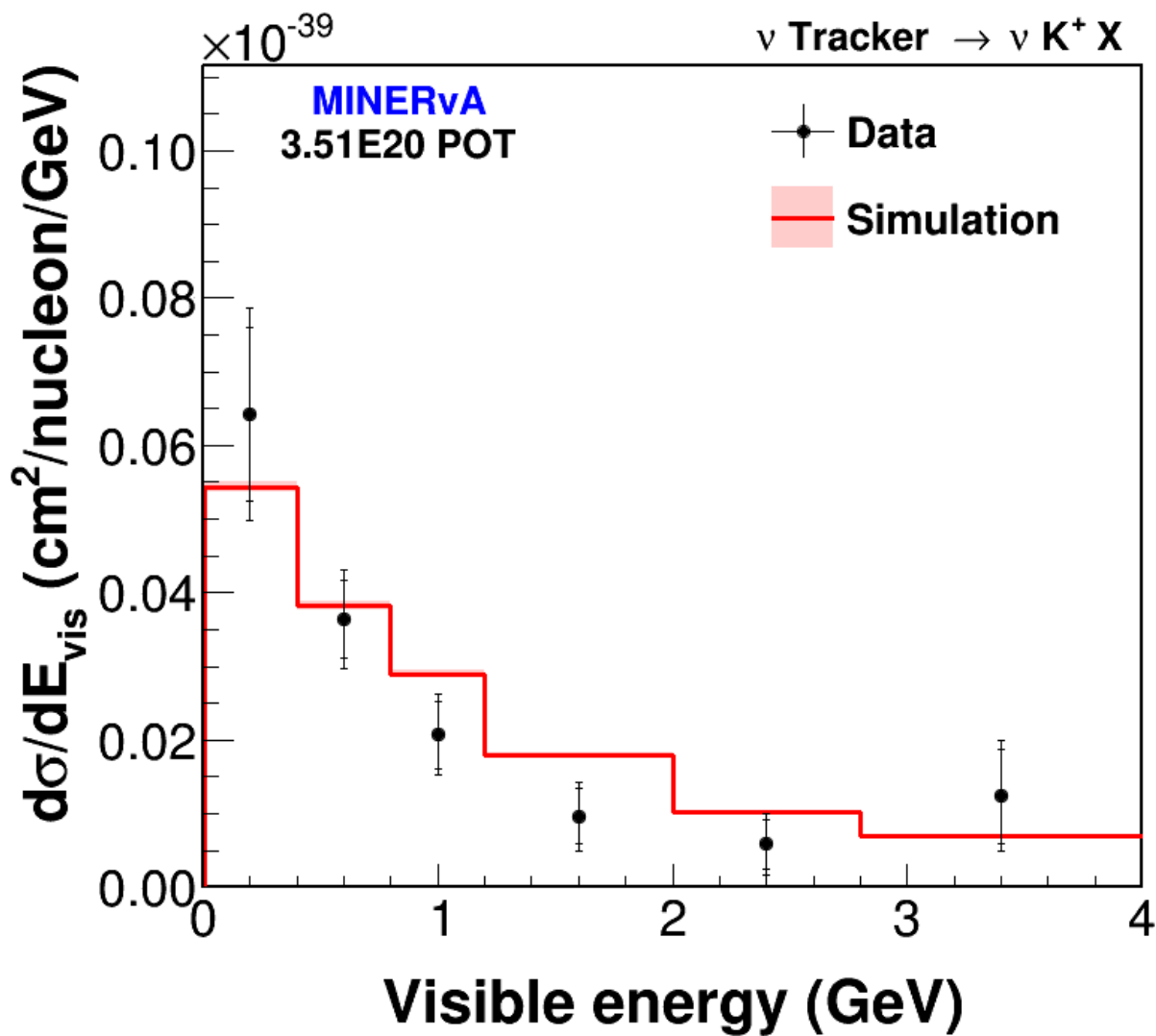


Defining a model-independent proxy for “visible energy”



- Total non-kaon hadron energy is $v - E_K$
- But detector response to neutrons, protons, pions is very different – we don't want to rely on a Monte Carlo to tell us how the energy is distributed
- Define “true visible energy”:
 - Kinetic energy of p, π^\pm, K^-
 - Total energy of π^0, K^0
 - Include prompt decay products of strange baryons Λ, Σ

Visible energy cross section





The big picture

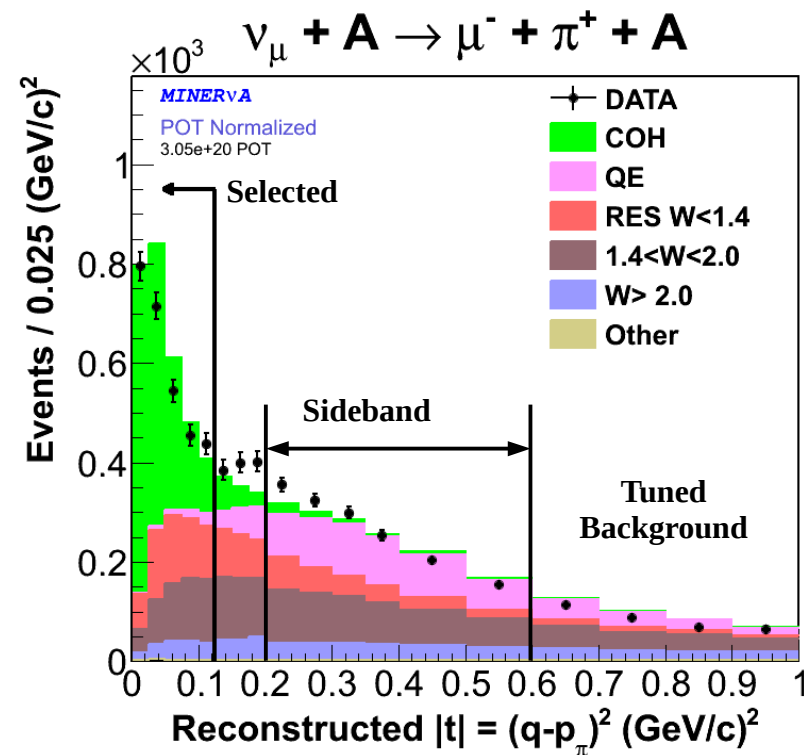
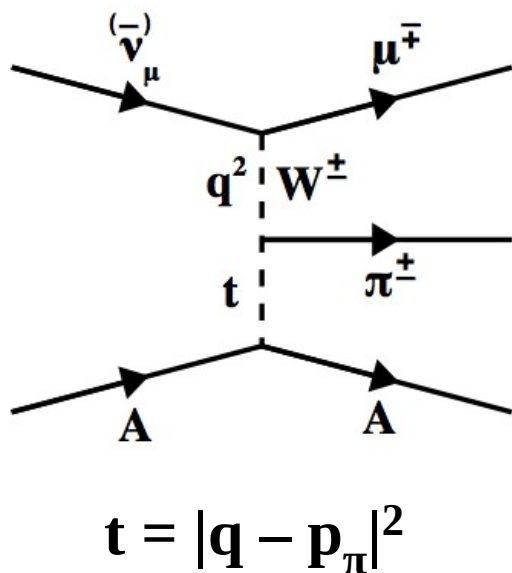


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Coherent meson production

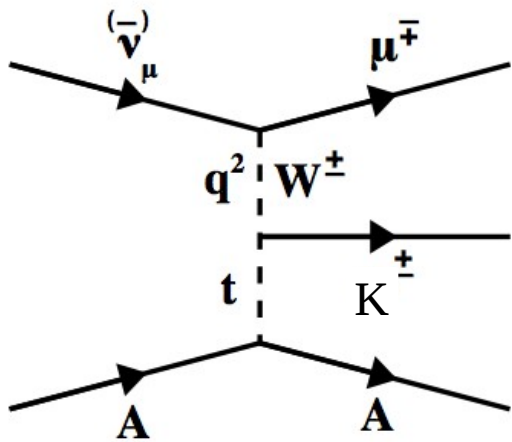
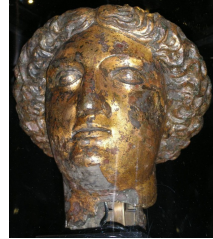


Phys. Rev. Lett. 113, 261802 (2014)



- Neutrino interacts with entire nucleus, which remains in its ground state
- Characterized by small four-momentum transfer to nucleus

Coherent kaon production?



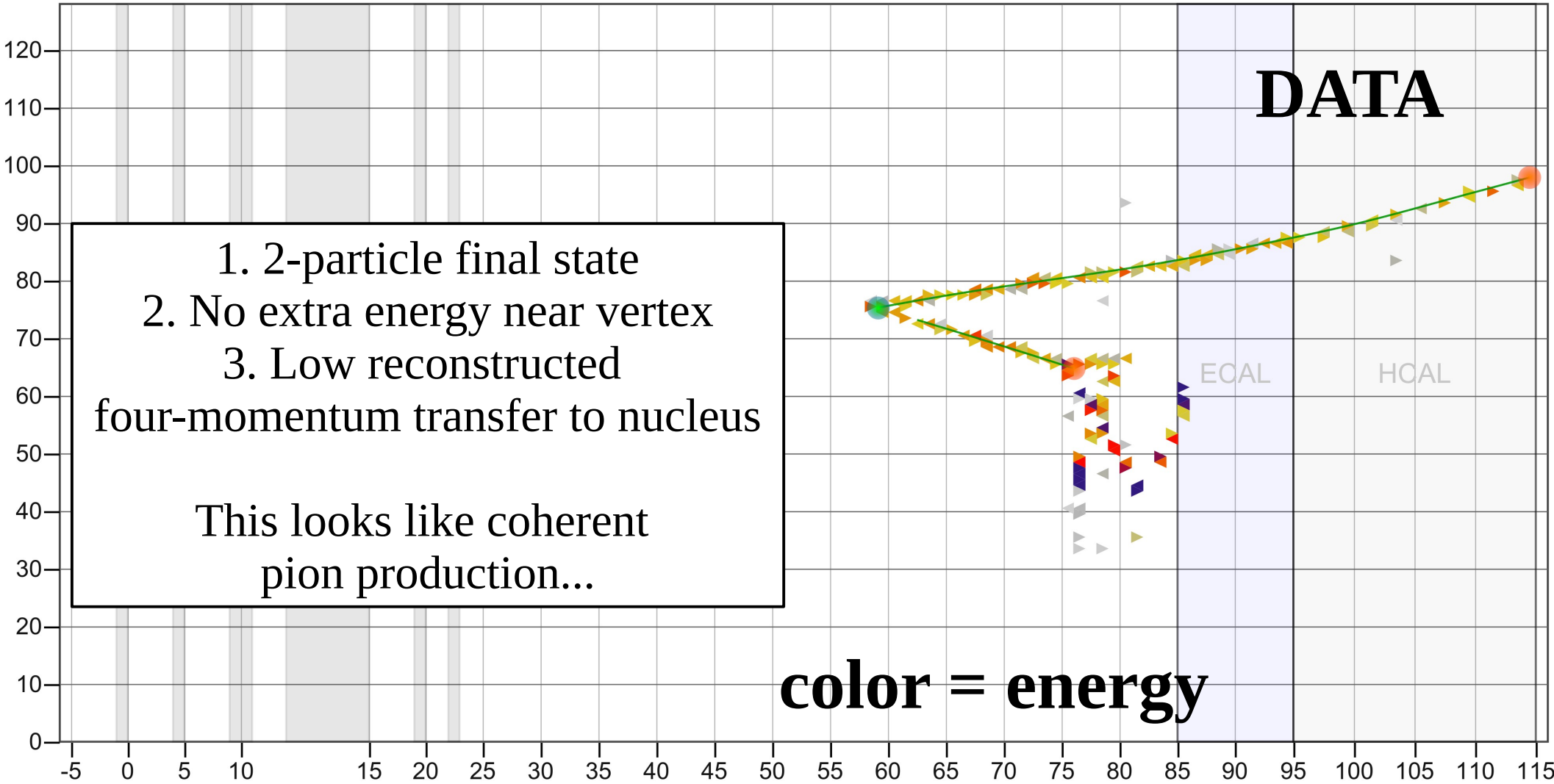
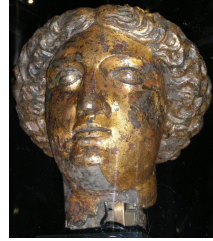
$$t = |\mathbf{q} - \mathbf{p}_K|^2$$

Expect factor of ~ 20 Cabibbo suppression, plus additional factor of ~ 4 phase space suppression due to heavier final state

- Never been observed experimentally
- Theoretical prediction from L. Alvarez-Ruso et al., Phys. Rev. C 87, 015503

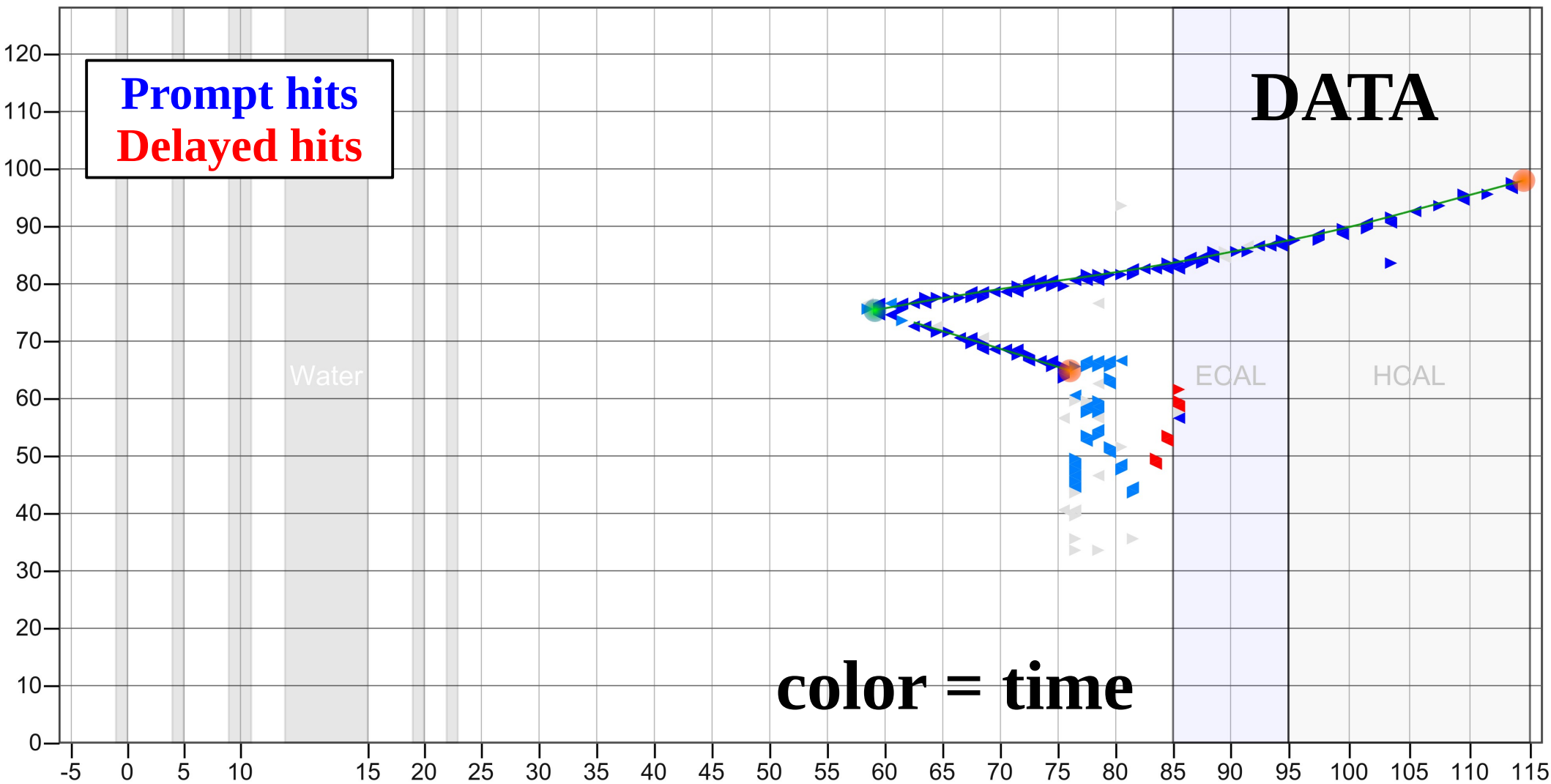


Coherent kaon production?

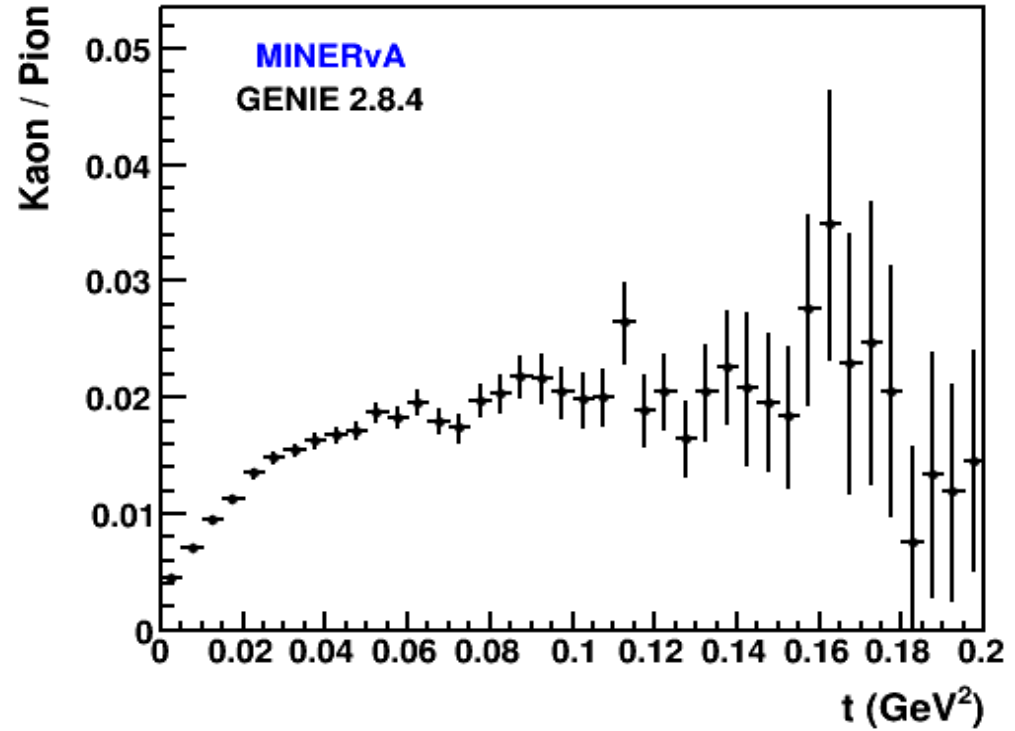
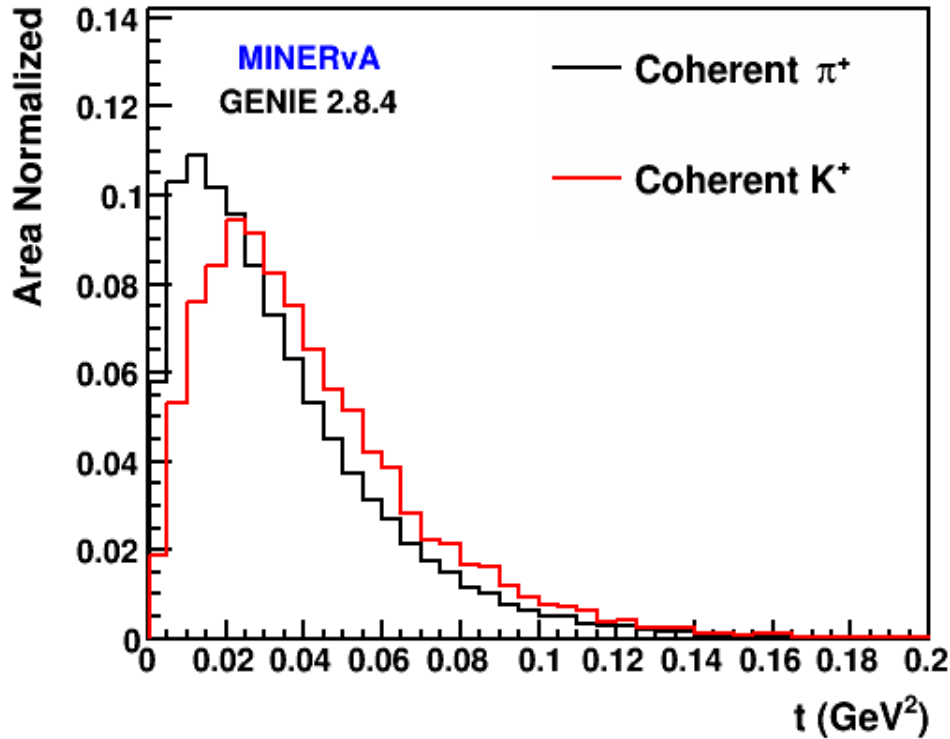
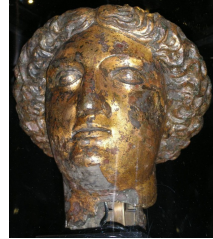




Coherent kaon production?

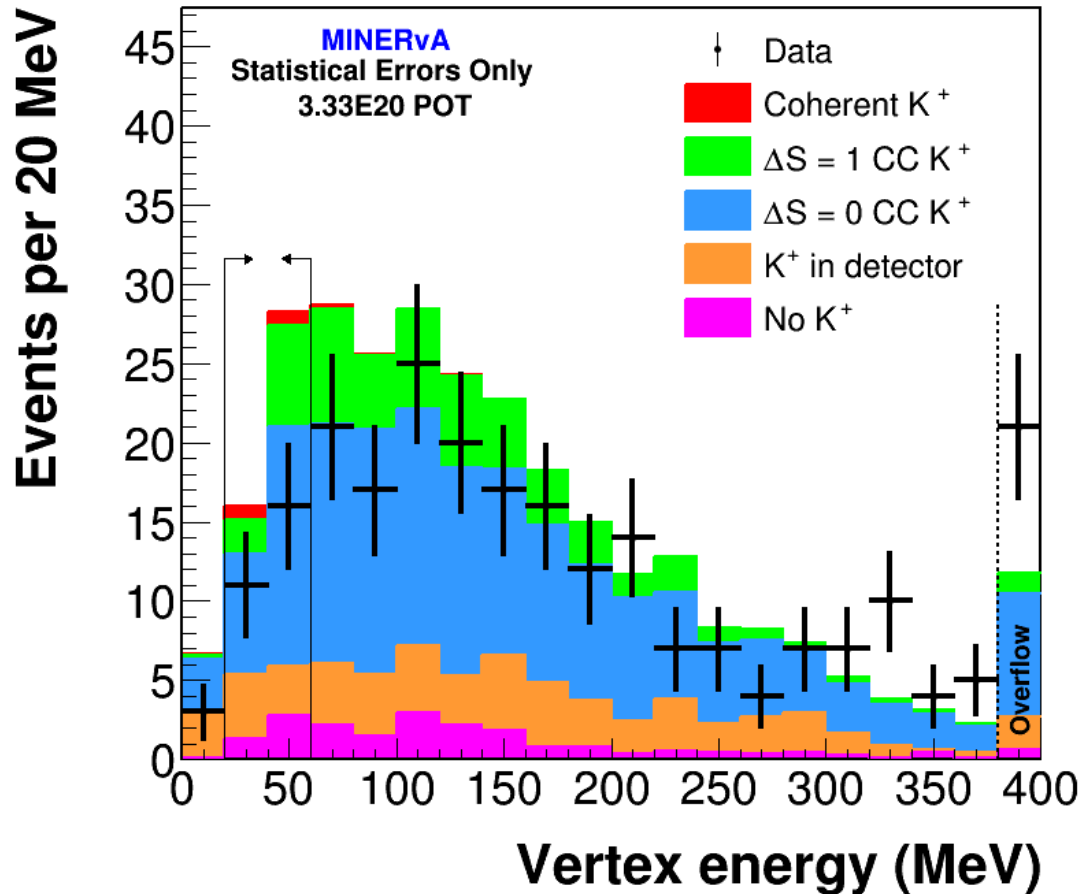
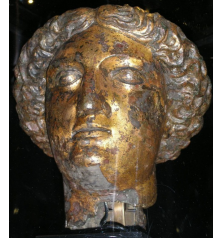


Coherent signal simulation



- Take coherent π^+ events from GENIE 2.8, and replace the π^+ with a K^+
- Assumes π -A and K -A elastic cross sections are equal
- MC only used for shape of reconstructed t

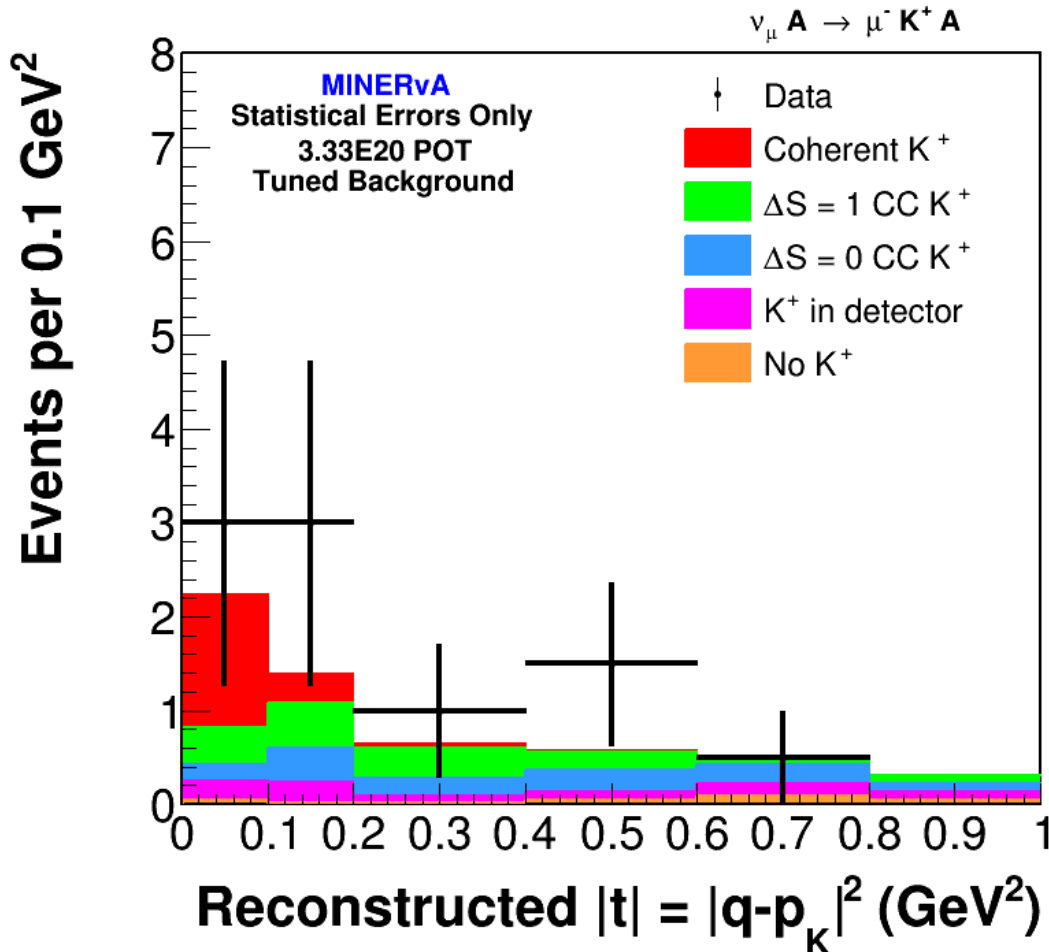
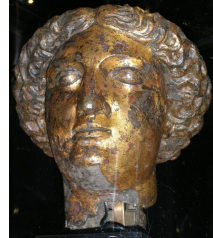
Energy ~ 10 cm around vertex



- Require two tracks, with vertex energy between 20 and 60 MeV
- Red is coherent signal MC



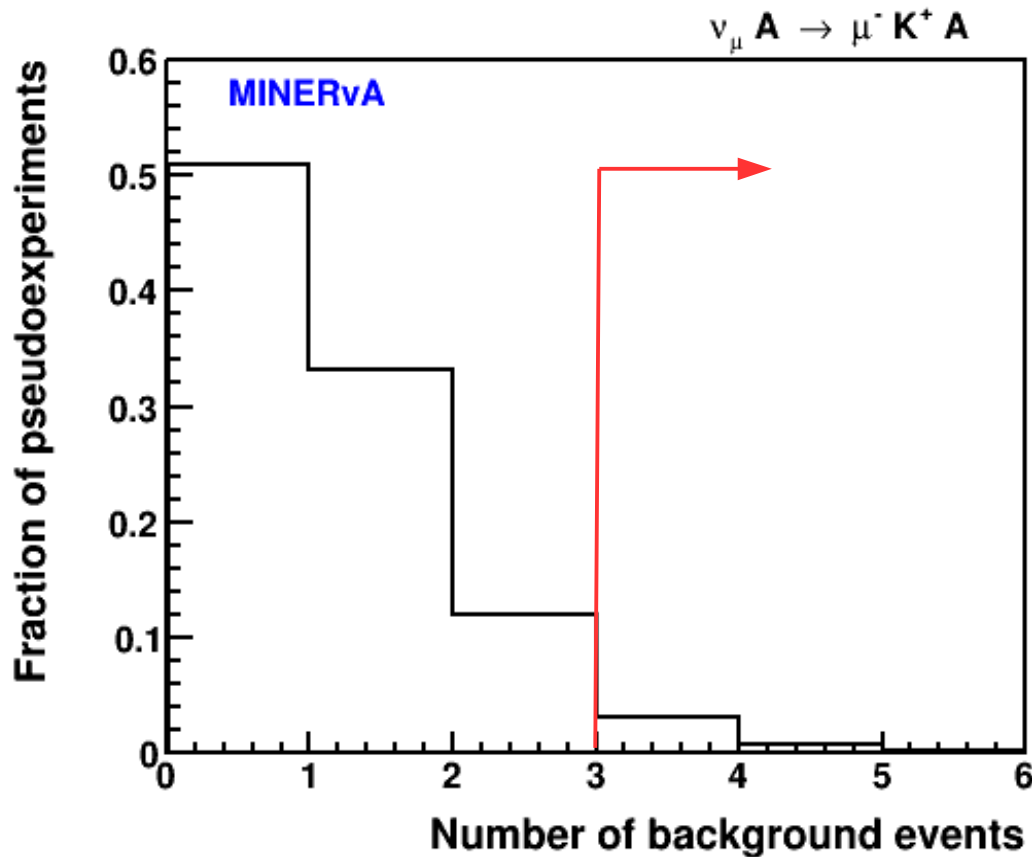
Reconstruct t from muon and kaon 4-vectors



- Cut on vertex energy, no isolated showers from π^0
- Tune background to sideband region
- Event counting analysis: signal region $t < 0.1$ was chosen blind
- Spectral analysis: use $t < 0.2$

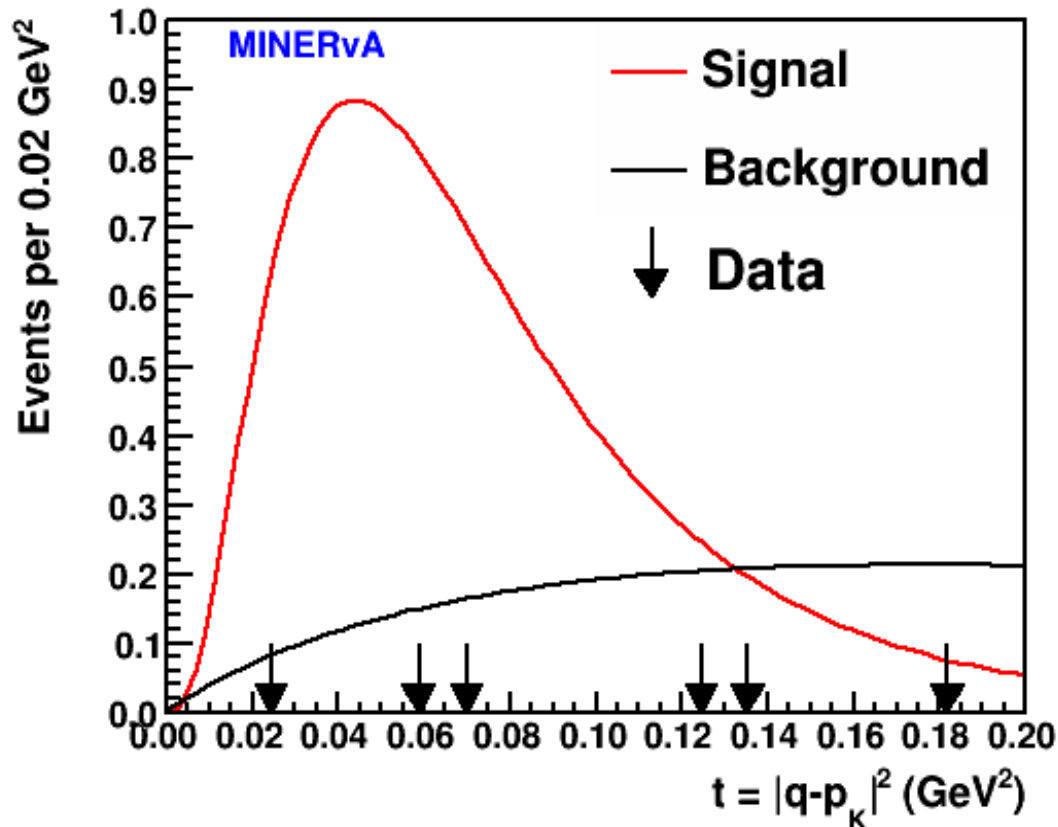


Event counting analysis: Reject null hypothesis at 96%



- Probability to observe 3 or more background events is 3.9%

Spectral analysis



For background and signal PDFs B and S ,

$$\mathcal{L}(\mu) = \prod_{\text{data } i} (B(t_i) + S_{\mu}(t_i))$$

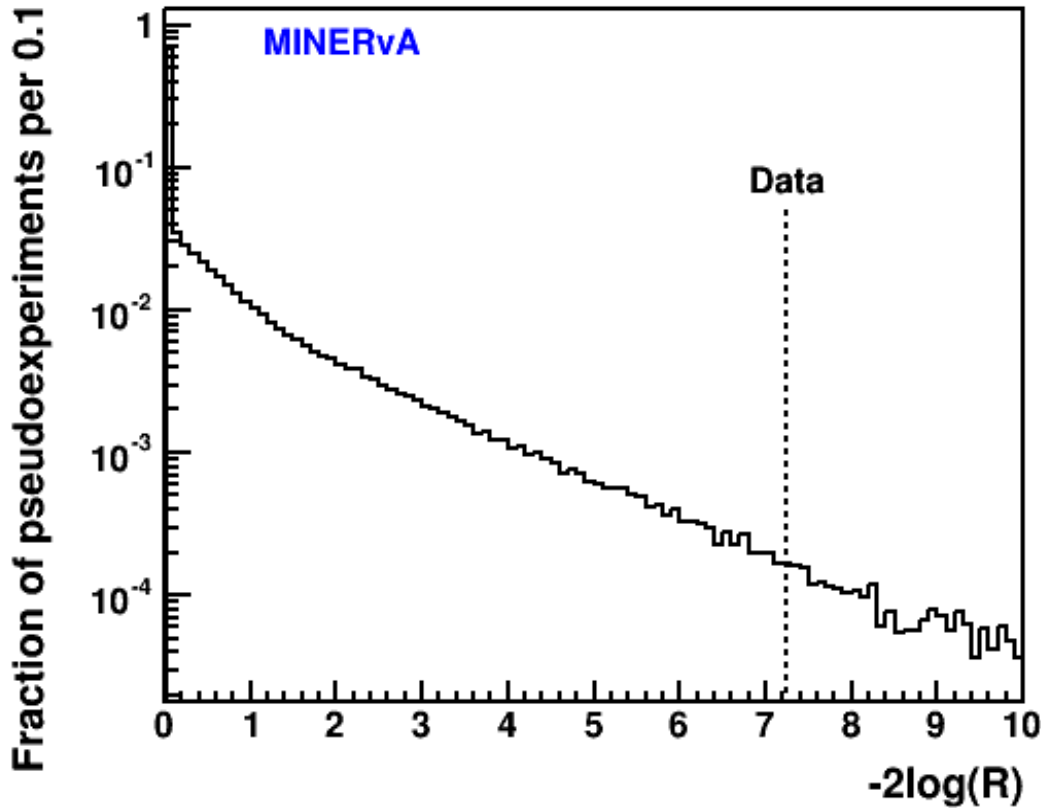
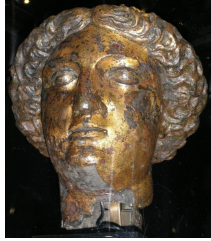
where μ is the integrated number of signal events:

$$\int_0^{0.2} S_{\mu}(t) dt = \mu$$

R is the likelihood ratio of the null hypothesis ($\mu = 0$) to the best-fit value of μ

$$R = \frac{\mathcal{L}(0)}{\mathcal{L}(\mu_{best})}$$

Spectral analysis



- μ_{best} in data is 4.0
- $-2\log(R) = 7.24$
- In background-only pseudoexperiments, the probability to observe $-2\log(R) > 7.24$ is 0.3%
- 3σ observation of coherent K^+ signal in spectral analysis



Summary



- MINERvA has made the best measurement to date of charged-current and neutral-current K^+ production by neutrinos
- Probed FSI by studying kaon spectrum
- Looked for “kaon plus nothing” neutral current events that could fake proton decay signal
- Observed charged-current coherent K^+ production at 3σ
- GENIE cross section + nuclear model does a good job of reproducing the data – great news for DUNE & Hyper-K nucleon decay searches



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Thank you



The MINERvA collaboration in Duluth, Minnesota, 2014



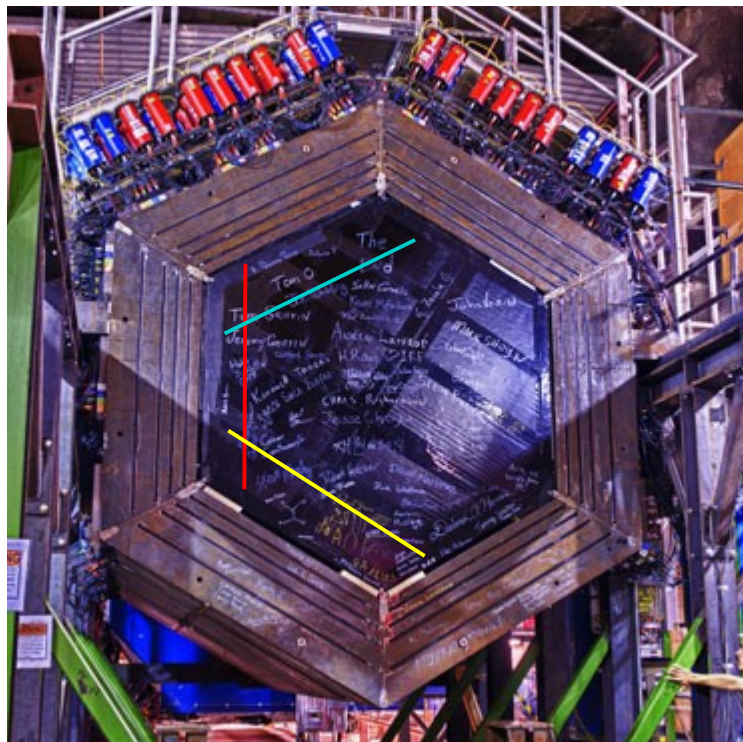
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Backups

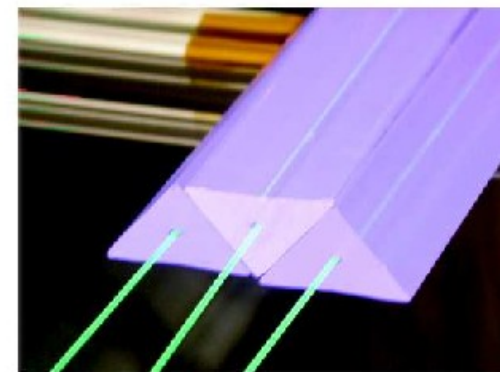




The MINERvA detector



208 active planes \times 127 scintillator bars



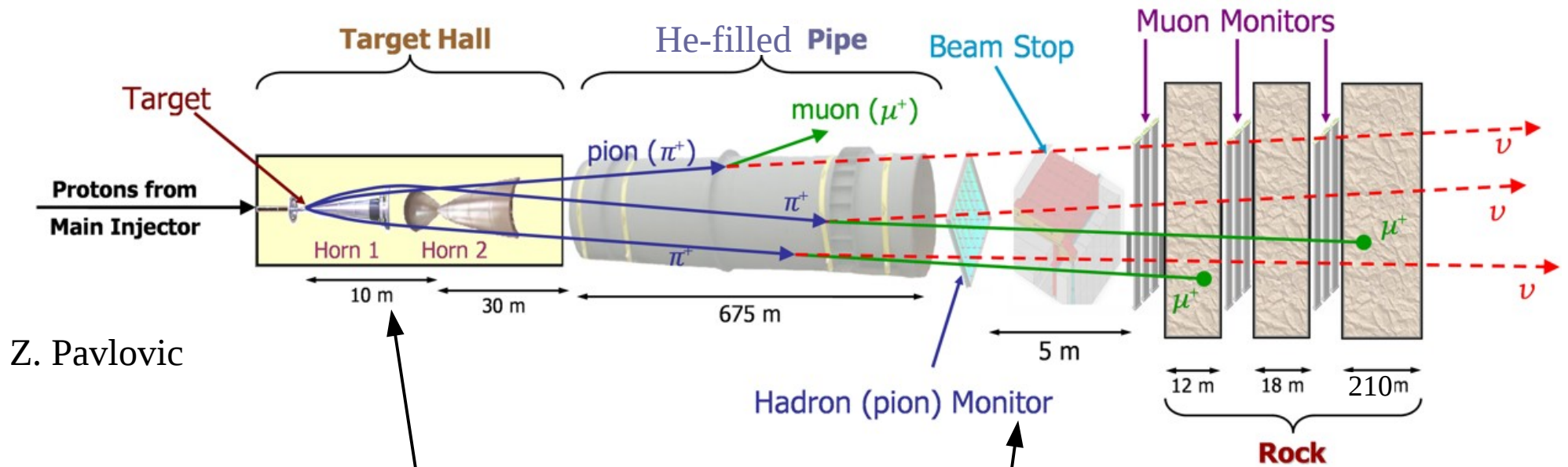
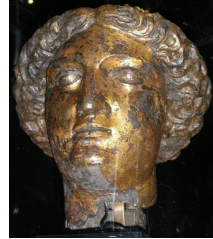
Plane views:

1. Vertical bars
2. $+60^\circ$
3. -60°

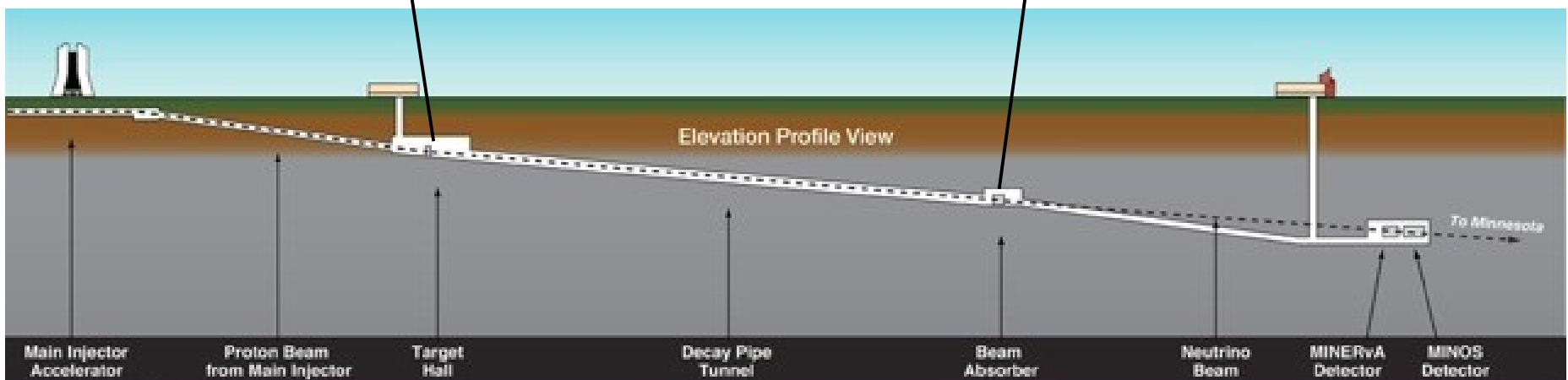
Nucl. Inst. and Meth. A743 (2014) 130
arXiv:1305.5199



NuMI beamline



Z. Pavlovic

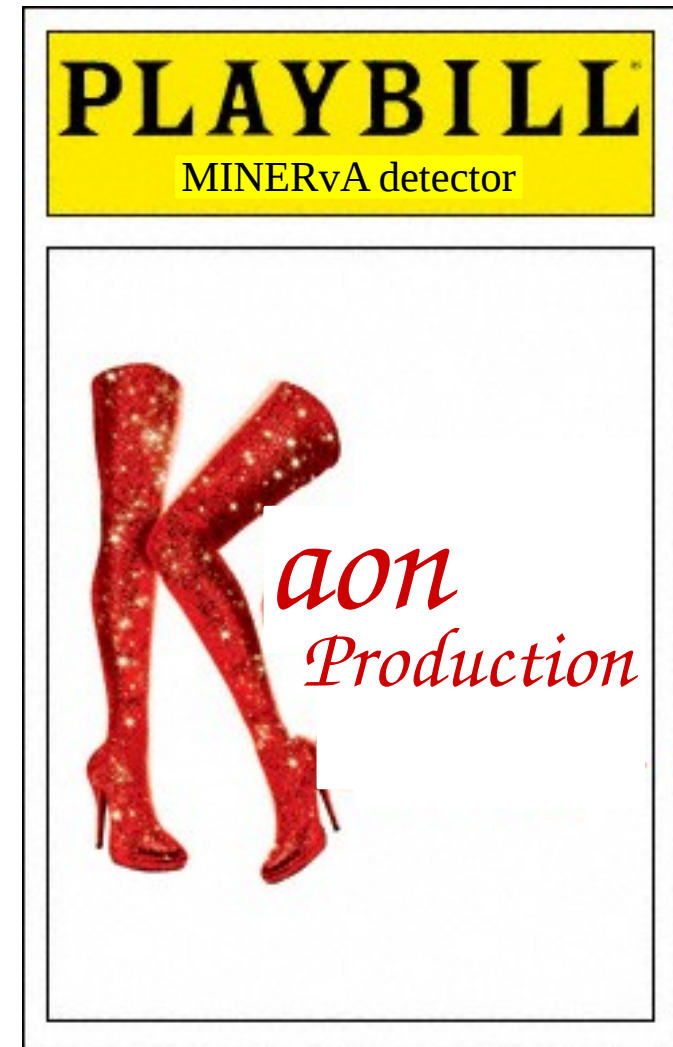




Meet the cast

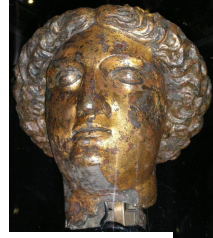


- K^+ ($u\bar{s}$), 494 MeV, $\tau = 12.4$ ns
 - $K^+ \rightarrow \mu^+ \nu$ (64%)
 - $K^+ \rightarrow \pi^+ \pi^0$ (20%)
- Λ (uds), 1115 MeV, $\tau = 0.3$ ns
- Σ^\pm (uus/dds), ~ 1190 MeV, $\tau \sim 0.1$ ns
- K^0 ($d\bar{s}$), 498 MeV, either decays promptly, absorbs, or charge exchanges to K^+

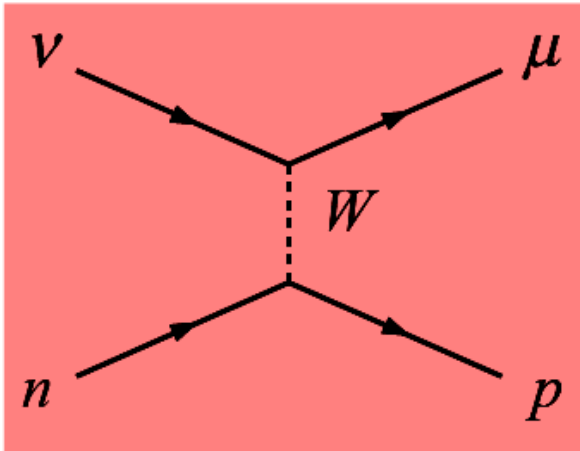




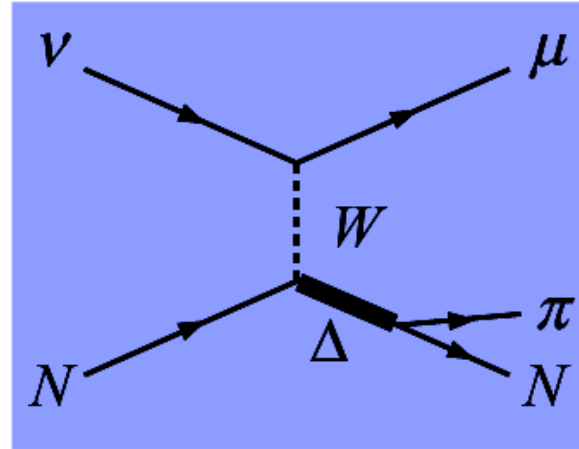
GENIE 2.8.4 MC simulation



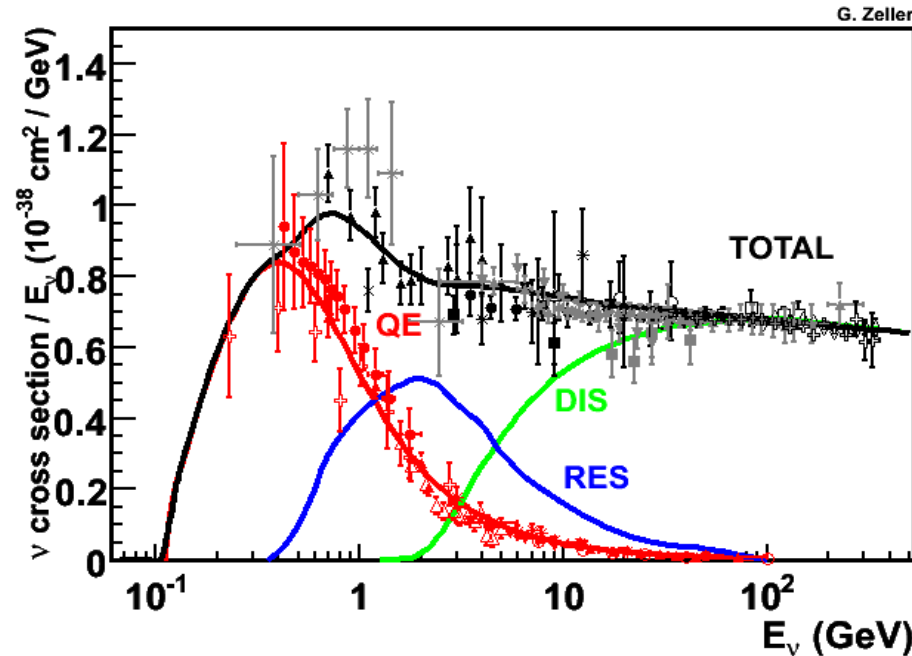
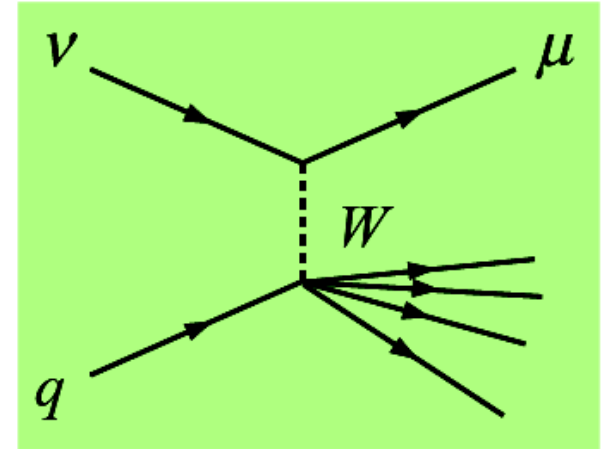
Quasielastic (QE)



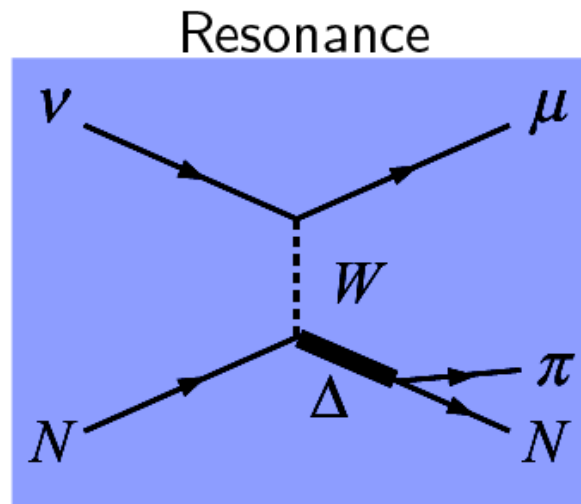
Resonance



DIS



Resonance production of kaons

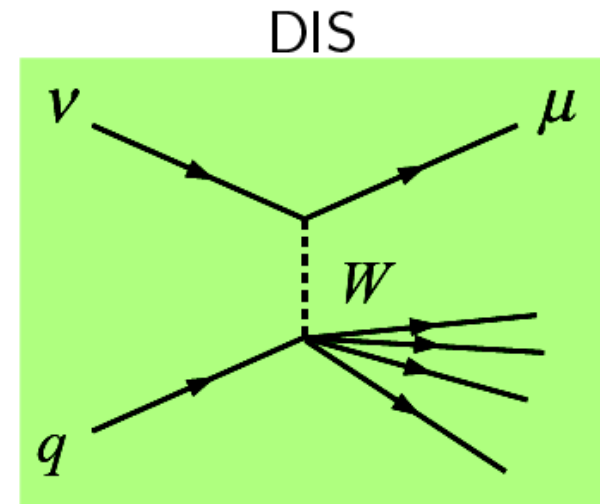


“Associated production” of $K +$ strange baryon (Λ, Σ) from the decay of high-mass baryon resonances

In GENIE, individual resonances are simulated up to hadronic invariant mass $W = 1.7$ GeV, which is barely above the $K\Lambda$ threshold of ~ 1.6 GeV, so very few kaons come from resonance decays in GENIE



Kaons from hadronization

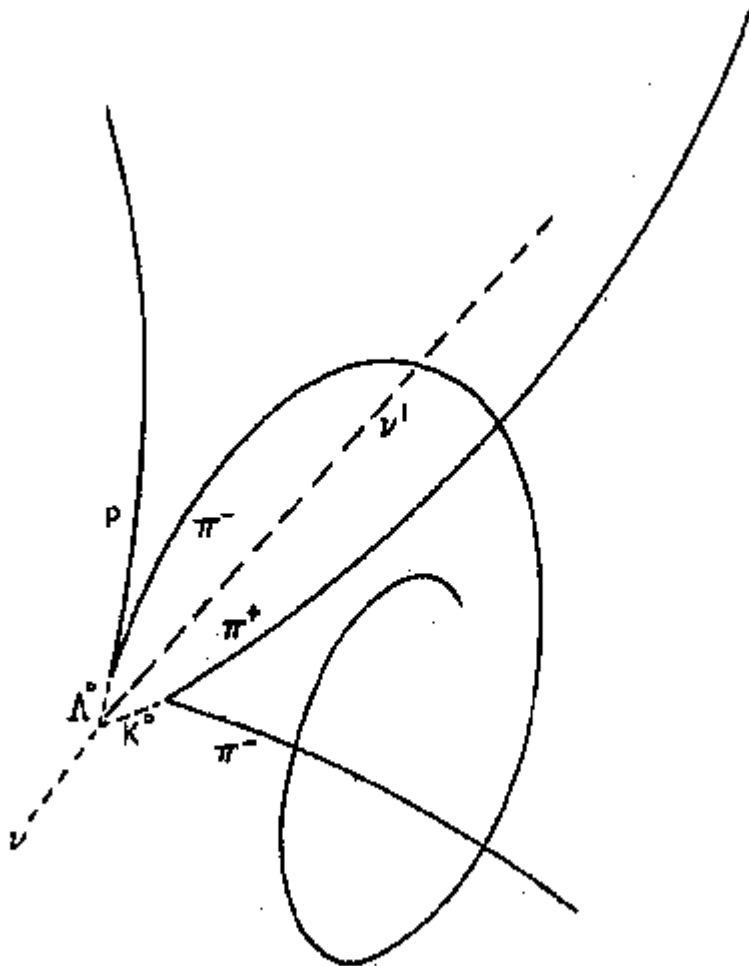


In DIS, it is possible to get $s\bar{s}$ pairs in hadronization, which results in KK , $K\Lambda$ or $K\Sigma$ pairs

GENIE uses KNO parameterization for $1.7 < W < 2.3$ GeV, the “AGKY” model for $2.3 < W < 3.0$, and PYTHIA for $W > 3.0$

Tuned to Λ and K^0 bubble chamber data vs. W

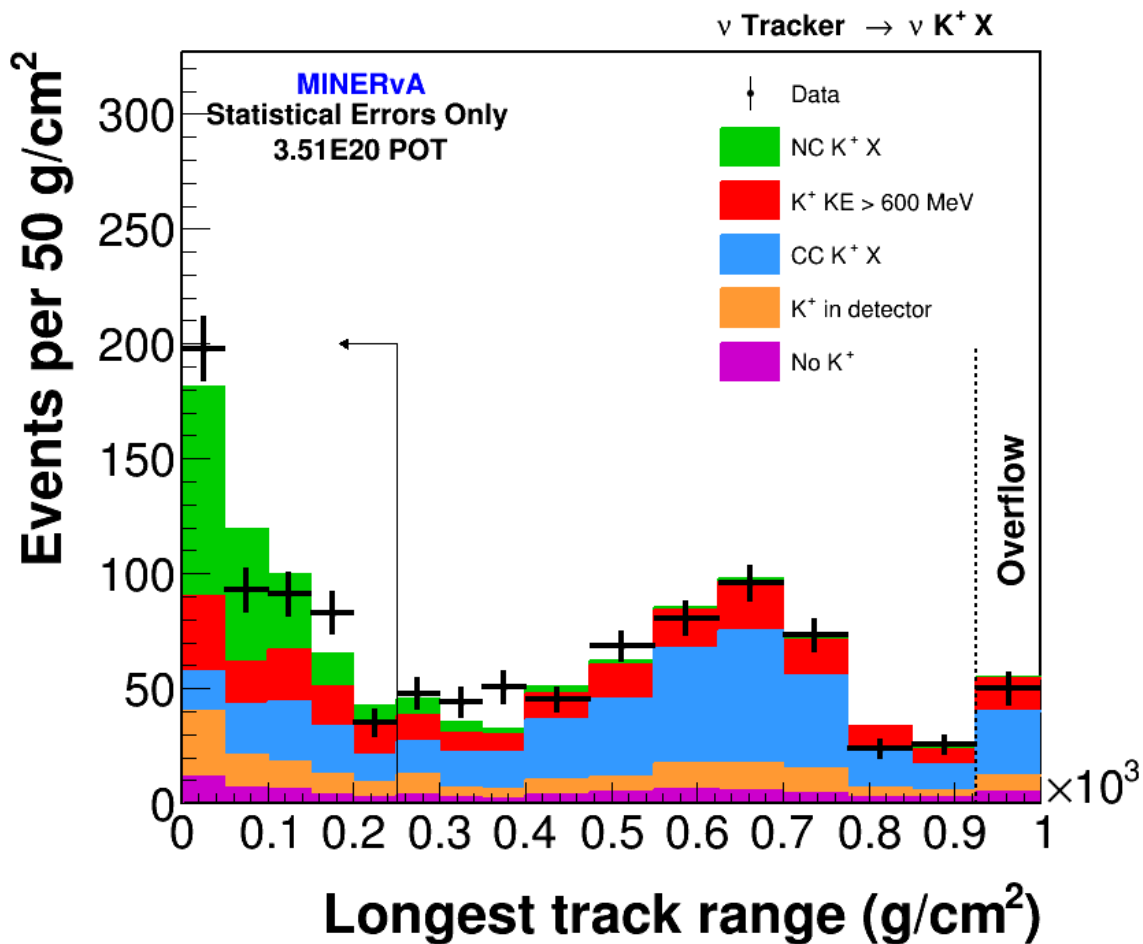
Kaons in bubble chambers



ANL 12' $K^0\Lambda$ event

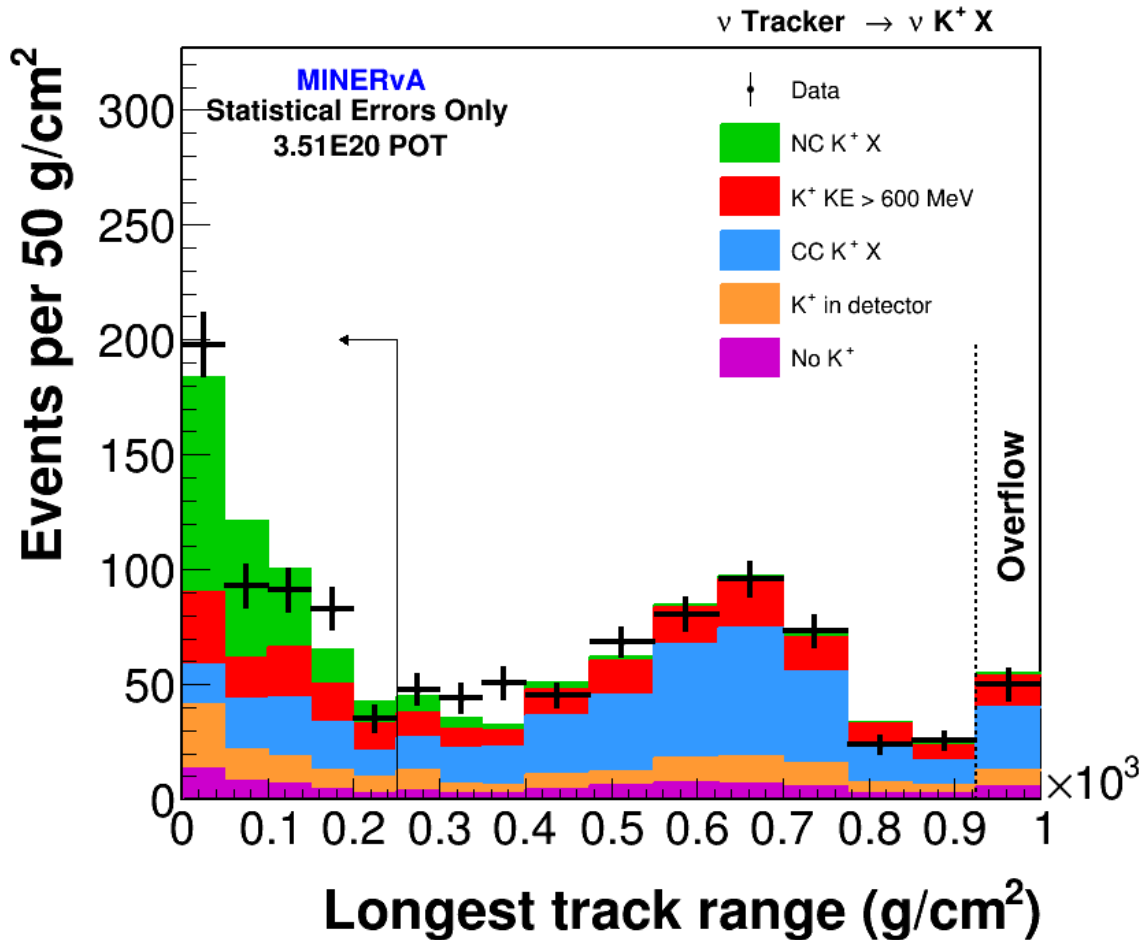
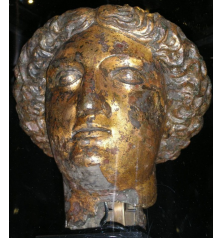
- Bubble chambers are fantastic detectors for $\Lambda \rightarrow p\pi^-$ and $K^0 \rightarrow \pi^+\pi^-$ from the “double V”
- K^+ are much harder
 - Ionization pattern can be ambiguous between $\pi/K/p$
 - Can reconstruct decay if the kaon stops in detector
 - Can infer from presence of Λ

Longest track range (NC)



- Additional cut: reject MINOS-matched tracks
- Use CC-like region as a sideband
- Rejecting MINOS tracks reduces the amount of extrapolation from low- y to high- y events

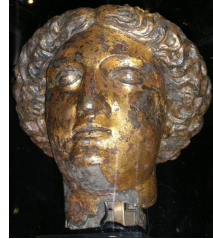
Tune the background



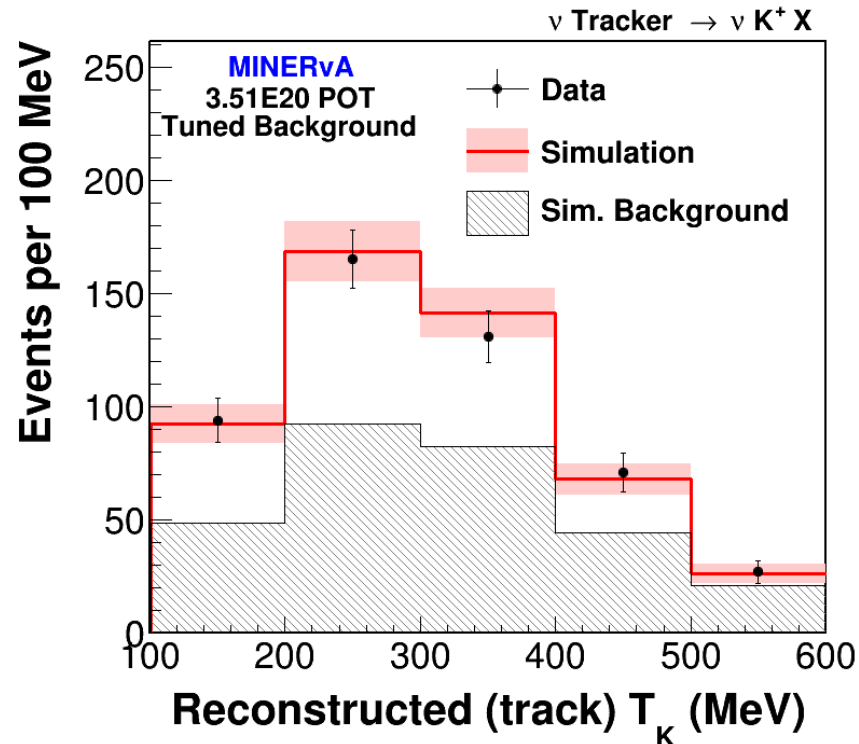
- Scale the non-pile-up backgrounds by 0.96
- Because you scale multiple backgrounds simultaneously, uncertainties arise when the composition is different in signal and sideband region



Extracting a cross section: NC

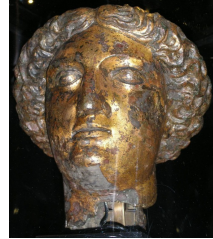


$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

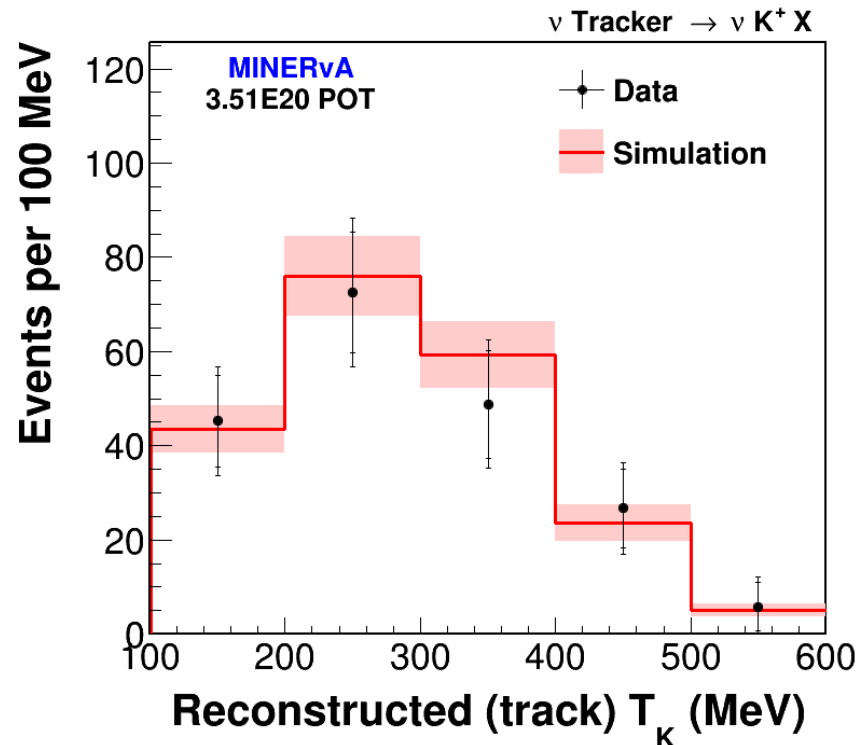




Extracting a cross section: NC



$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

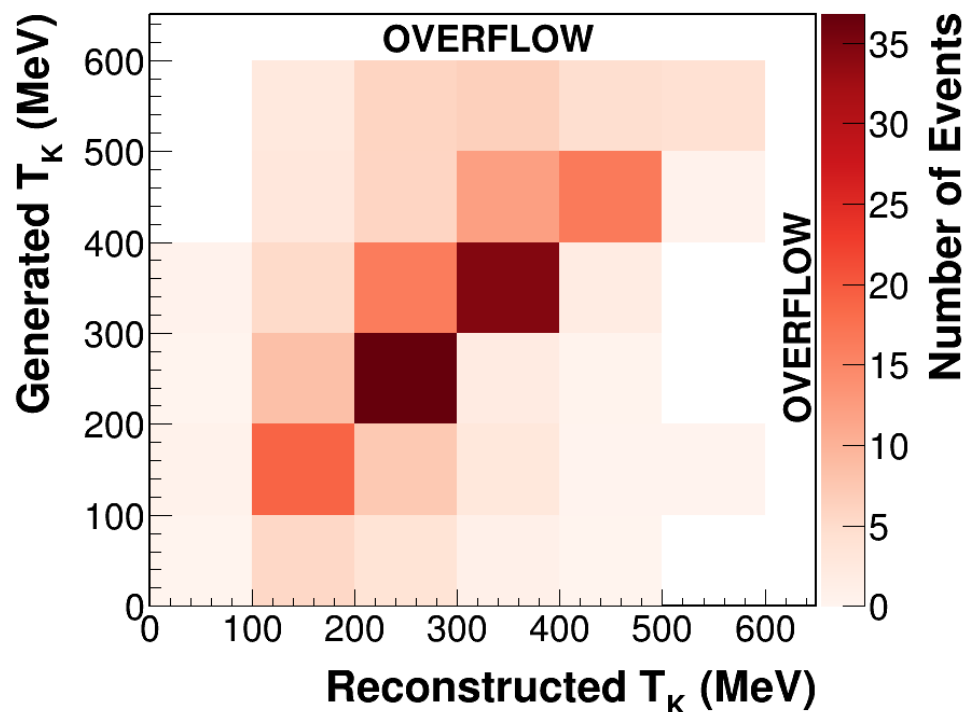




Extracting a cross section: NC

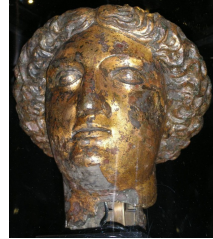


$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

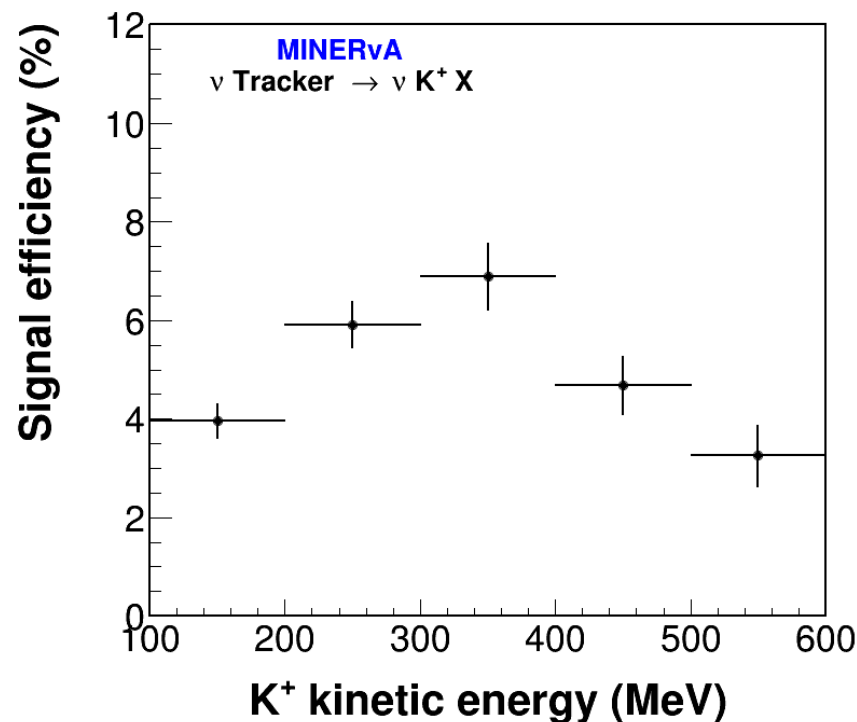




Extracting a cross section: NC

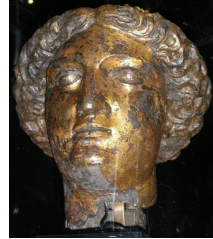


$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

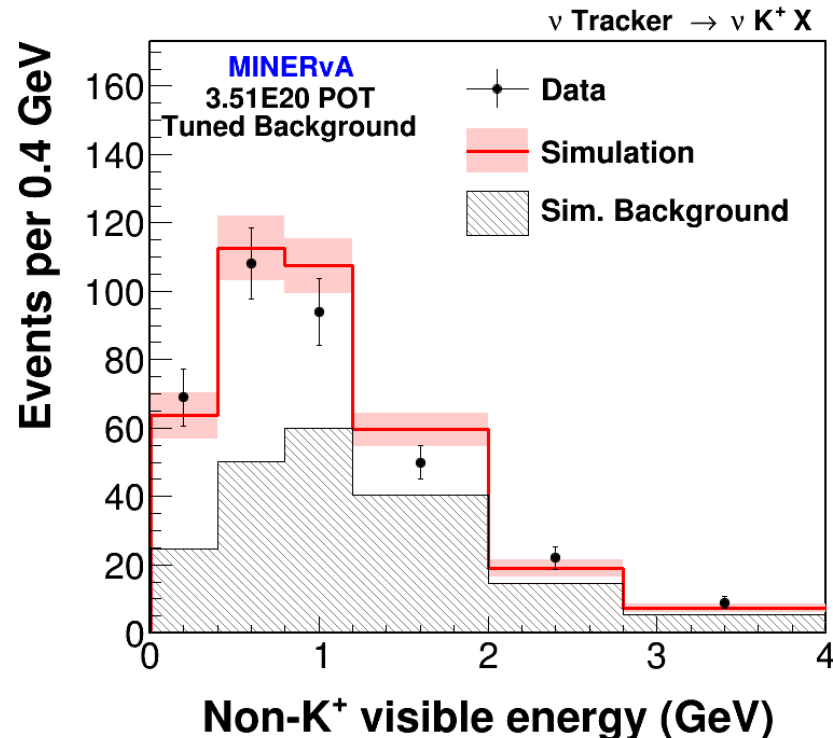




Extracting a cross section: NC

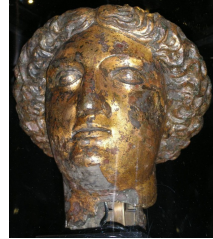


$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

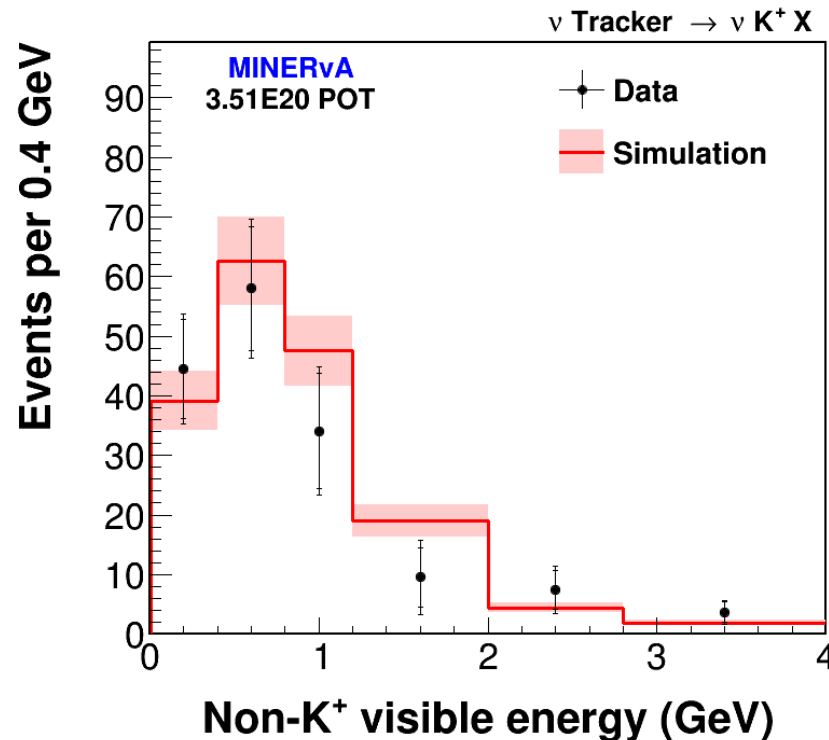




Extracting a cross section: NC



$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

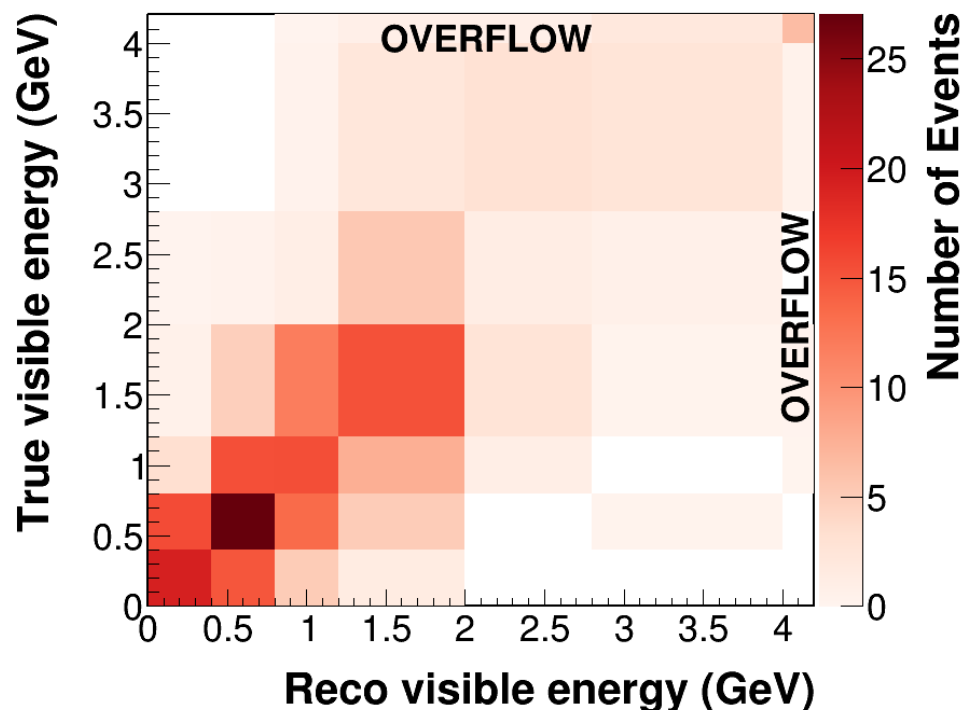




Extracting a cross section: NC



$$\left(\frac{d\sigma}{d\xi}\right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

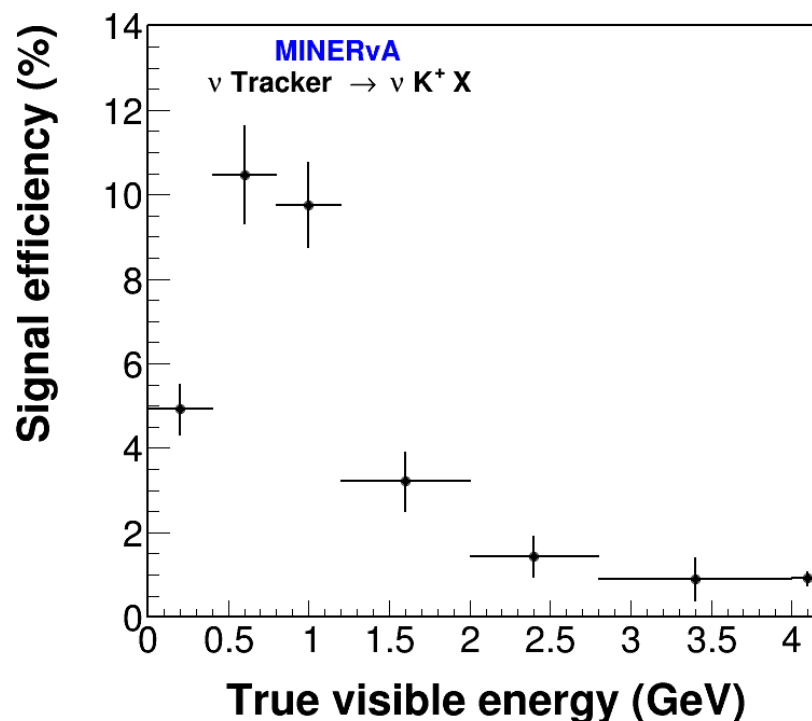




Extracting a cross section: NC

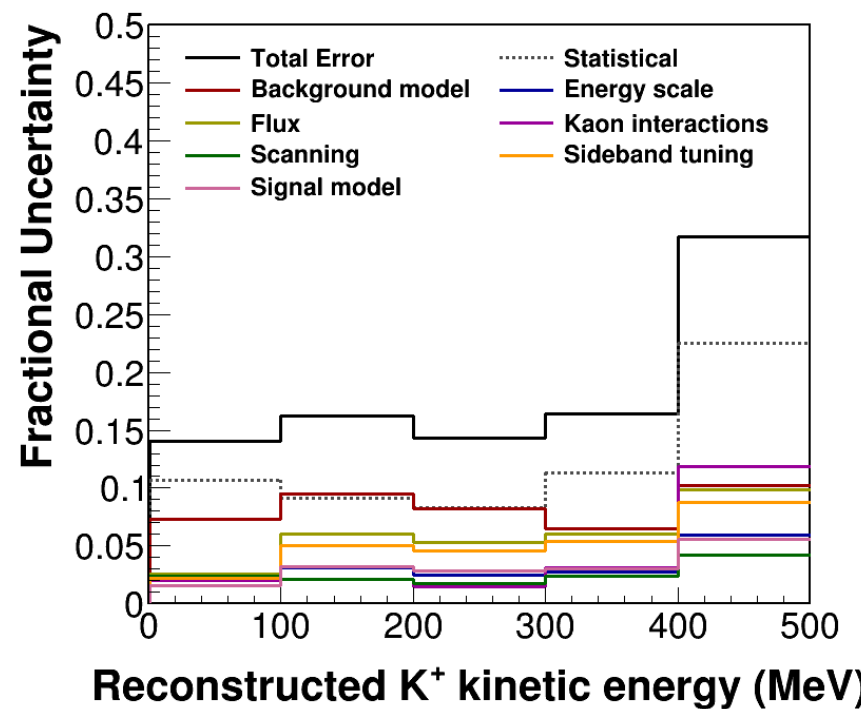
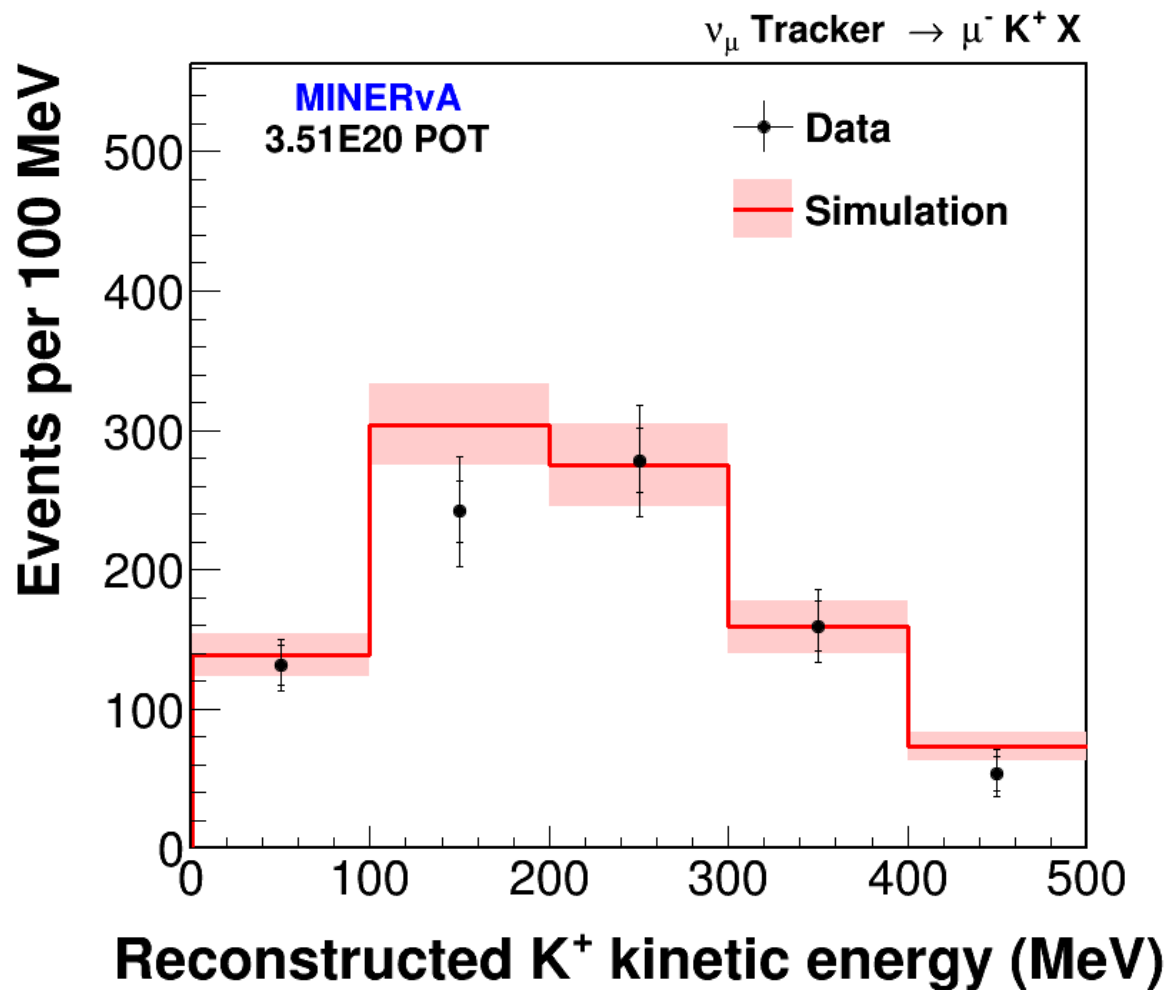


$$\left(\frac{d\sigma}{d\xi} \right)_i = \frac{1}{\Phi} \times \frac{1}{T_n} \times \frac{1}{(\Delta\xi)_i} \times \frac{\sum_j U_{ij} (N_j^{obs} - N_j^{bknd})}{\epsilon_i}$$

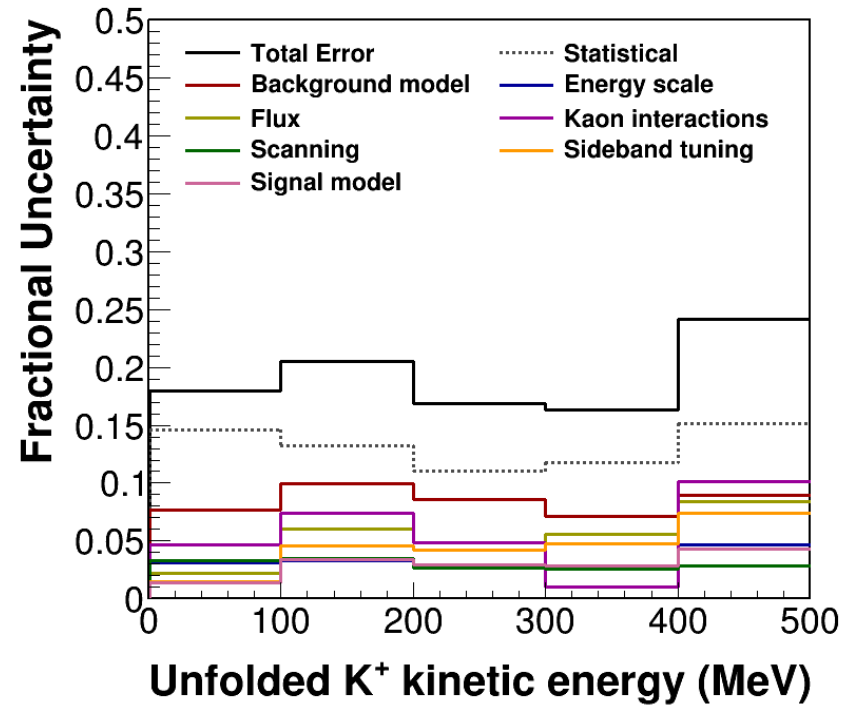
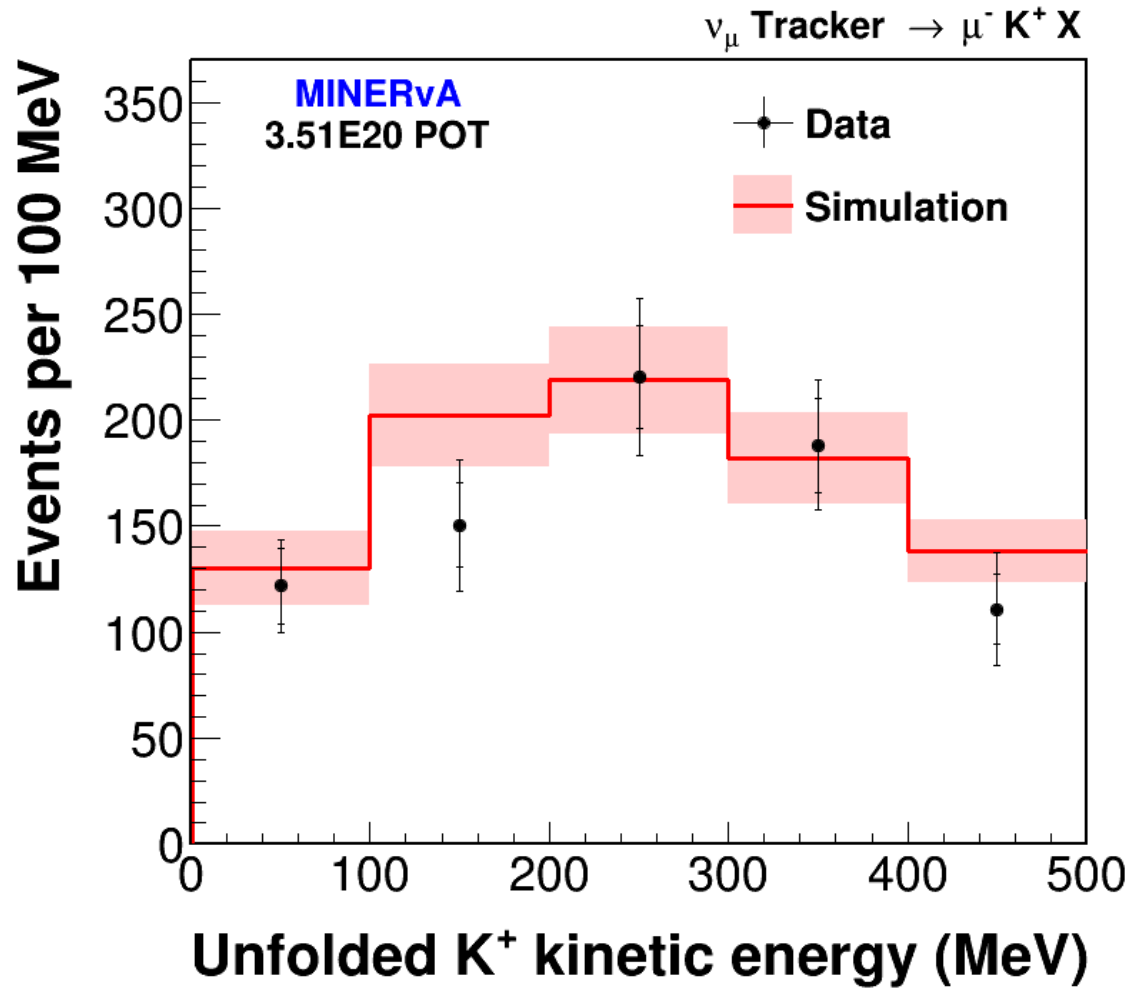
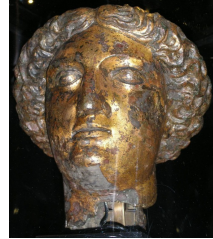




CC background-subtracted

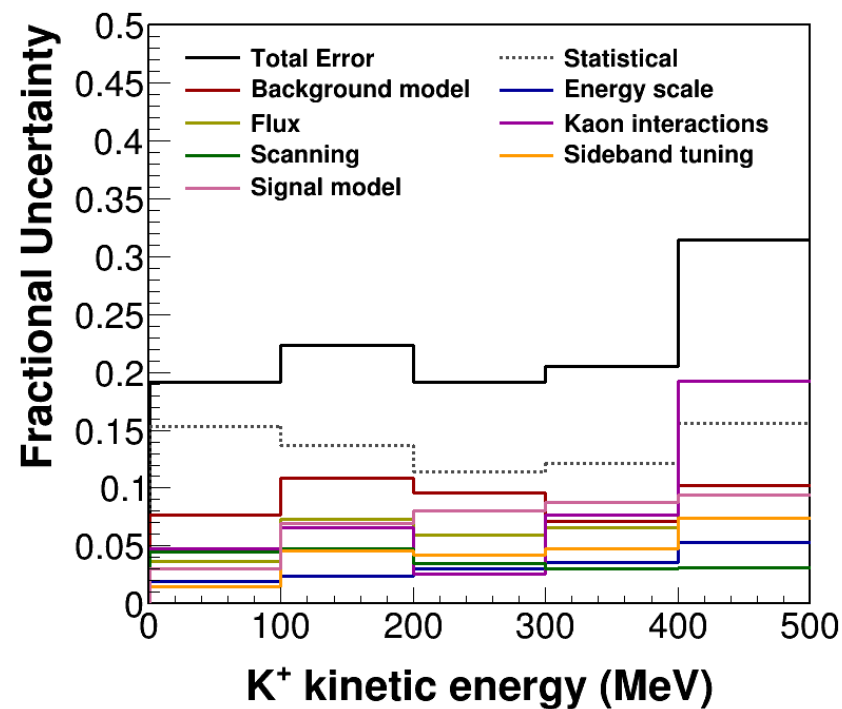
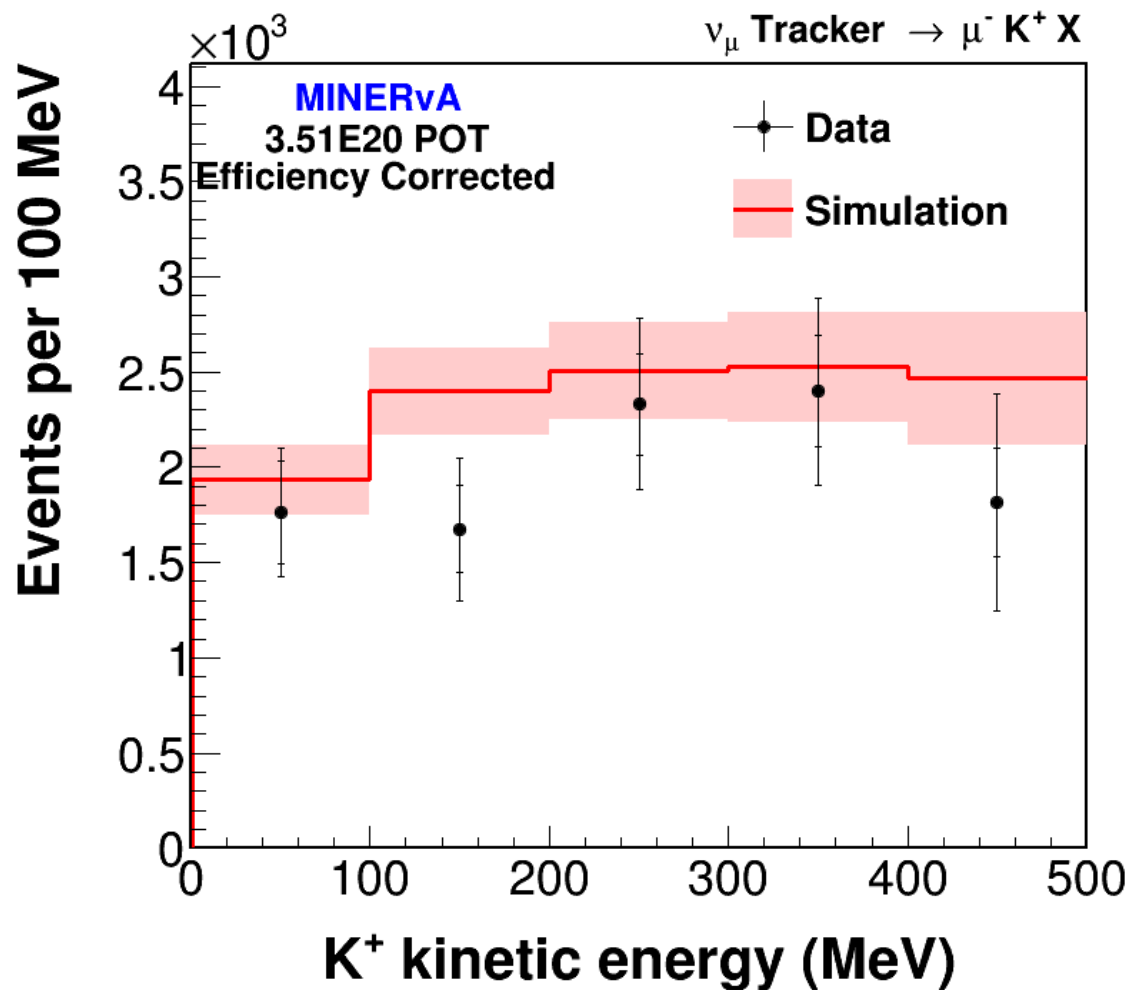
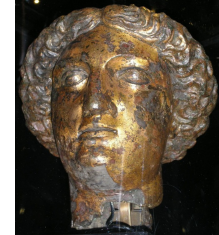


CC unfolded



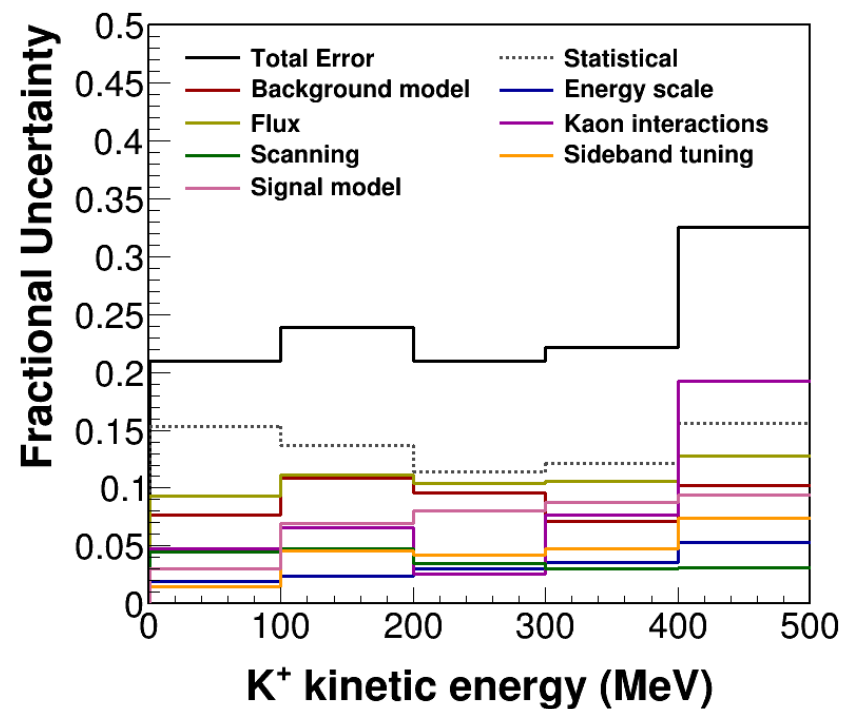
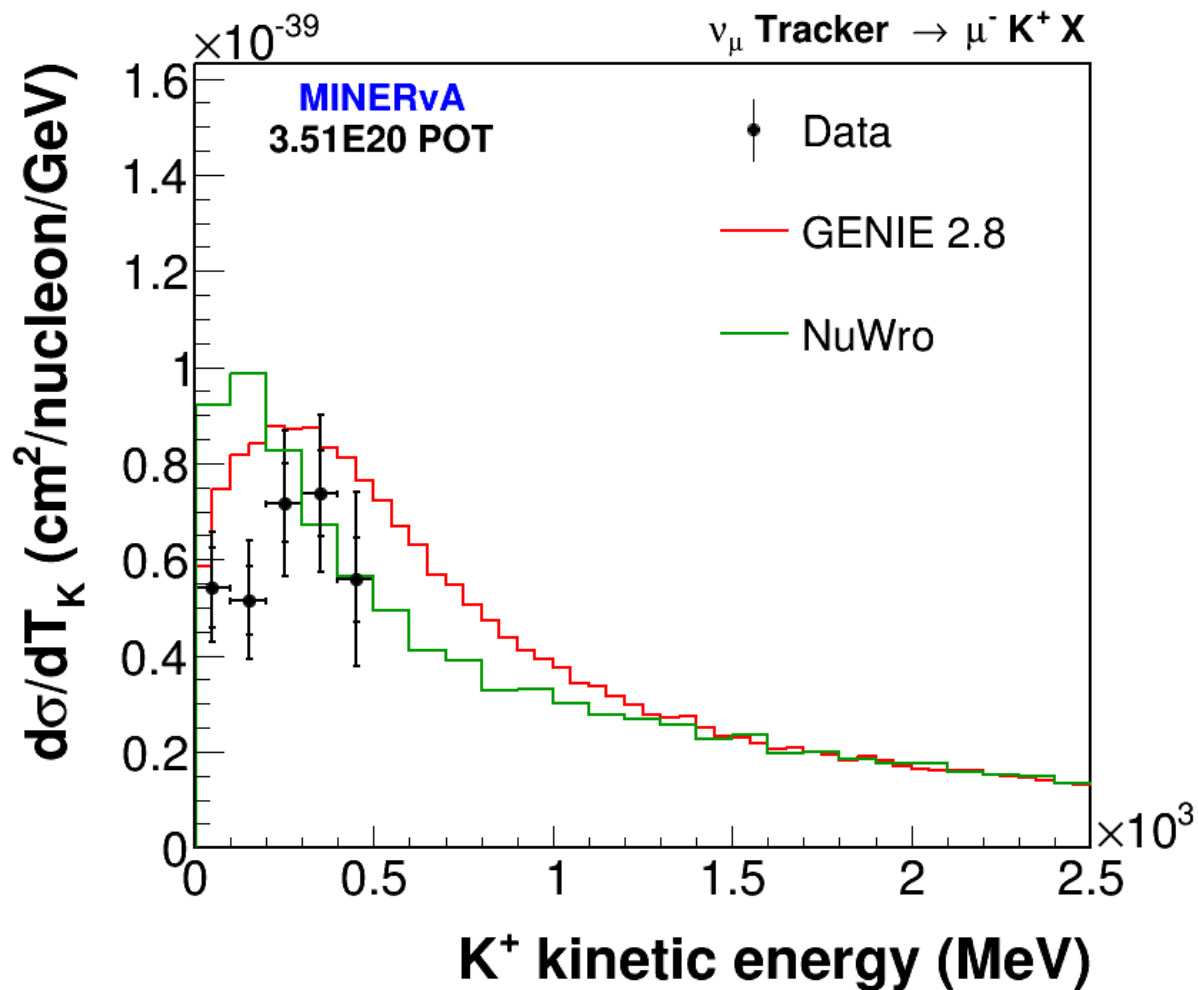


CC efficiency-corrected



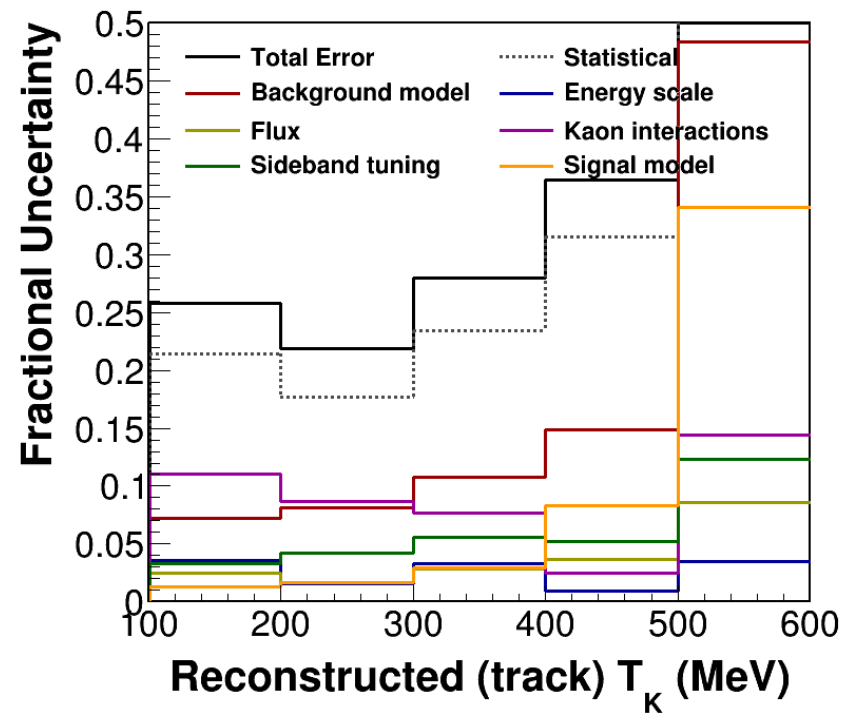
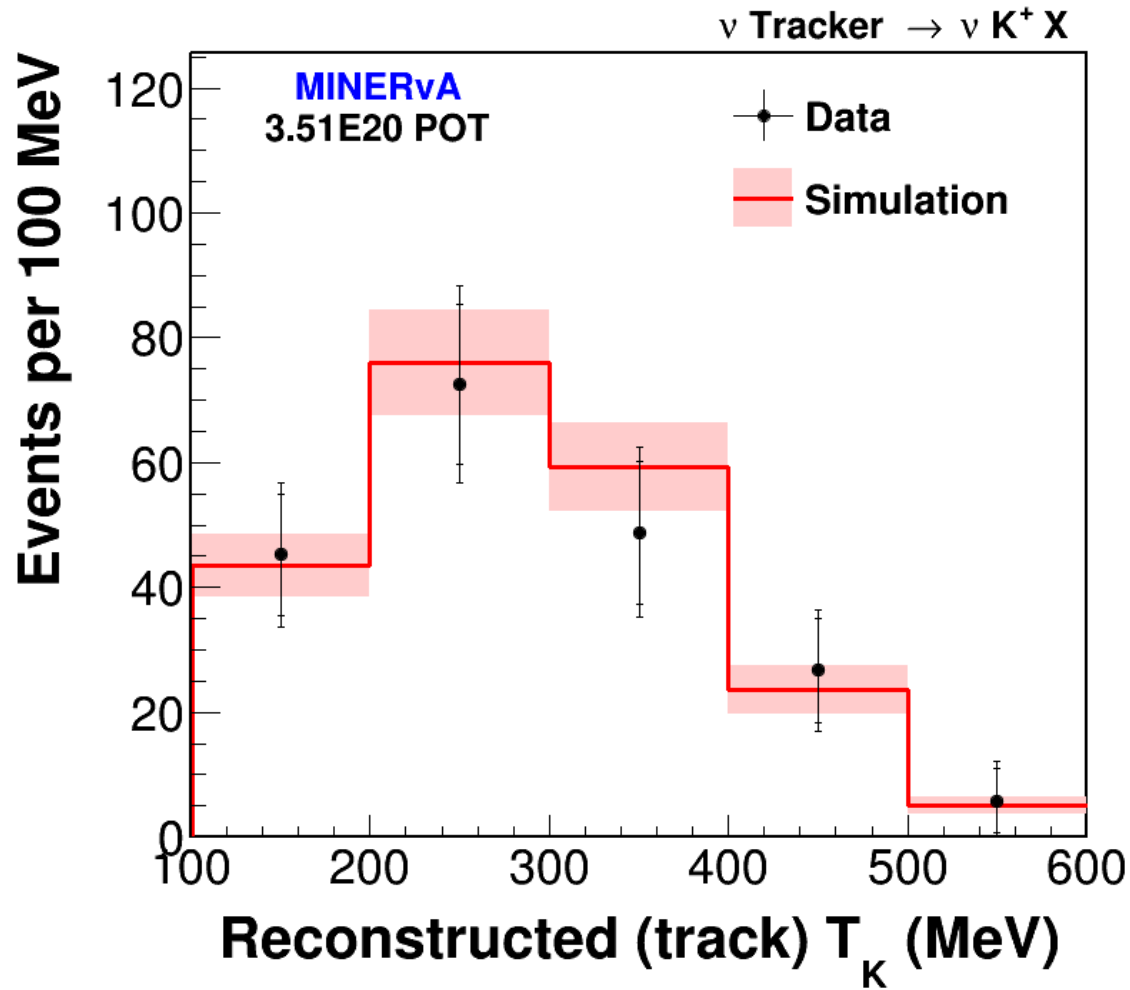


CC XS: zoomed out

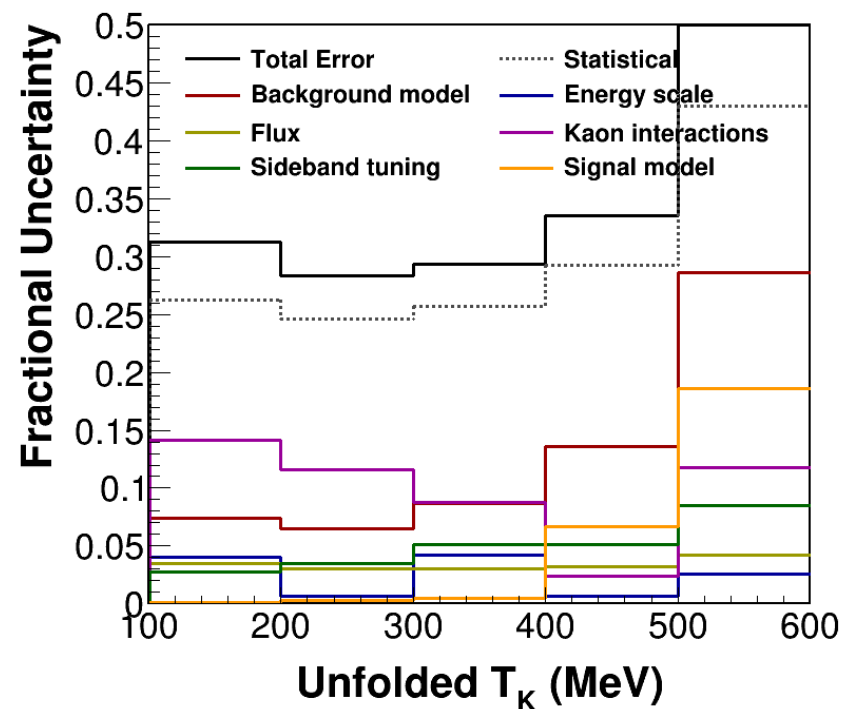
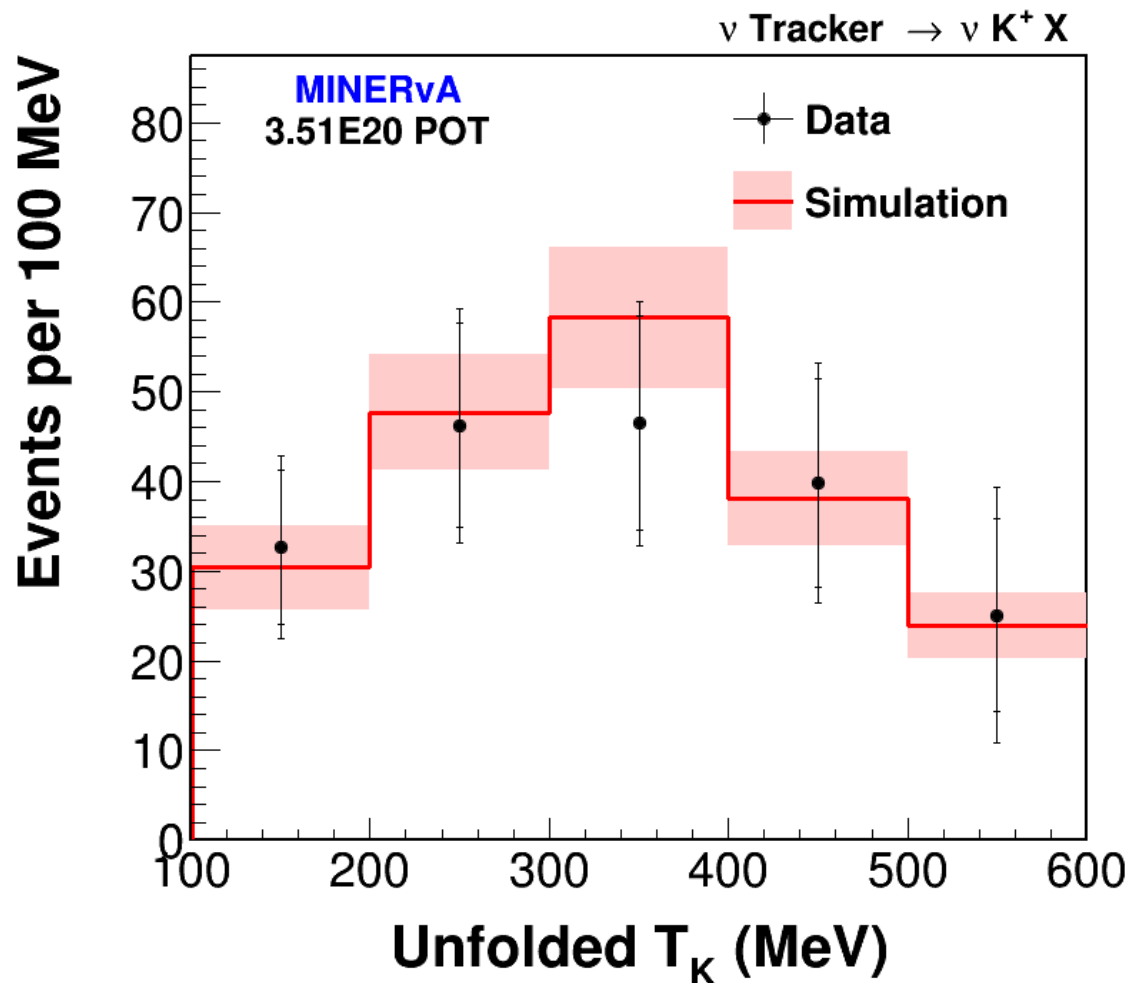




NC background-subtracted

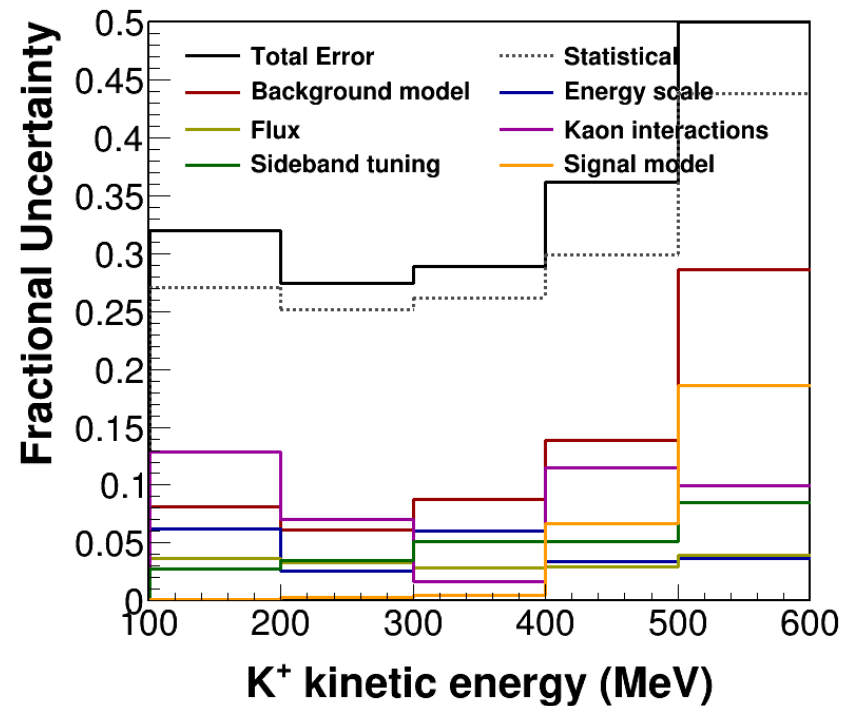
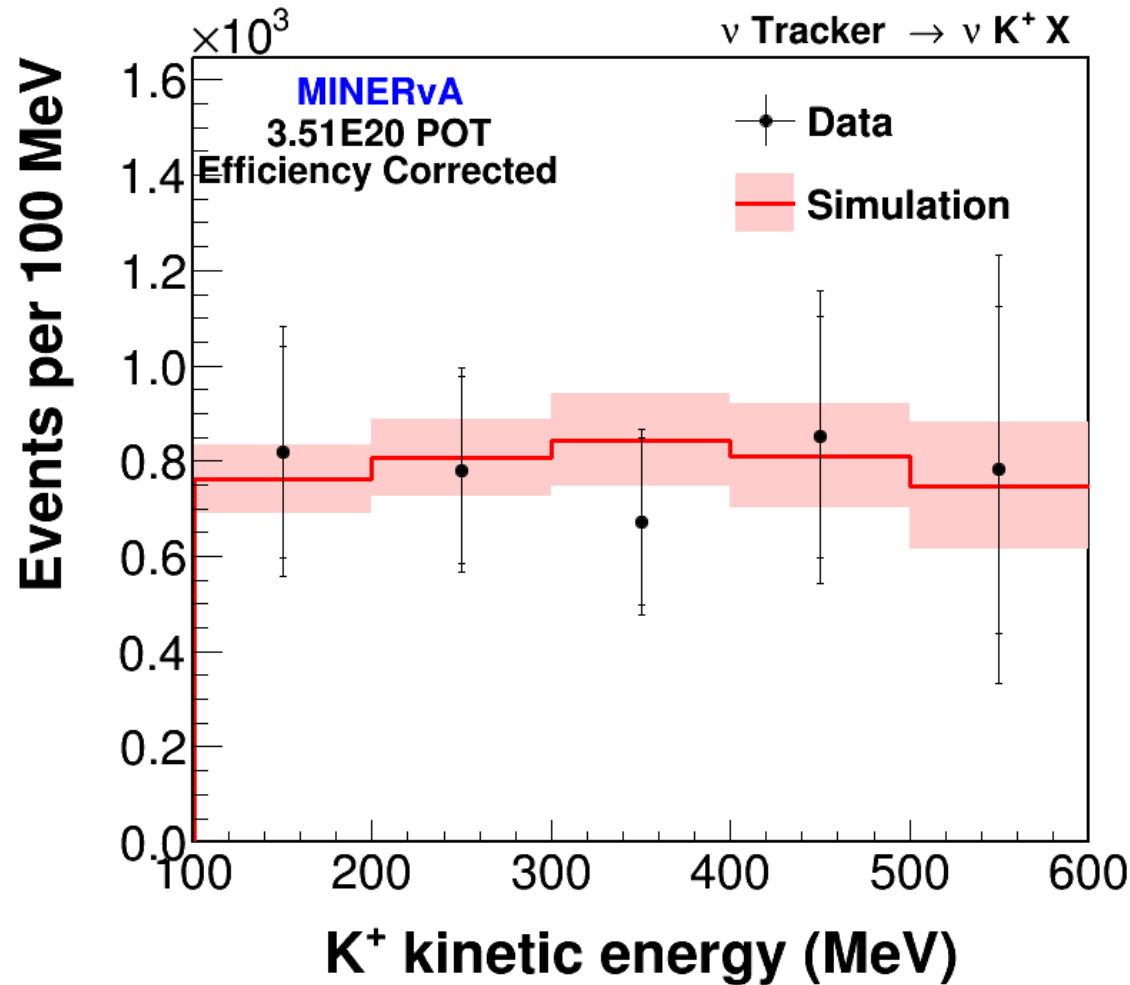
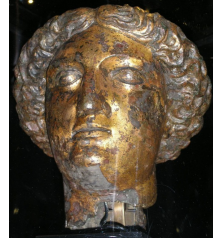


NC unfolded



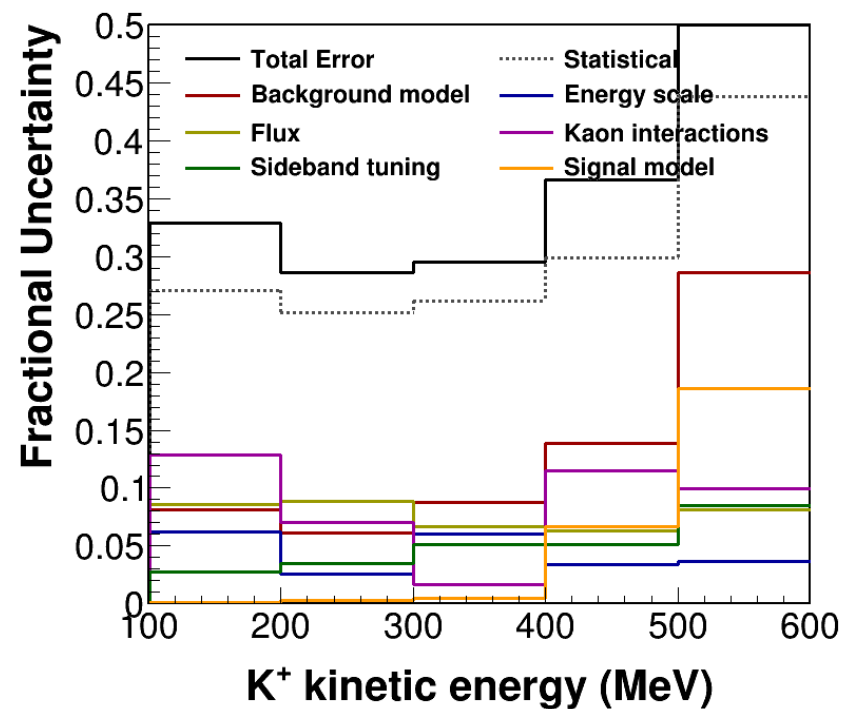
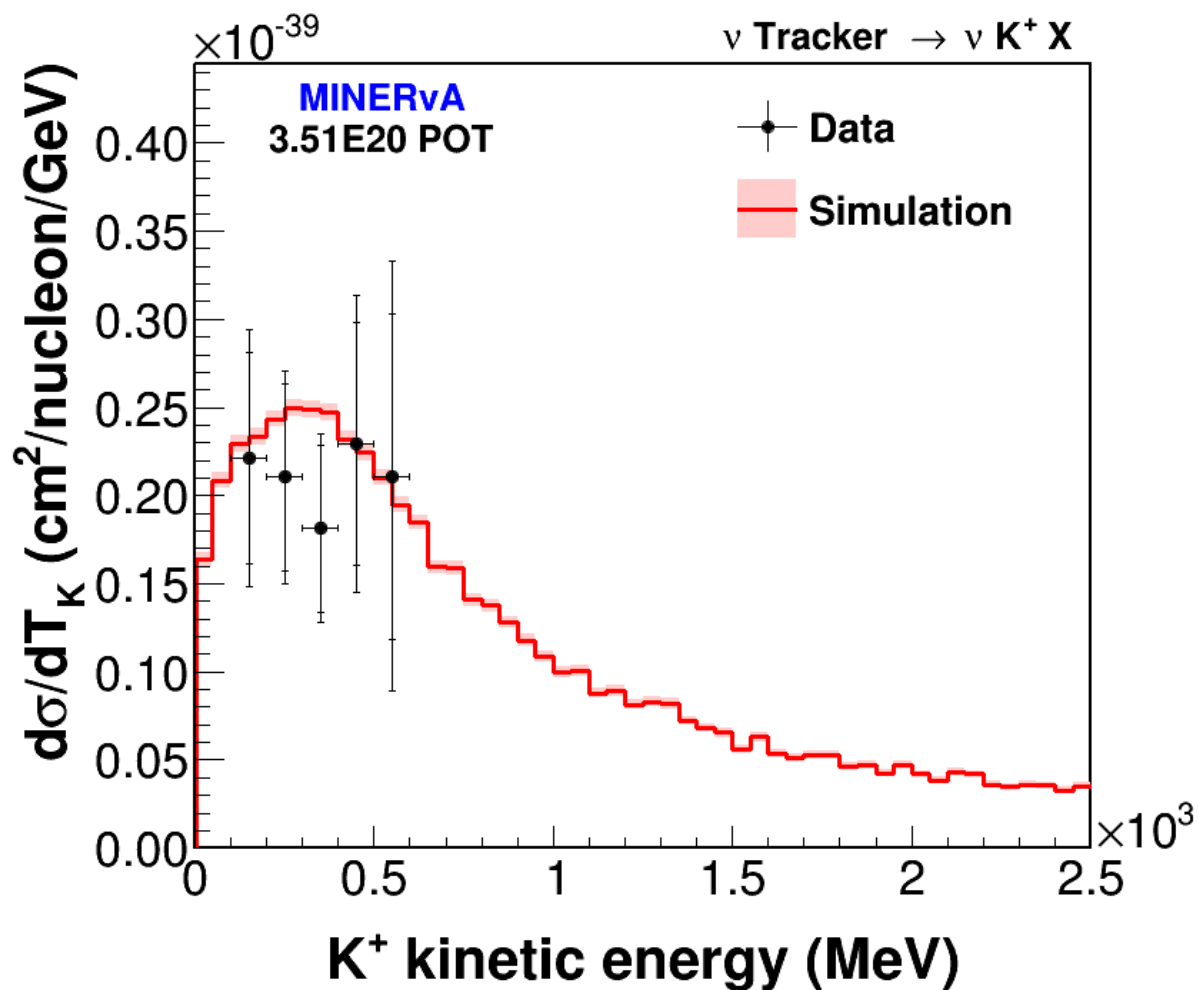


NC efficiency-corrected



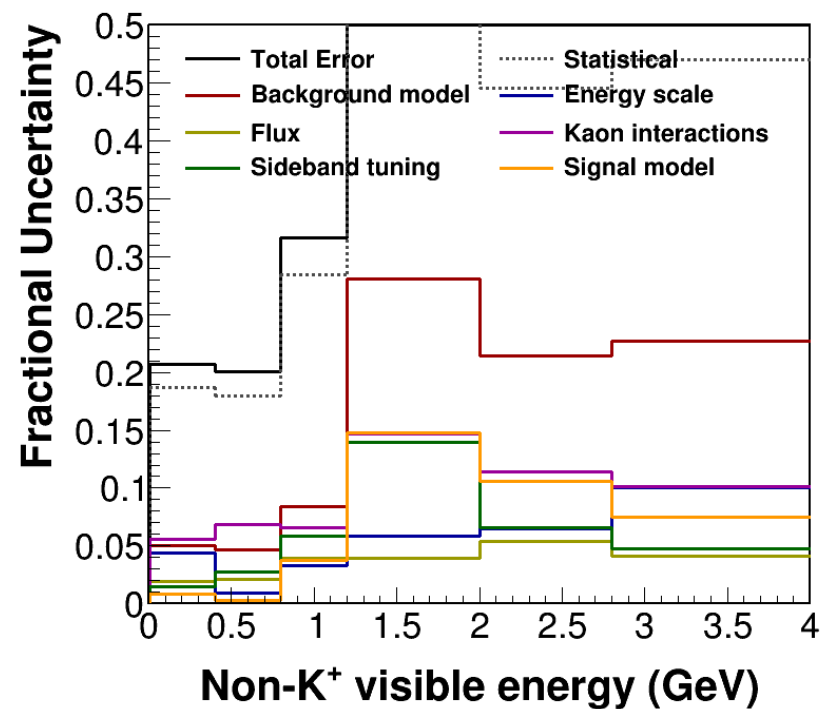
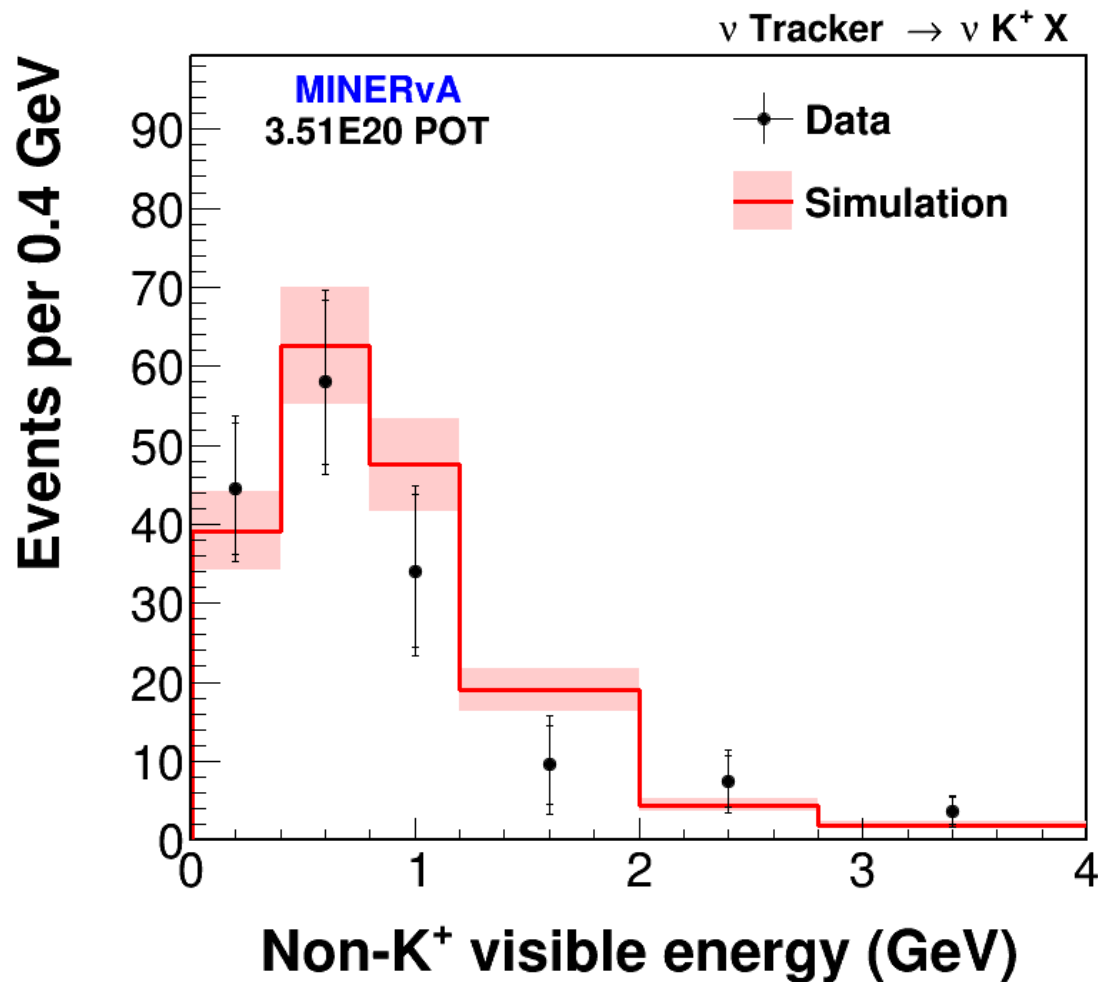


NC XS: zoomed out

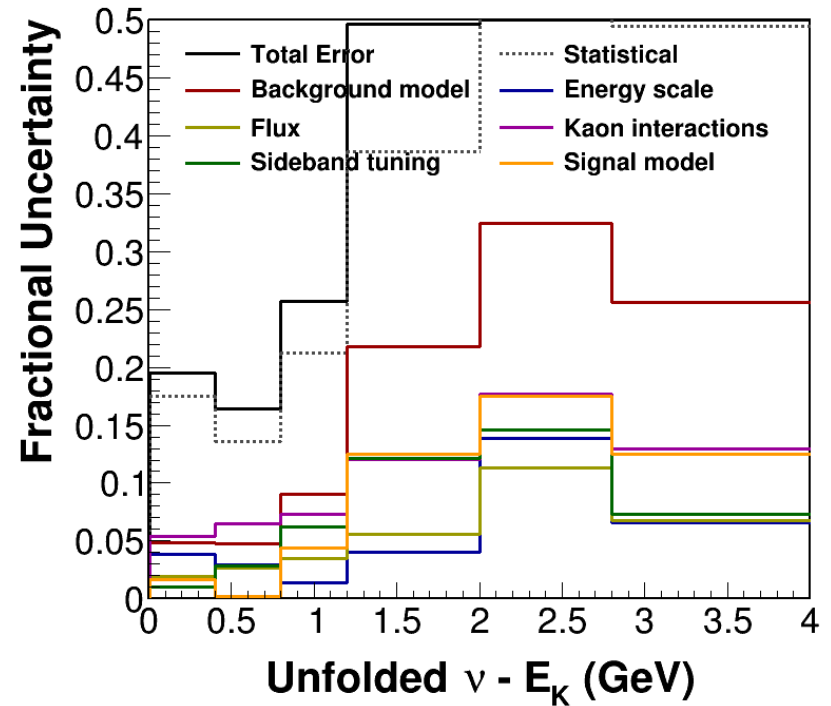
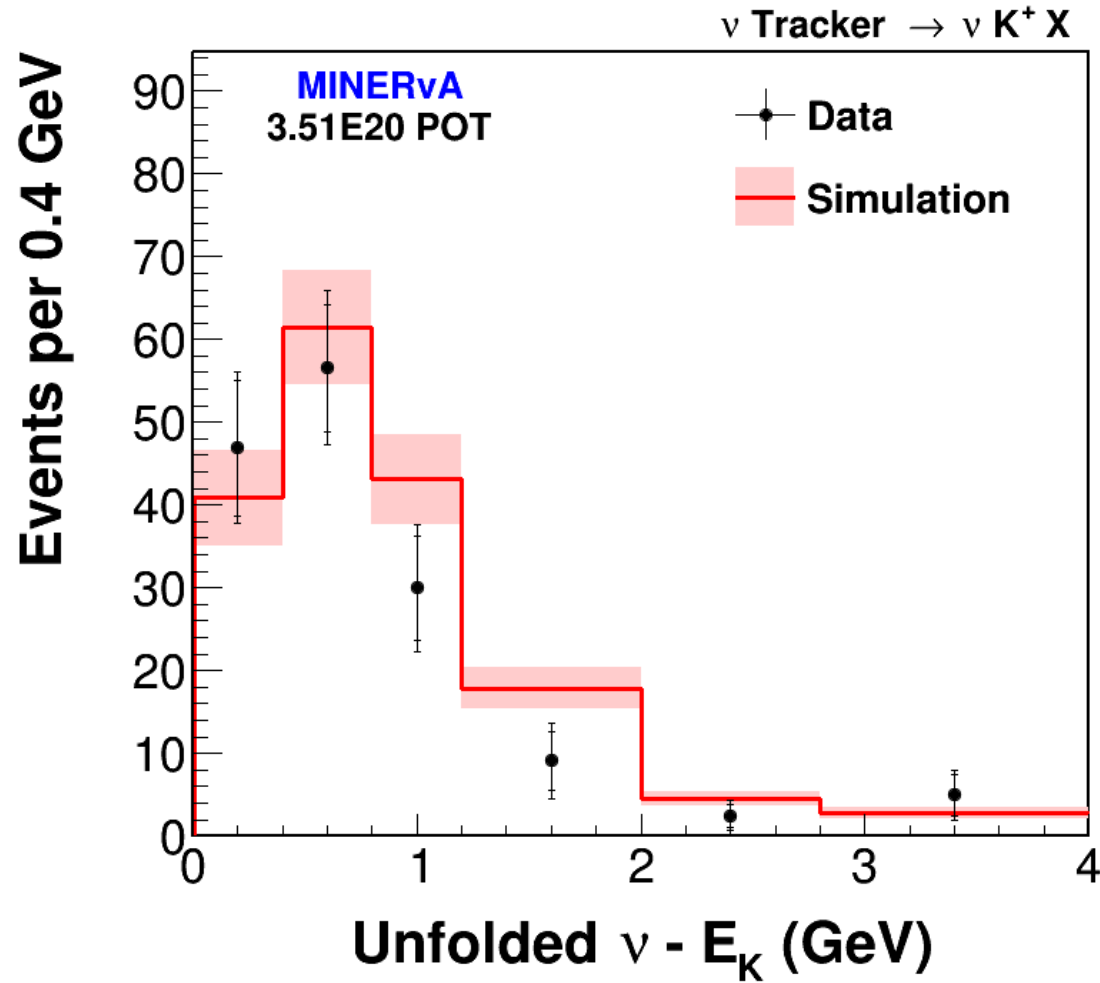
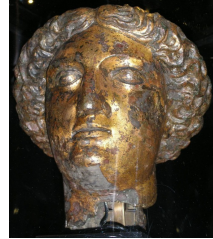




NC visible energy background-subtracted

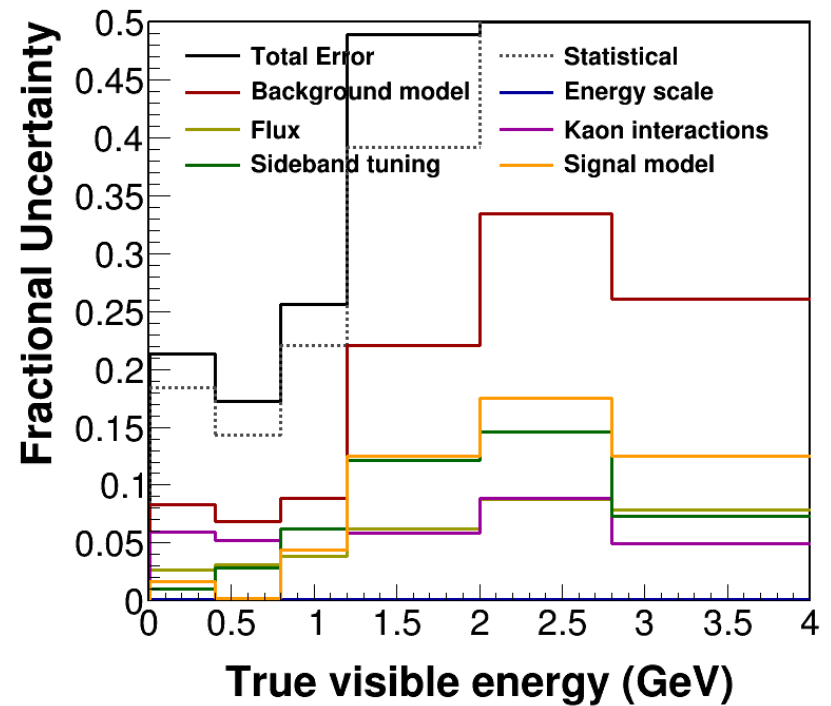
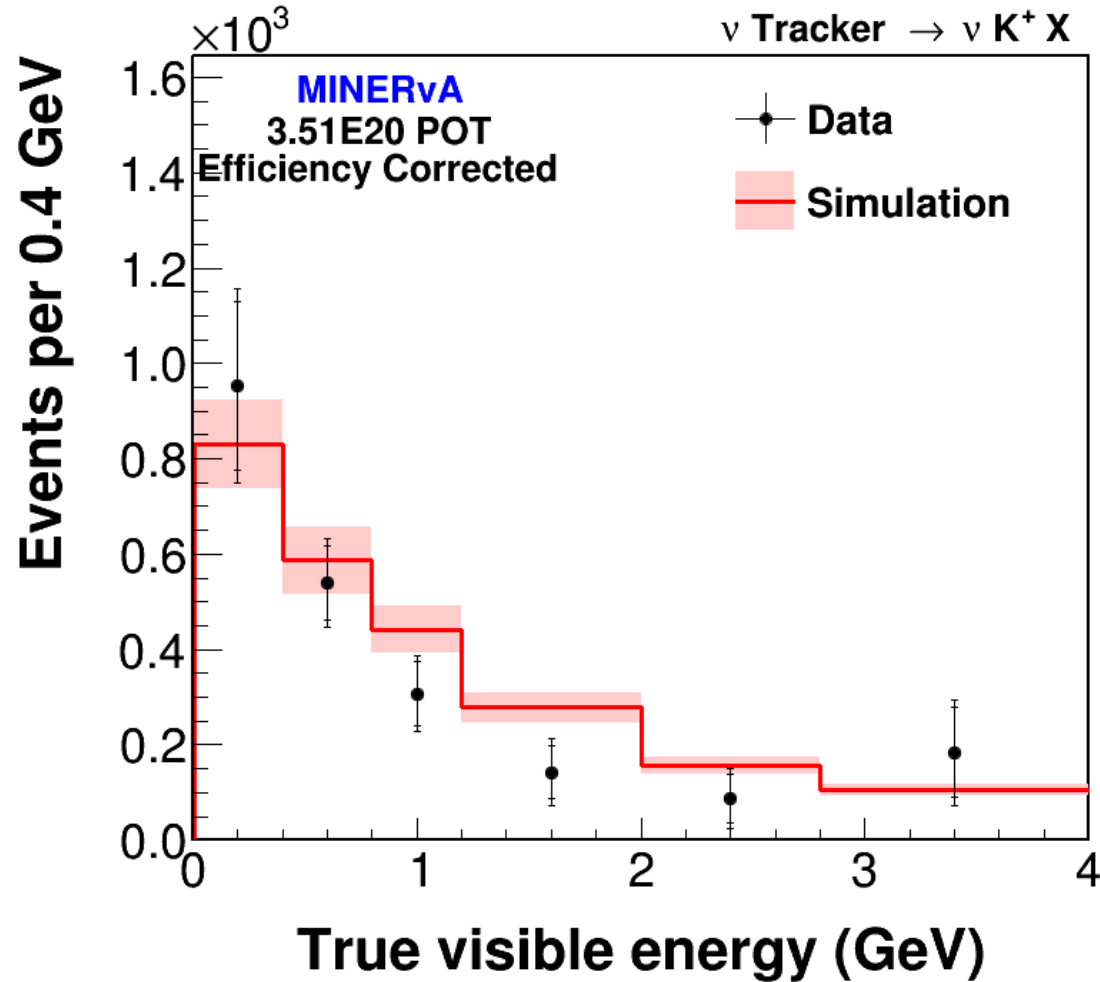
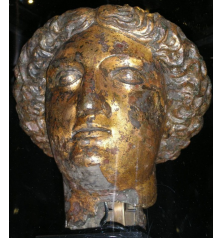


NC visible energy unfolded



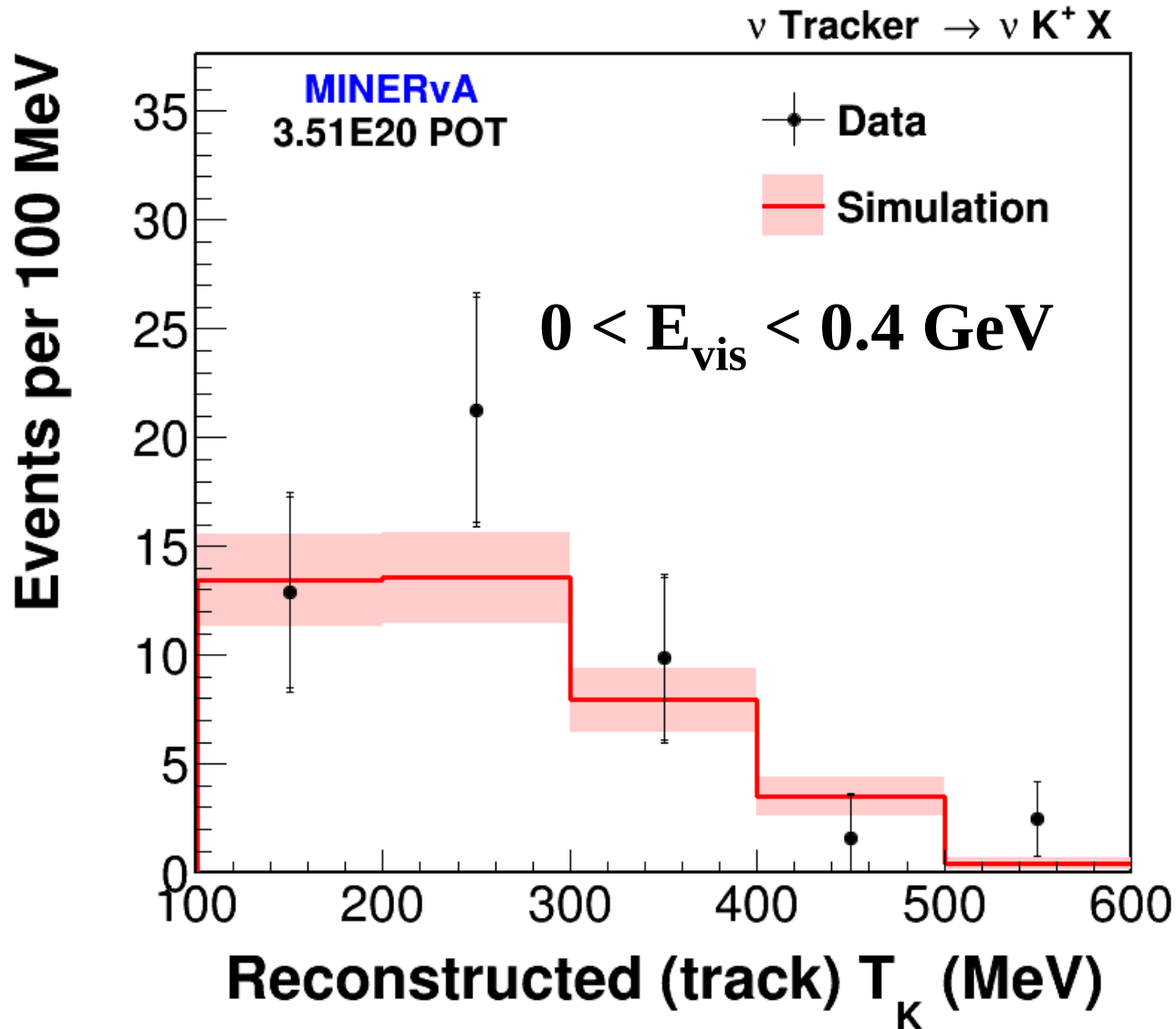
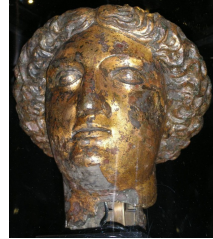


NC visible energy unfolded

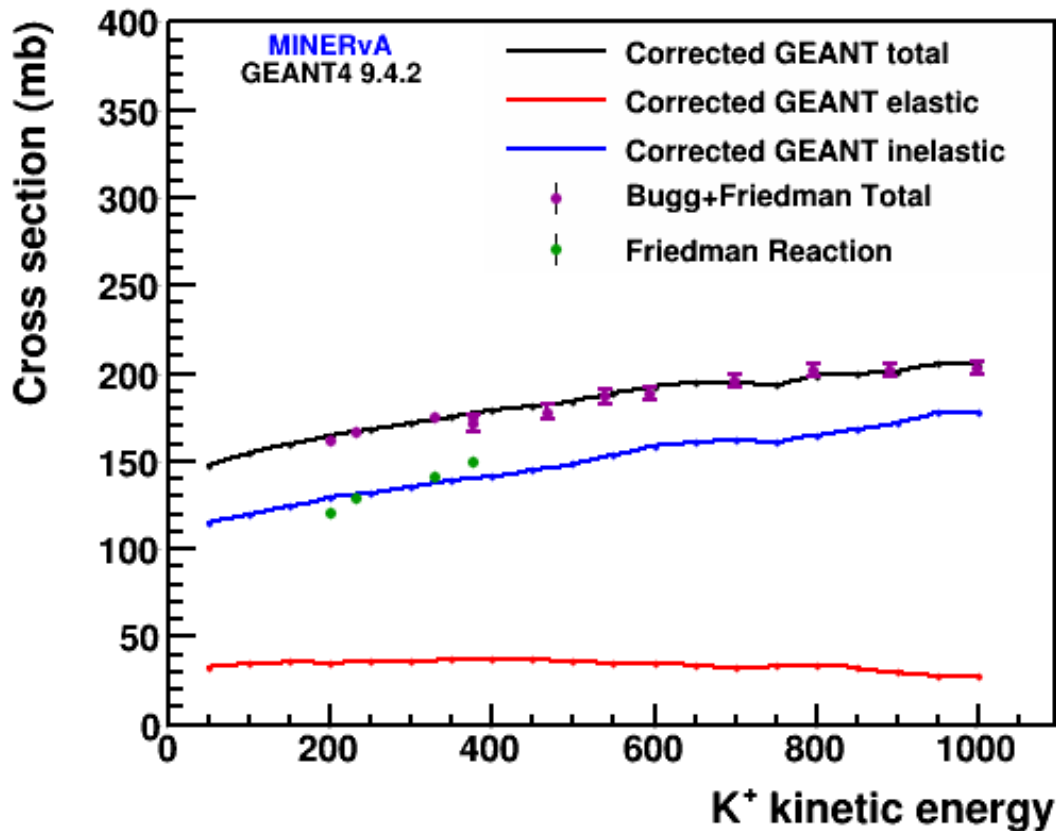
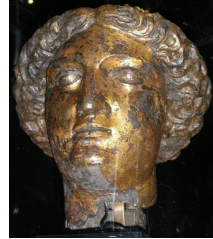




NC kinetic energy in lowest visible energy bin only



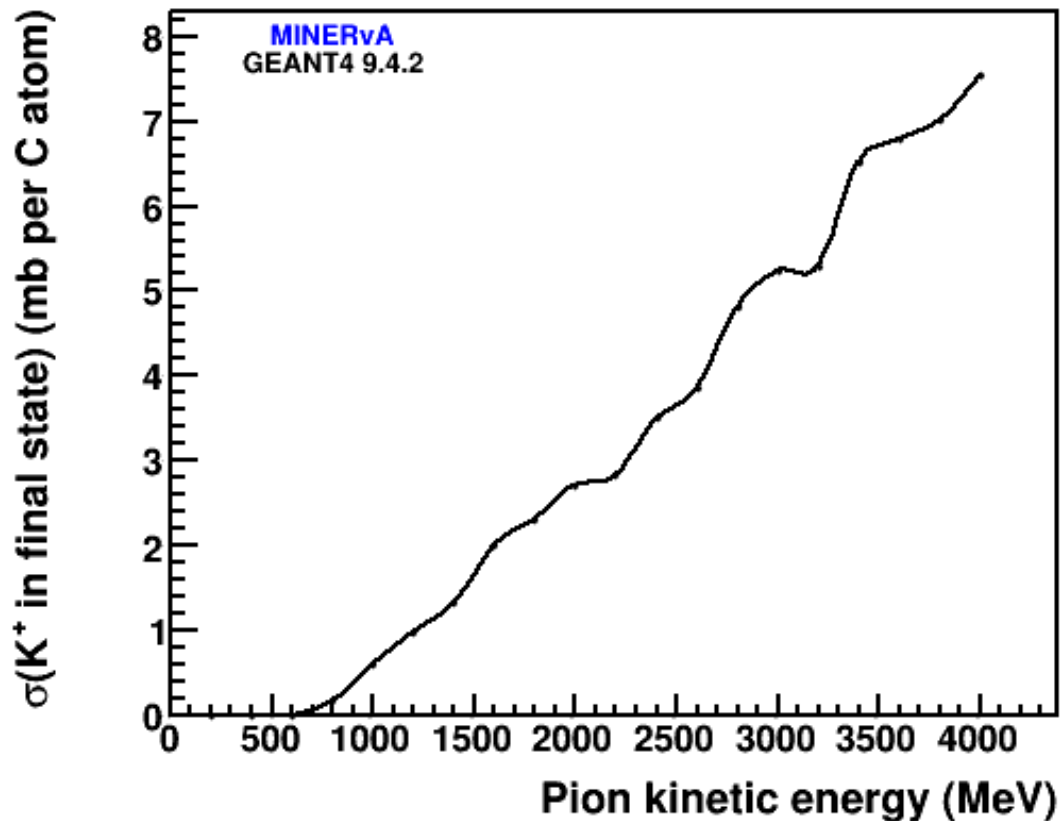
Kaon-carbon interactions



Force agreement between GEANT4 (old version) and external data by reweighting events based in interaction fate

Take $\pm 10\%$ uncertainty on inelastic cross section, which covers disagreement conservatively

$\pi^+C \rightarrow K^+X$ cross section

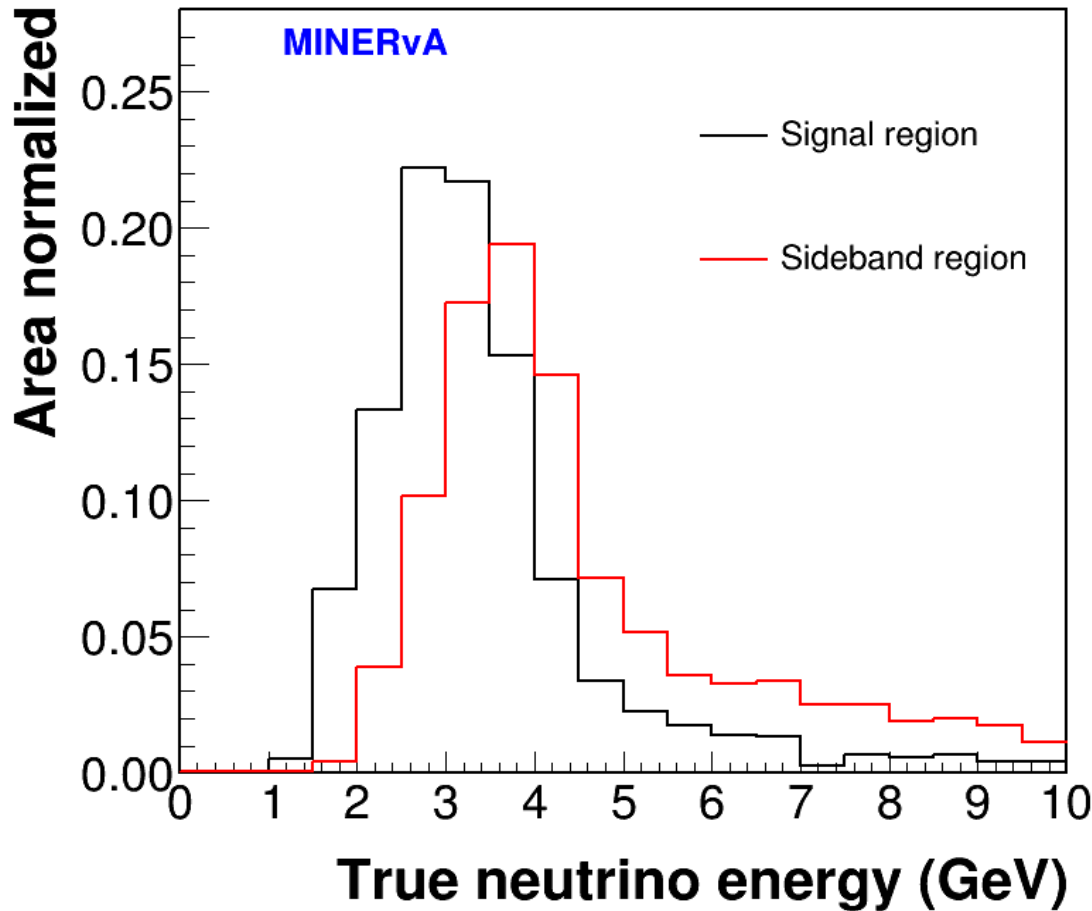
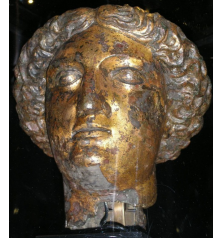


Force agreement between GEANT4 (old version) and external data by reweighting events based in interaction fate

Take $\pm 10\%$ uncertainty on inelastic cross section, which covers disagreement conservatively



NC sideband constraint on CC events: neutrino energy

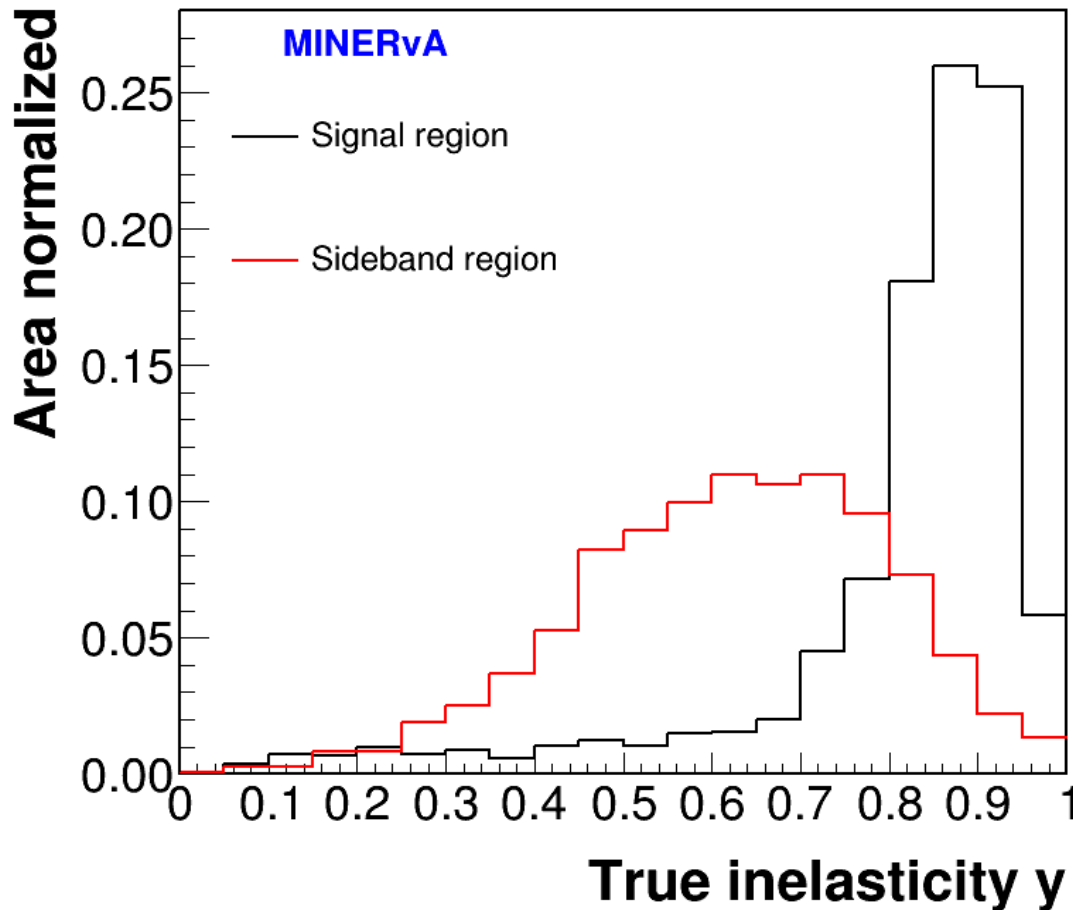
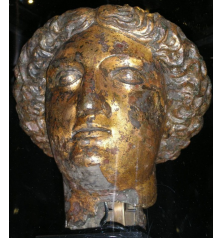


Flux error enters because signal region is low-energy muons, which tend to come from lower-energy neutrinos

Sideband region includes flux tail, where uncertainties are generally larger



NC sideband constraint on CC events: y distribution

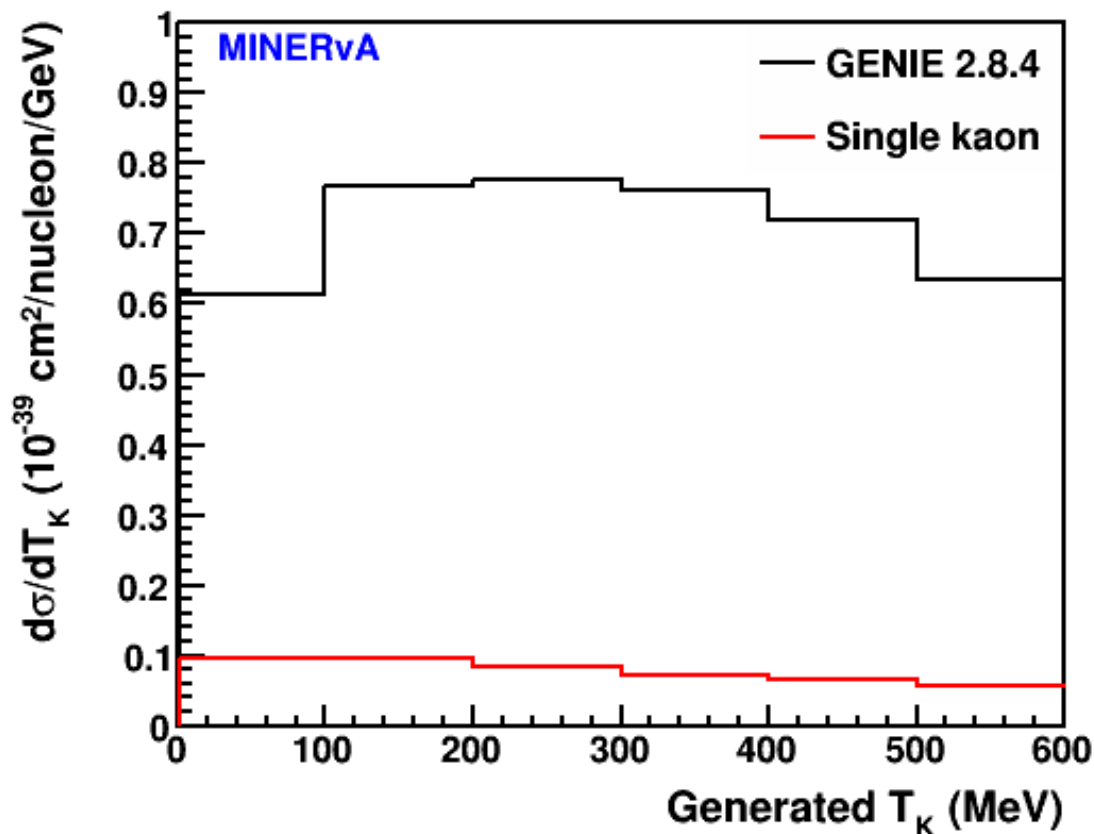


Signal region is very high y because muon energy is small (< 500 MeV)

Sideband region is all muons > 500 MeV, which is lower inelasticity, but we exclude very low y events from the sideband to reduce the extrapolation



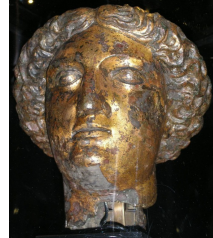
Single kaon production



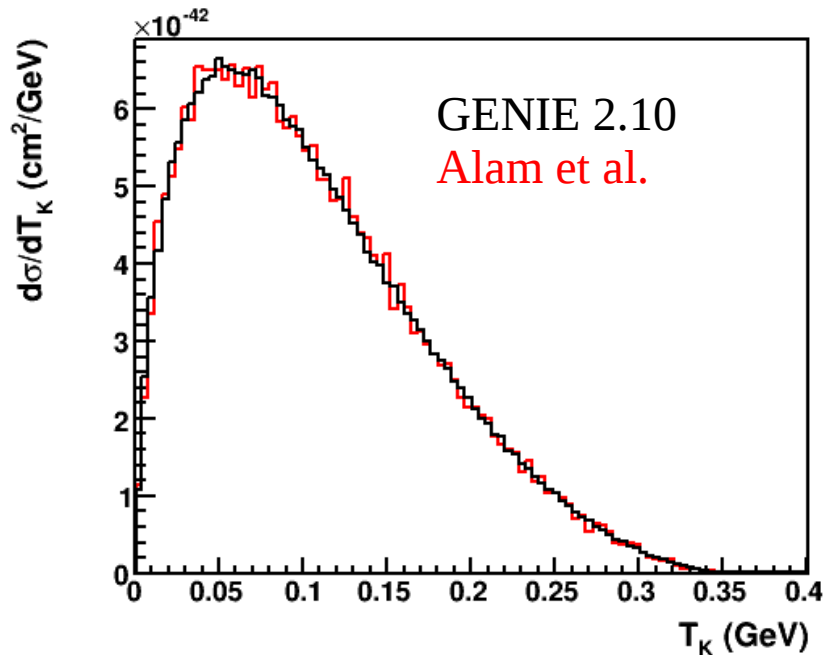
~10% of total cross section for MINERvA flux, according to this one model

Combine SK and nominal samples by fixing cross section as a function of W

Single kaon production



1.0 GeV $\nu_\mu p \rightarrow \mu^- K^+ p$



Cabibbo-suppressed channel
 $\nu_\mu N \rightarrow \mu^- K^+ N$ is not in GENIE 2.8

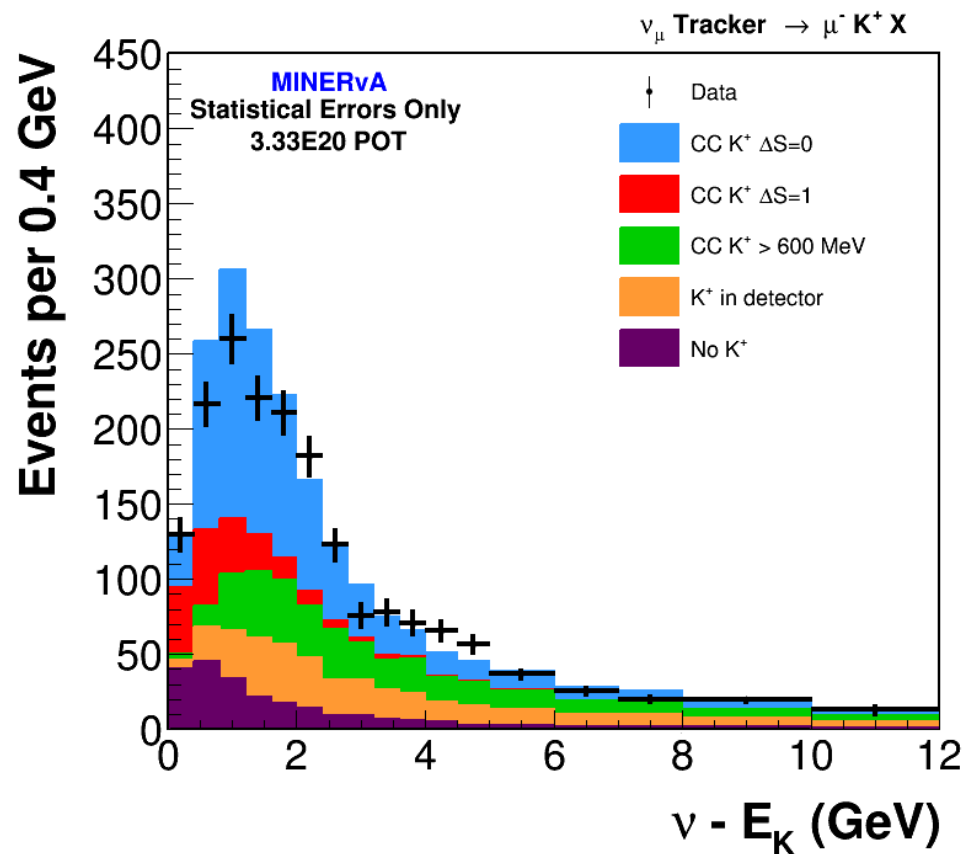
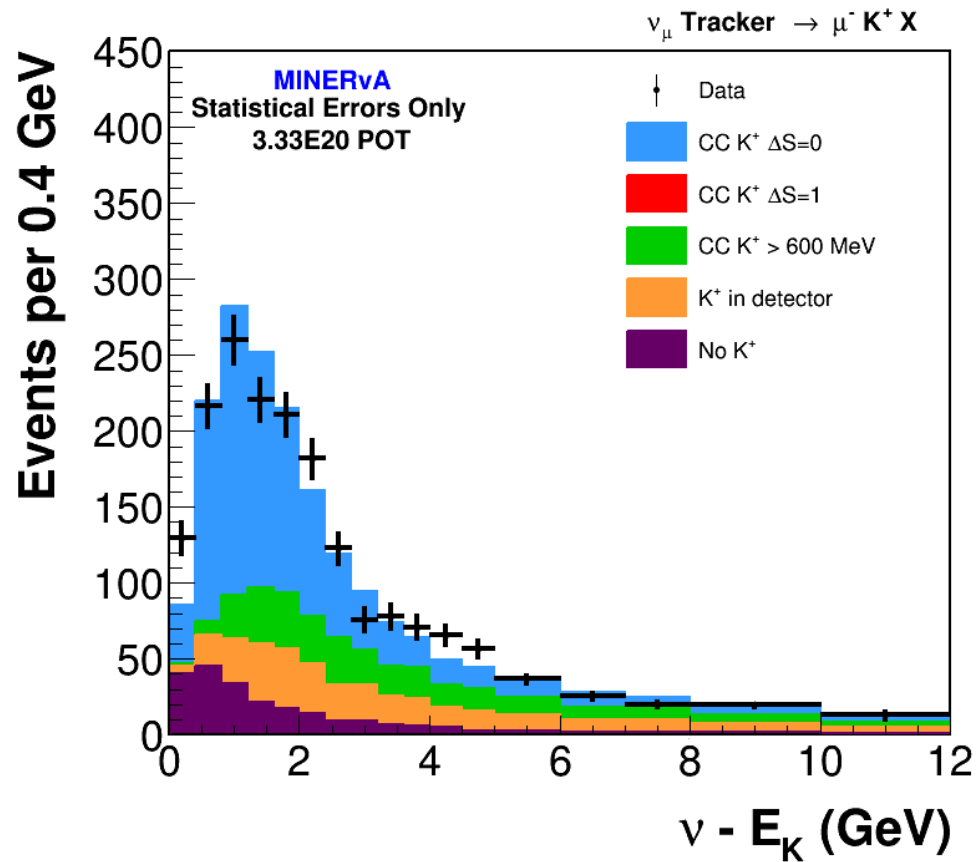
Potentially important, if acceptance is different for these events

Implemented based on Alam et al. Phys.Rev. **D82** 033001 (2010), and in GENIE 2.10

Used to implement a correction in this analysis

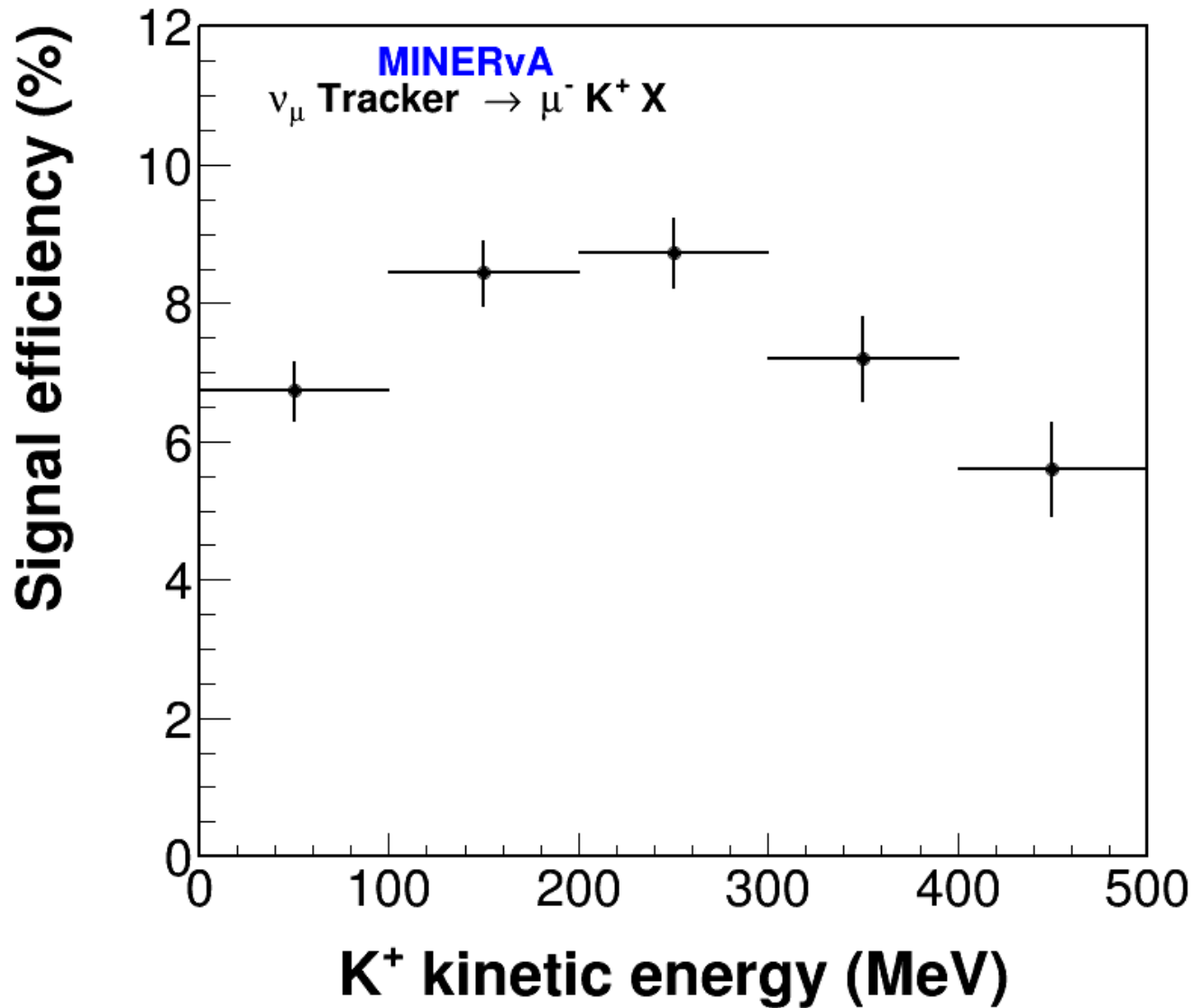


SK hadronic energy distribution



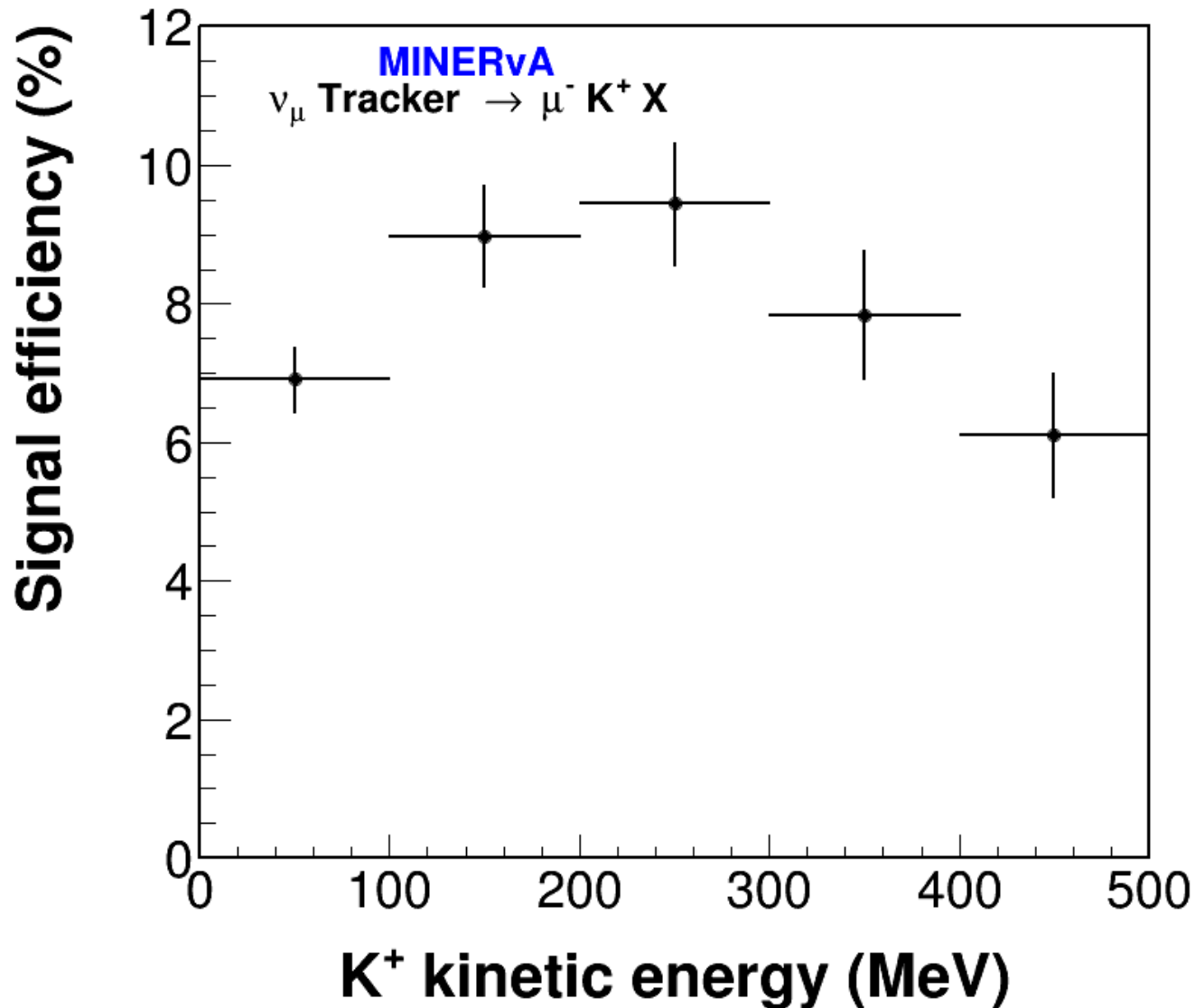
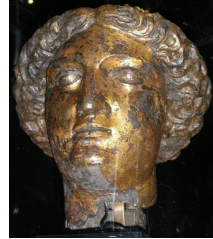


Nominal efficiency



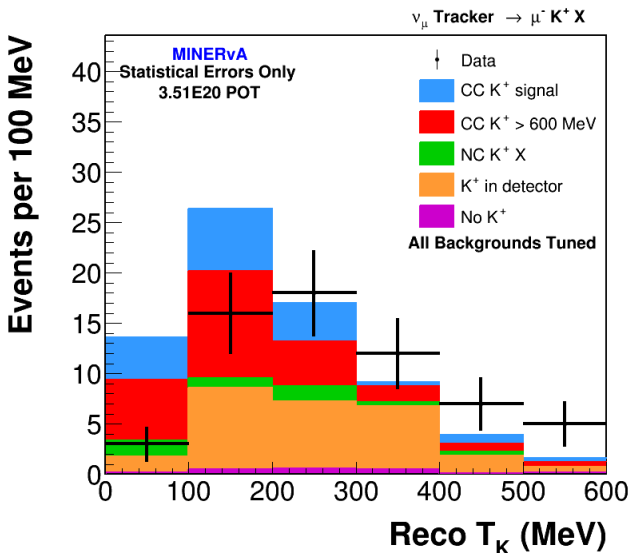
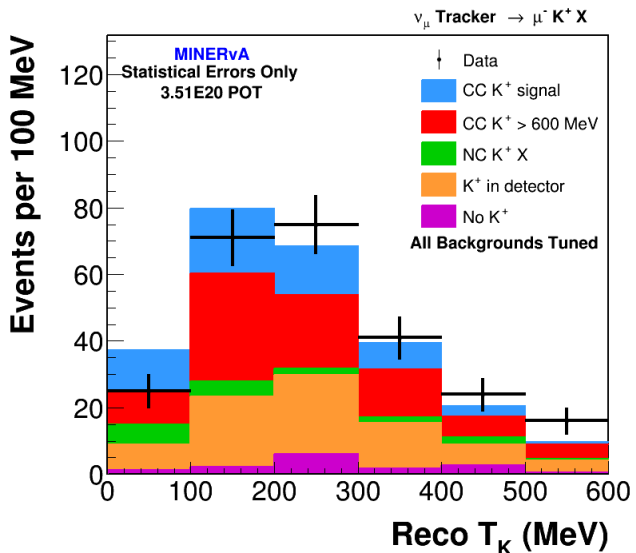
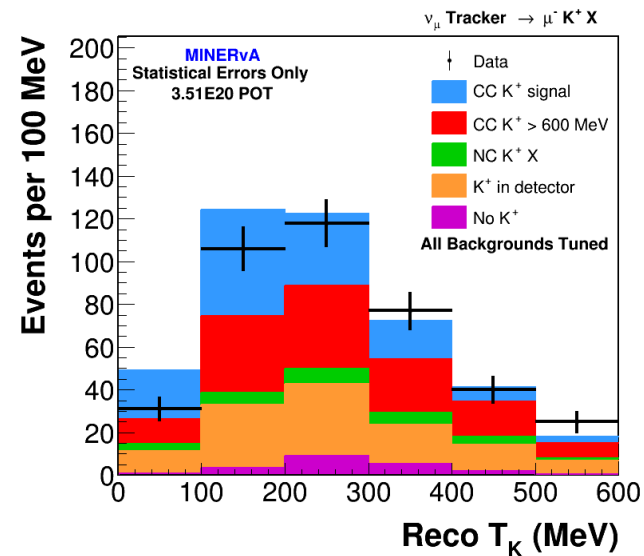
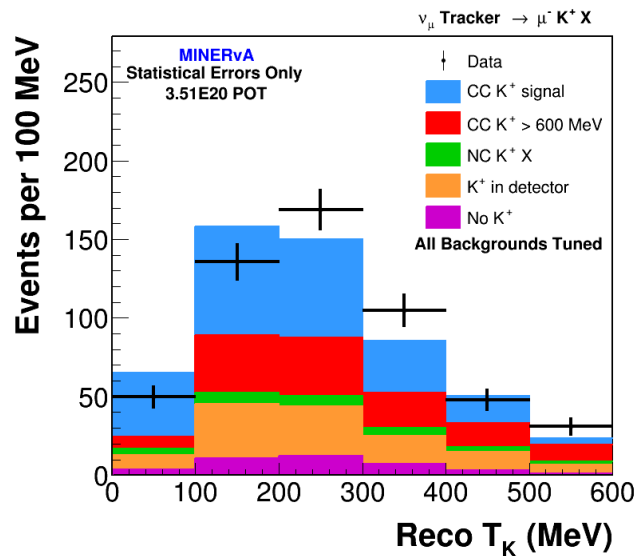
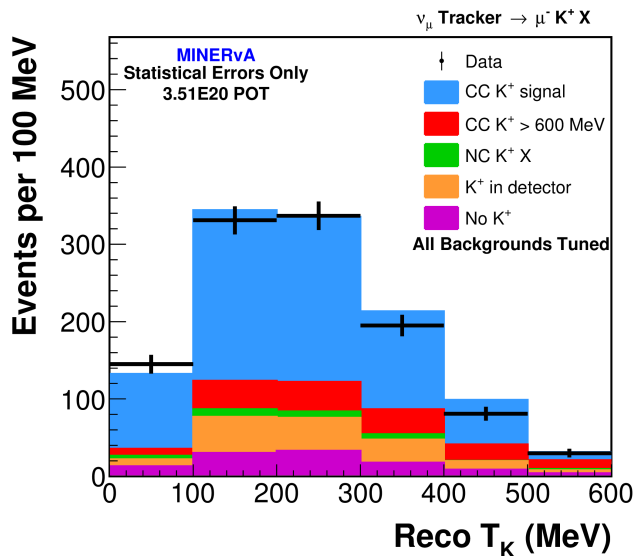


Corrected efficiency





Kaon kinetic energy vs. E_{vis}



Reconstructed kinetic energy in slices of hadronic visible energy

In reading order:

$0 < E_{vis} / \text{GeV} < 2$

$2 < E_{vis} / \text{GeV} < 4$

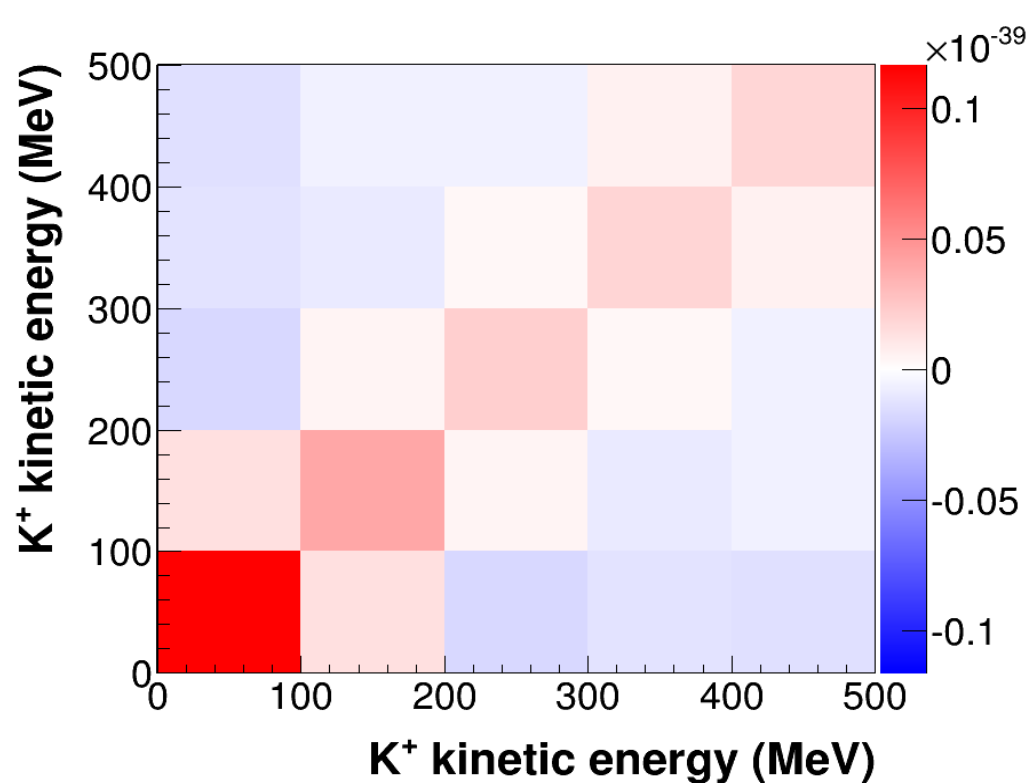
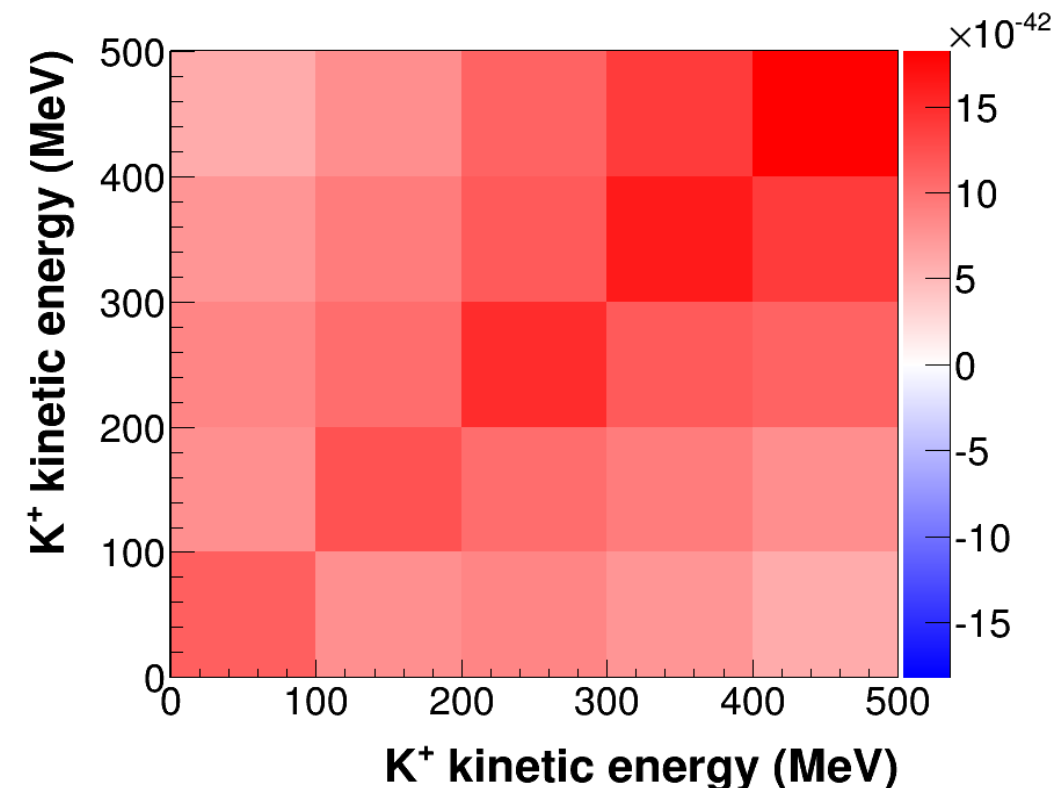
$4 < E_{vis} / \text{GeV} < 8$

$8 < E_{vis} / \text{GeV} < 20$

$20 < E_{vis} / \text{GeV}$



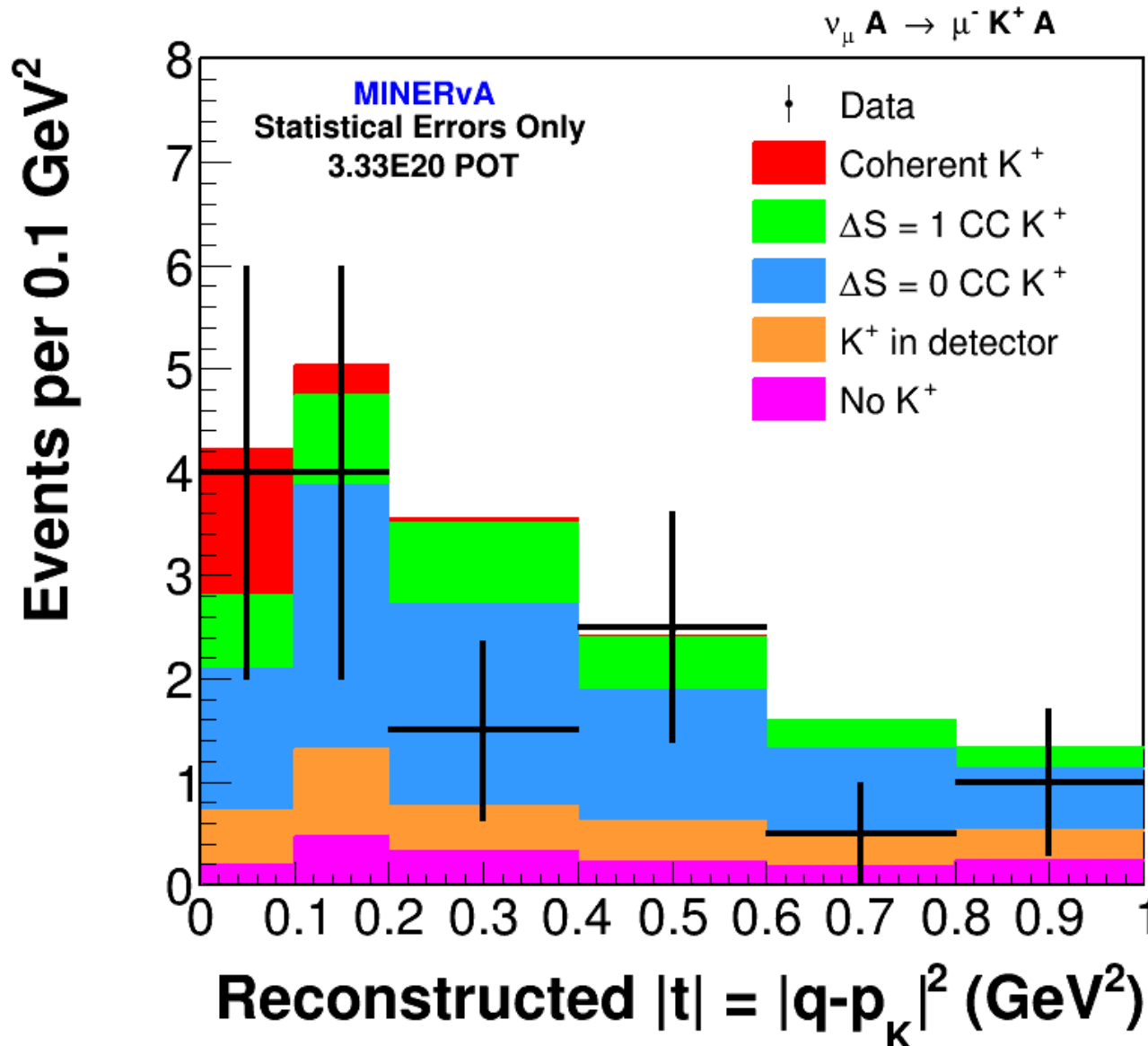
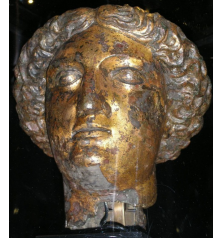
Covariance matrices: CC



Systematic uncertainties only (left), statistical uncertainty only, which enters via the unfolding procedure

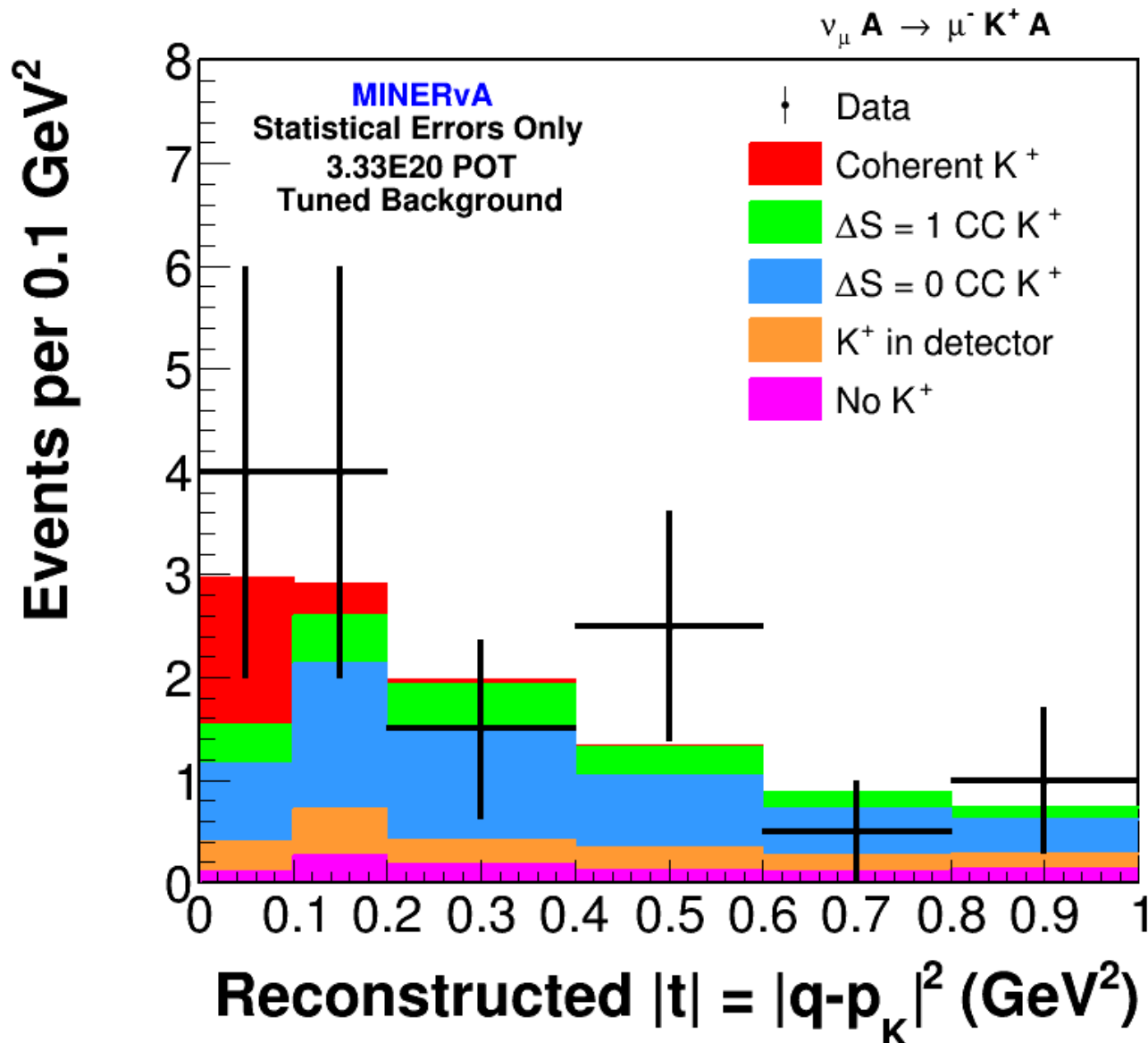


Coherent t raw background



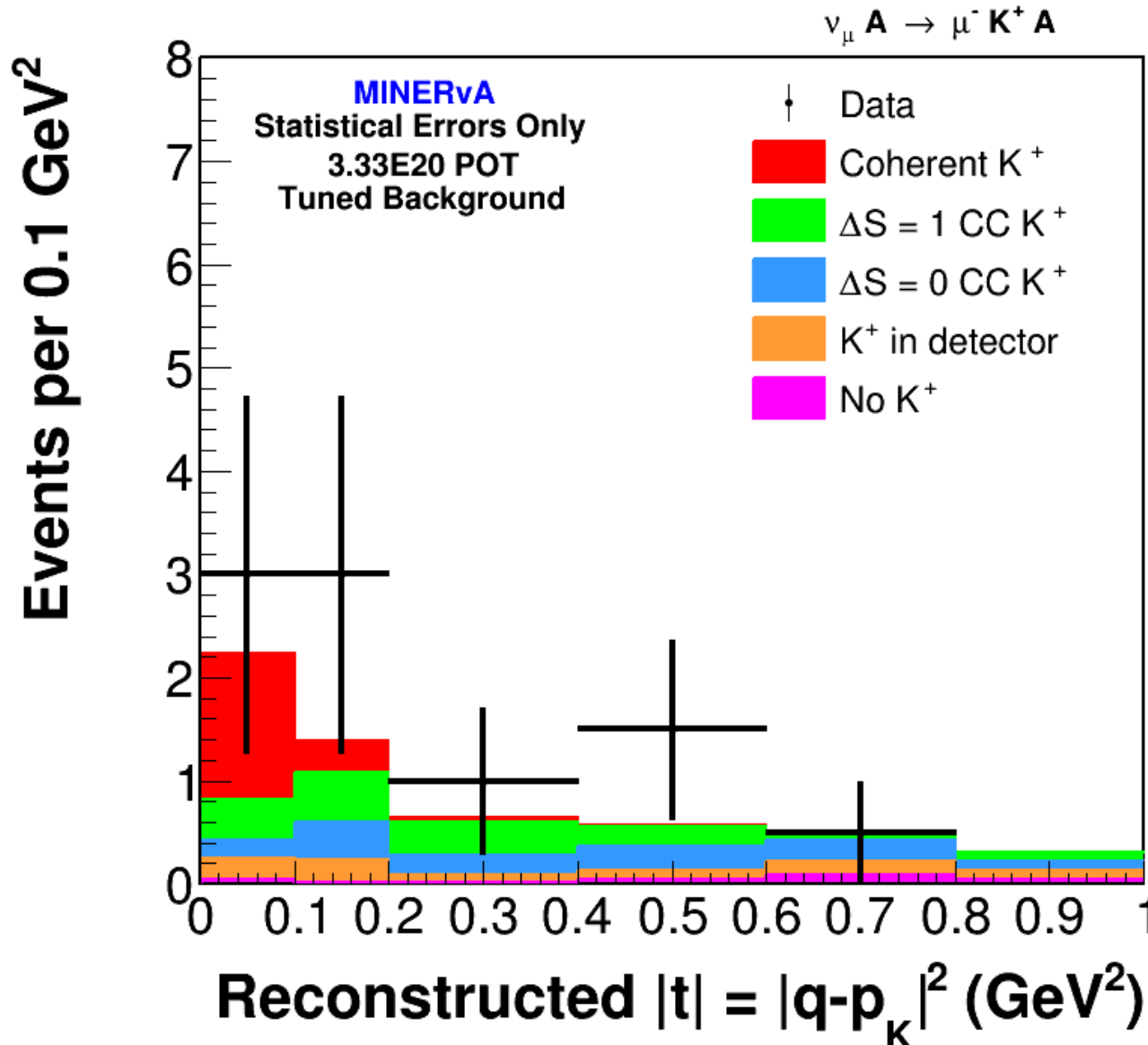
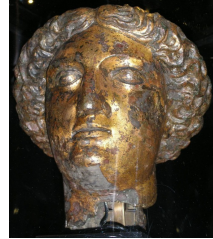


Coherent t tuned background



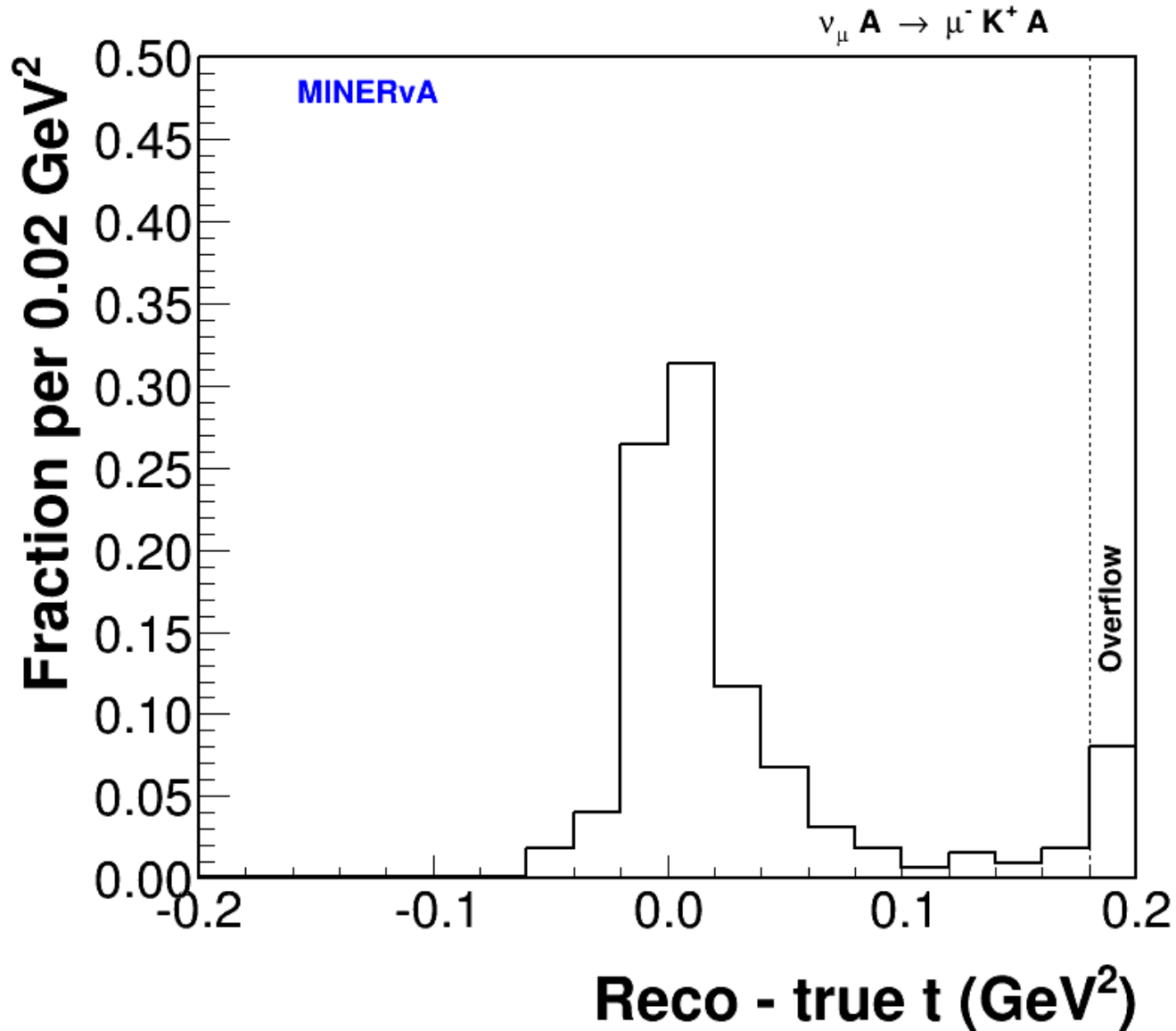


Coherent t tuned background after π^0 rejection scan

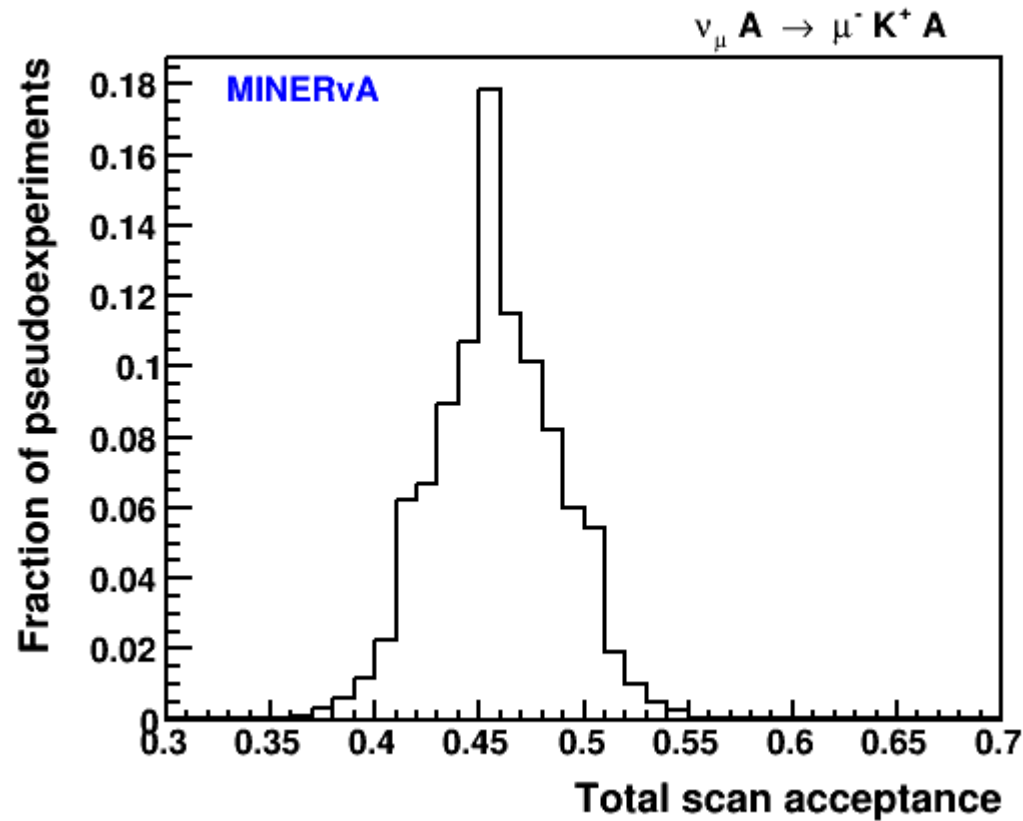
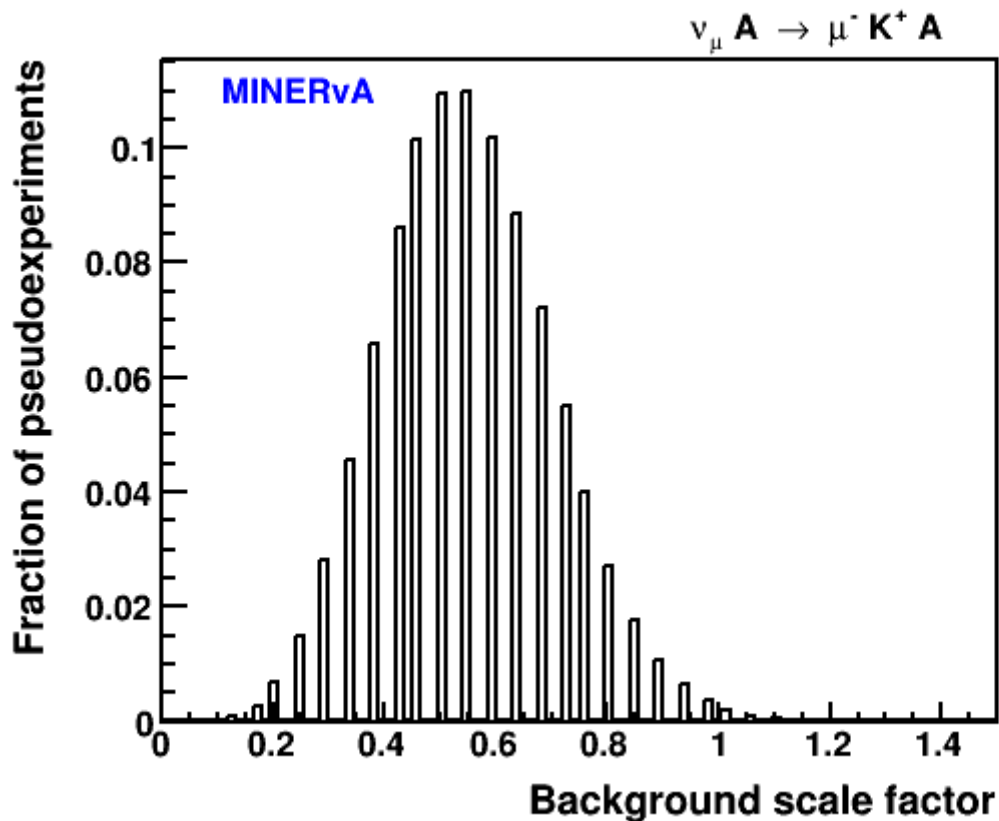
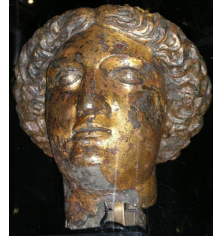




Coherent t residual



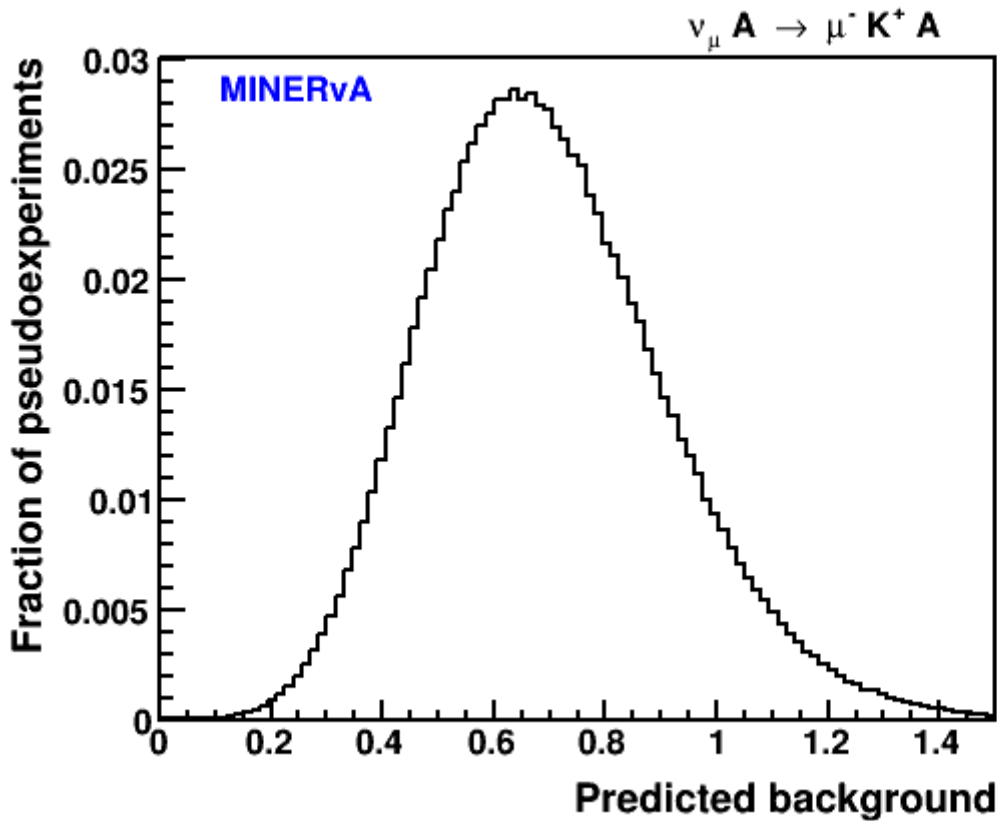
Coherent background prediction



Left: scale factor for background based on sideband constraint

Right: Background acceptance in the π^0 rejection scan

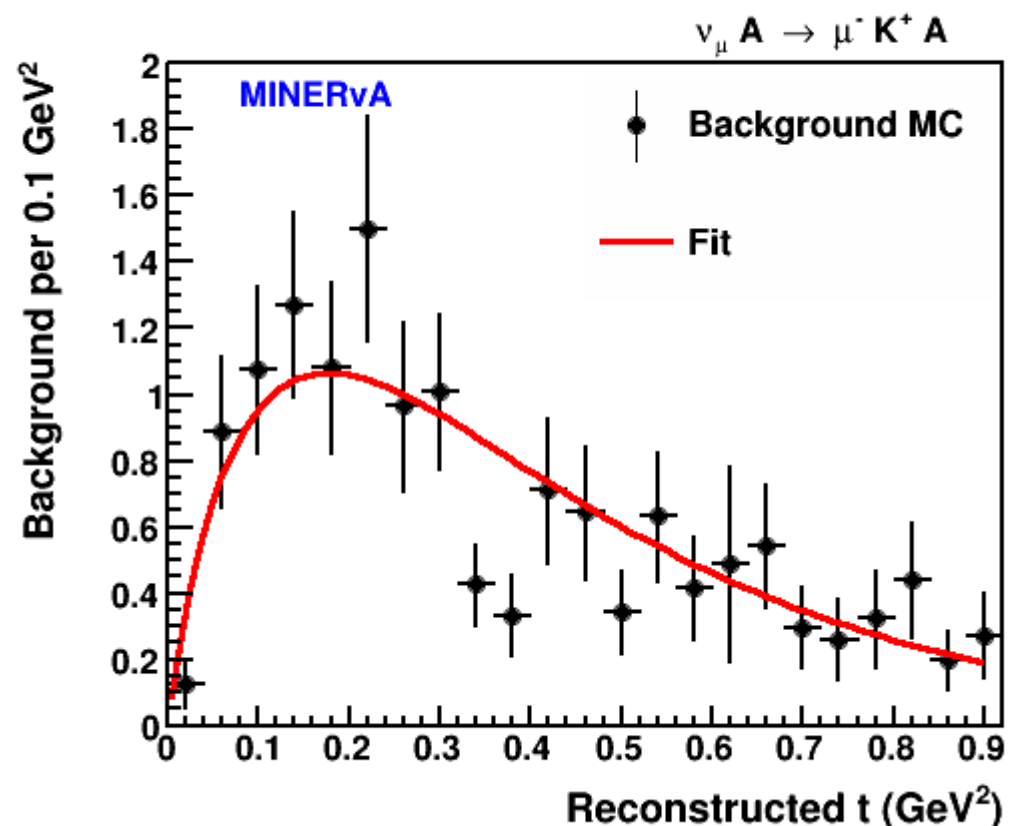
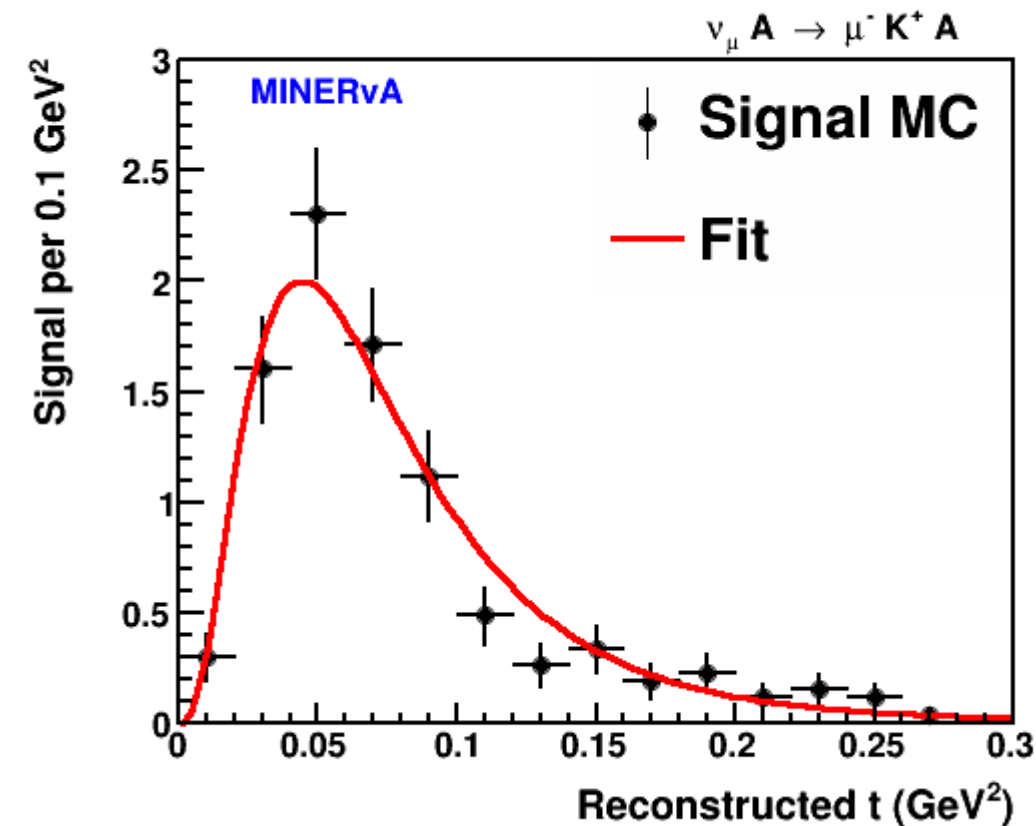
Coherent background prediction



In each pseudoexperiment, scale the nominal background by randomly taking a number from each of the plots on the previous slide and multiplying them together

This plot is the mean number of background events – “observed” background in a pseudoexperiment is a Poisson random number taken from a distribution with this mean

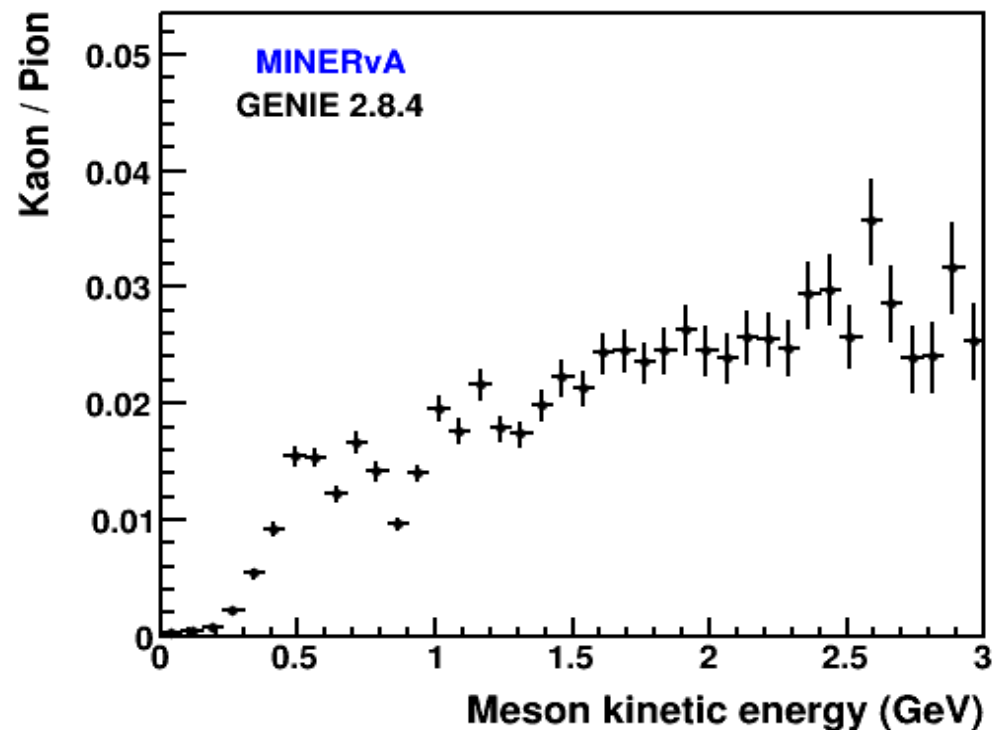
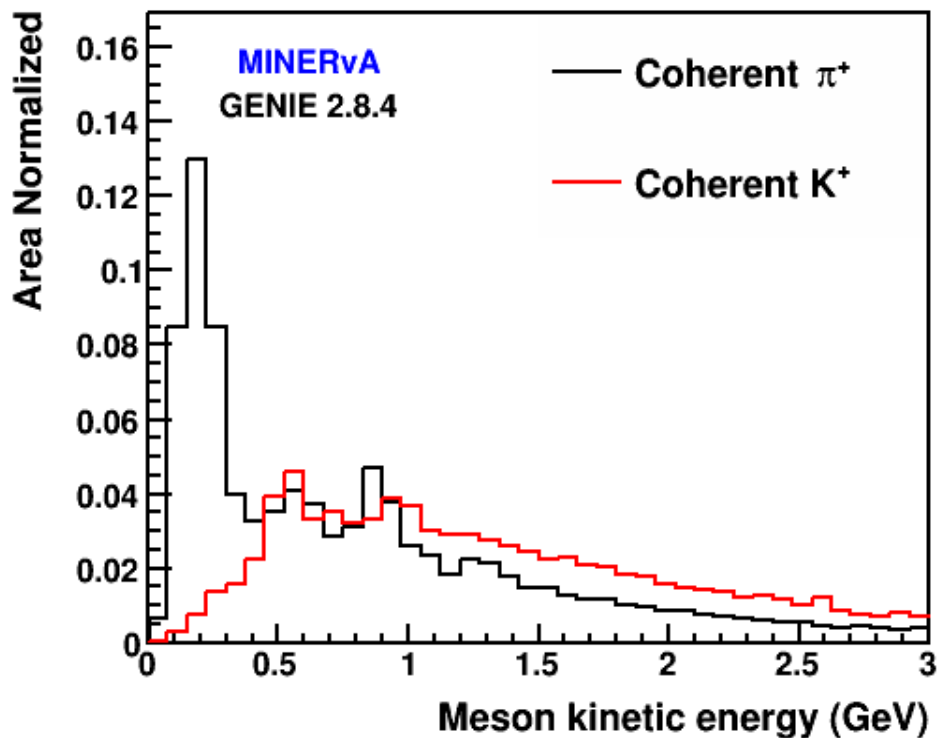
Signal and background templates



Use fits to the signal and background MC to perform an unbinned likelihood fit on the data

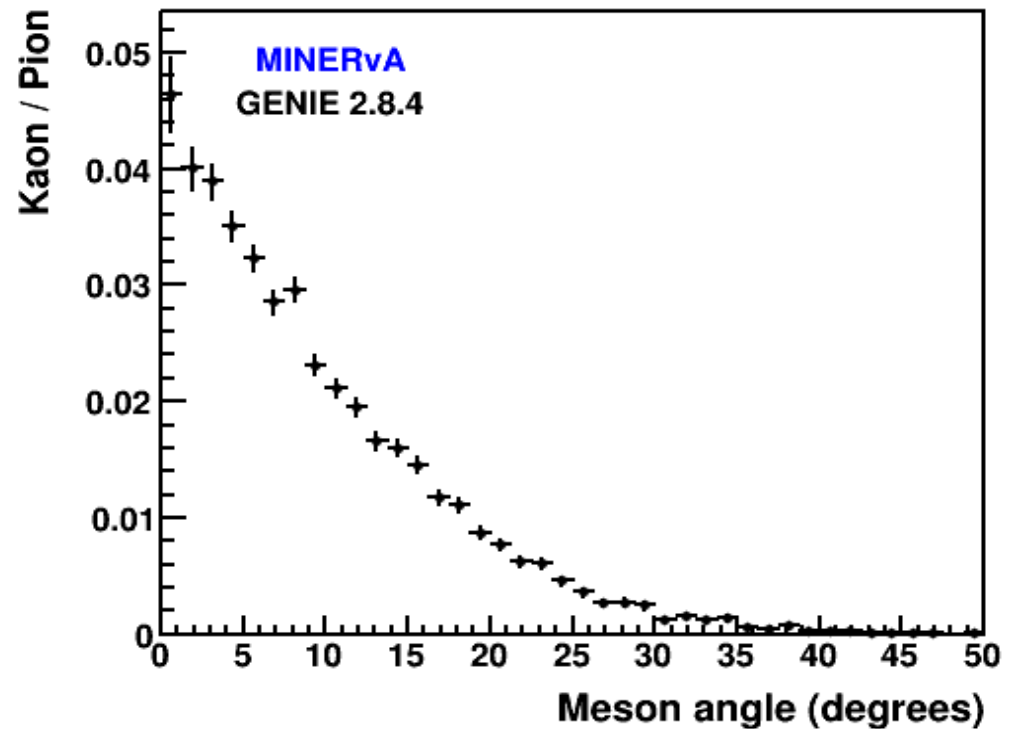
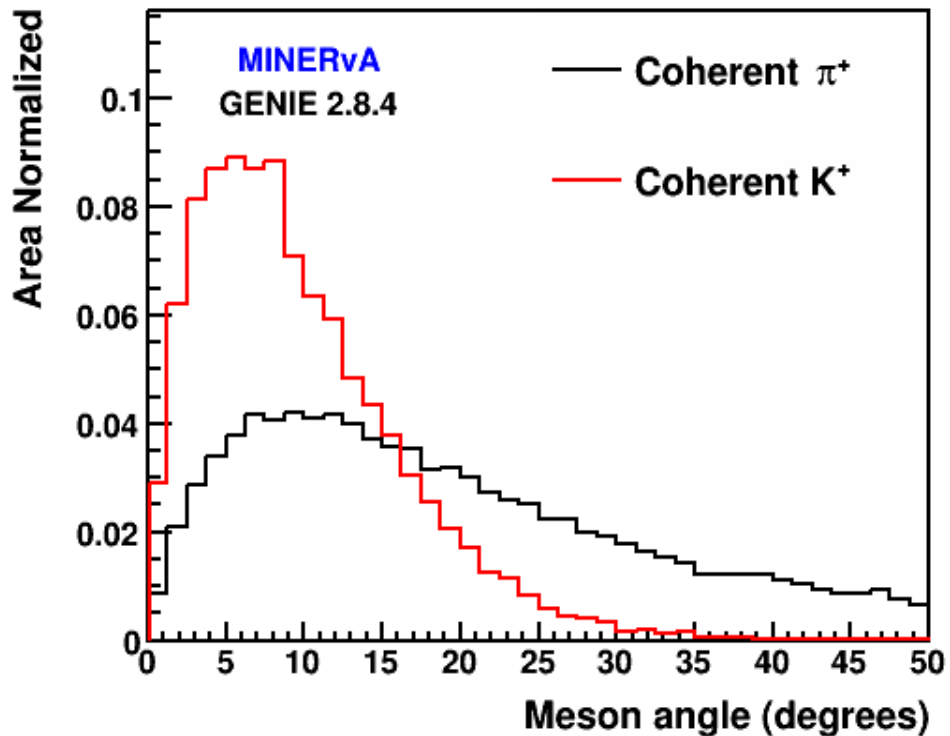
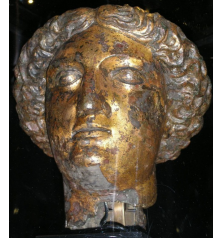


Coherent signal model: KE



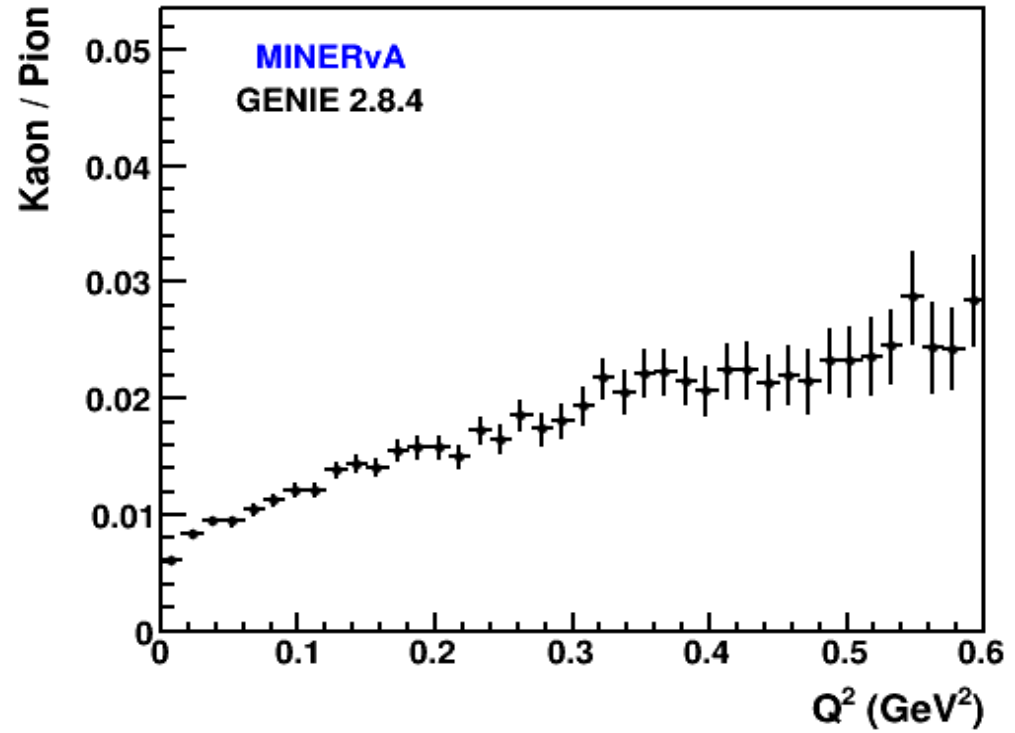
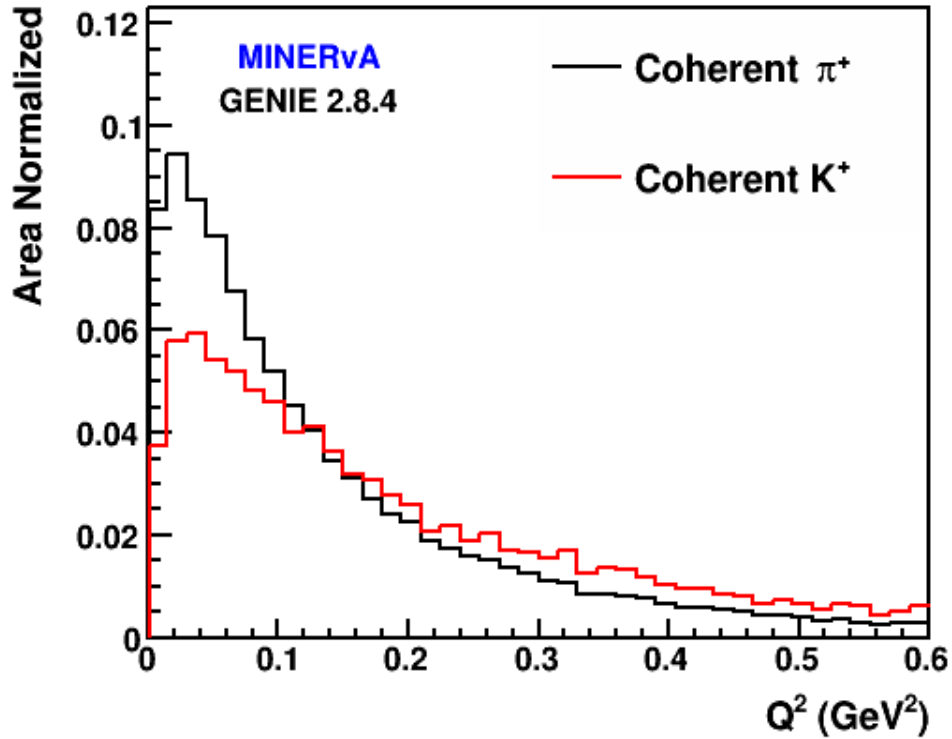
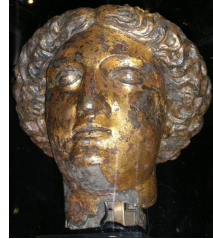


Coherent signal model: theta



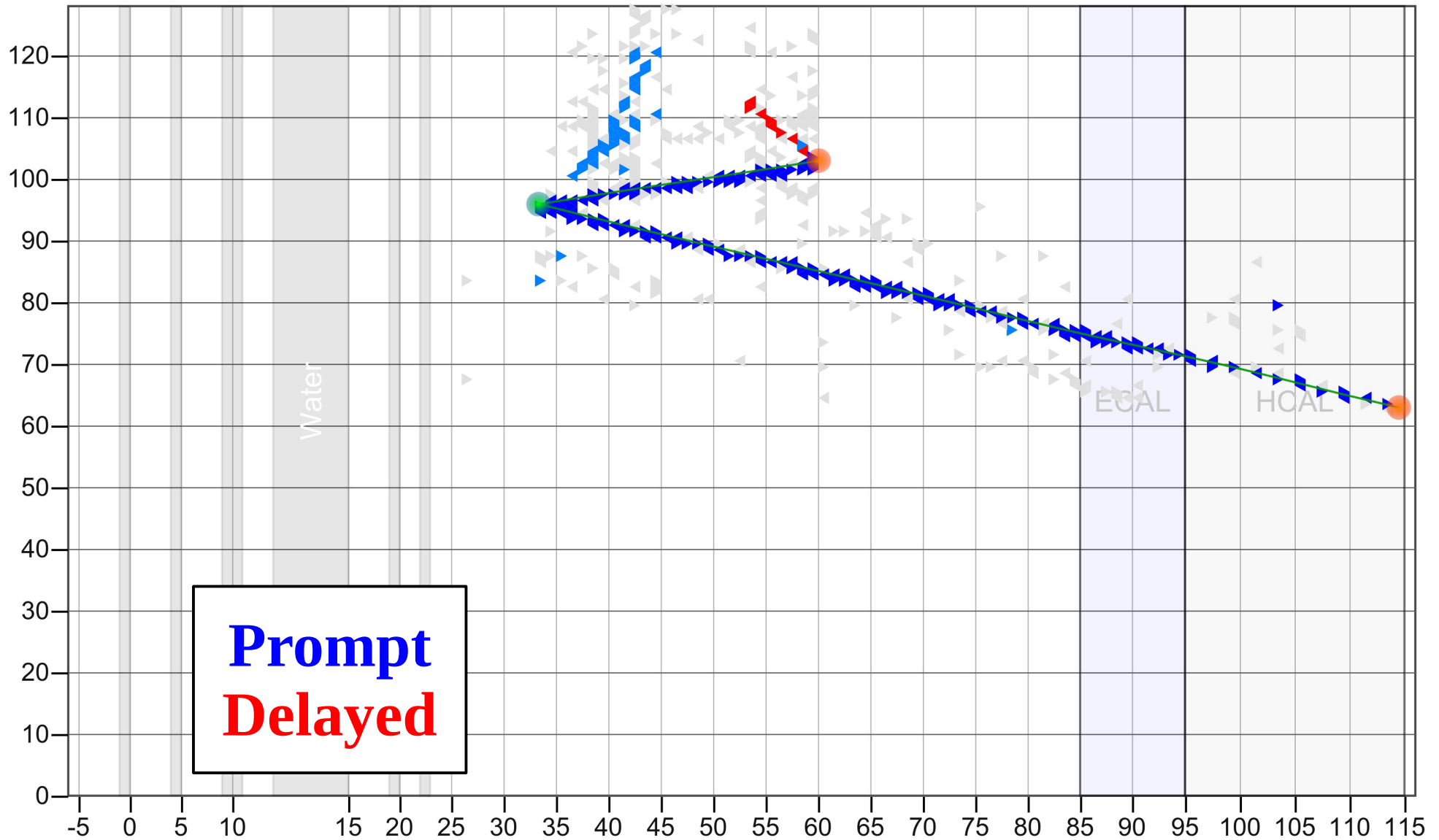
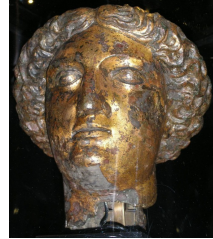


Coherent signal model: Q^2



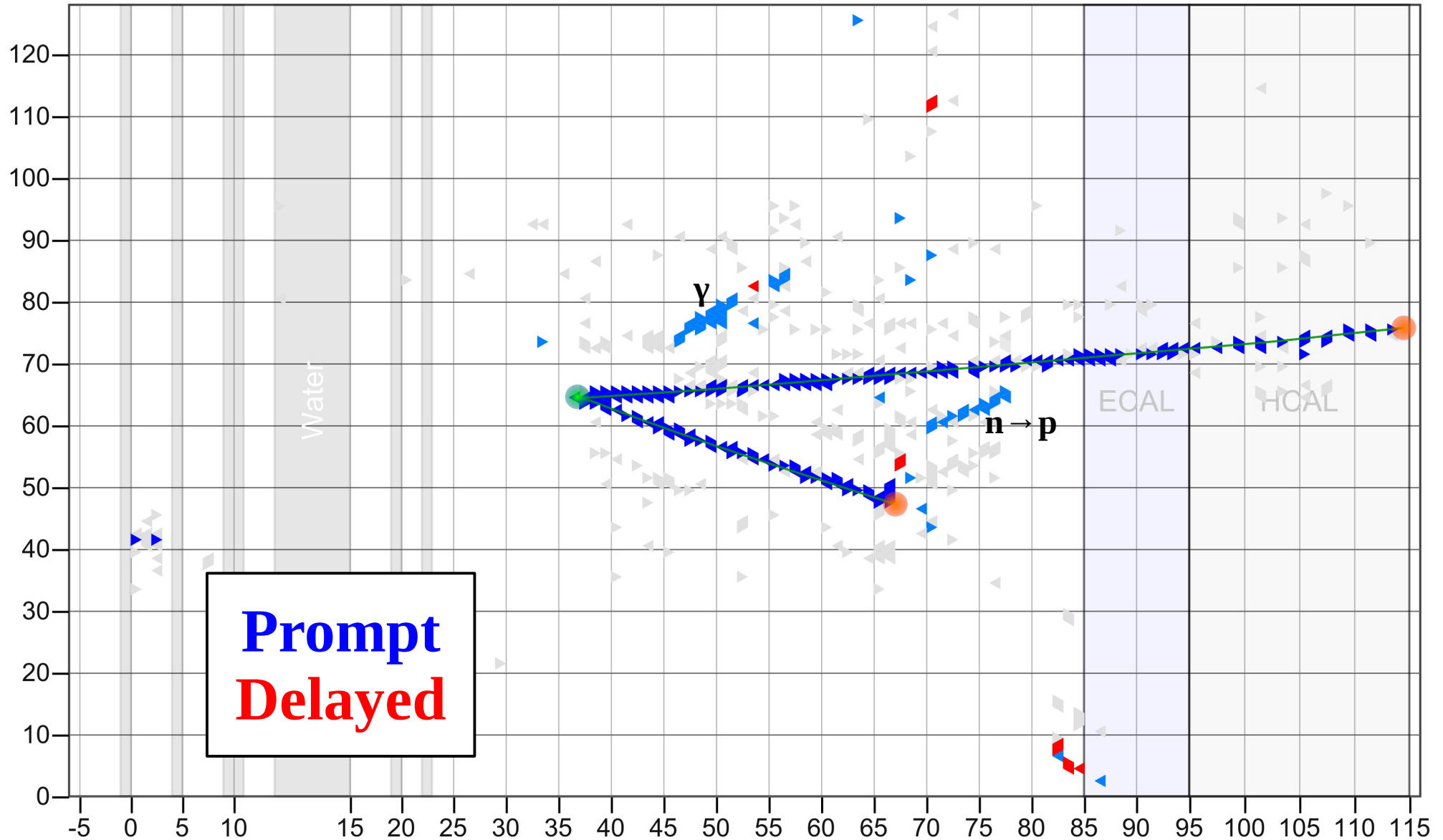


π^0 scan: reject #1



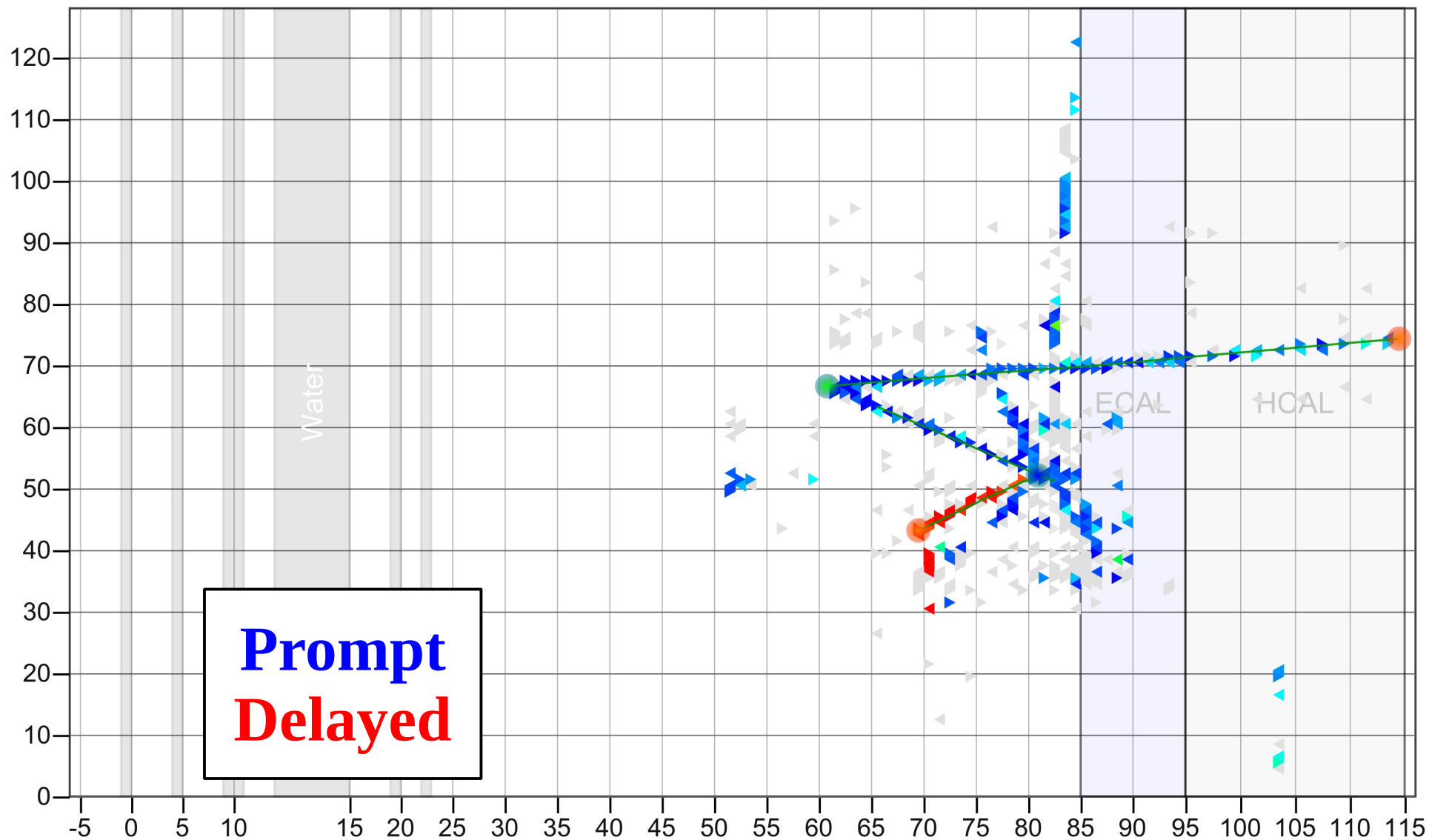


π^0 scan: reject #2



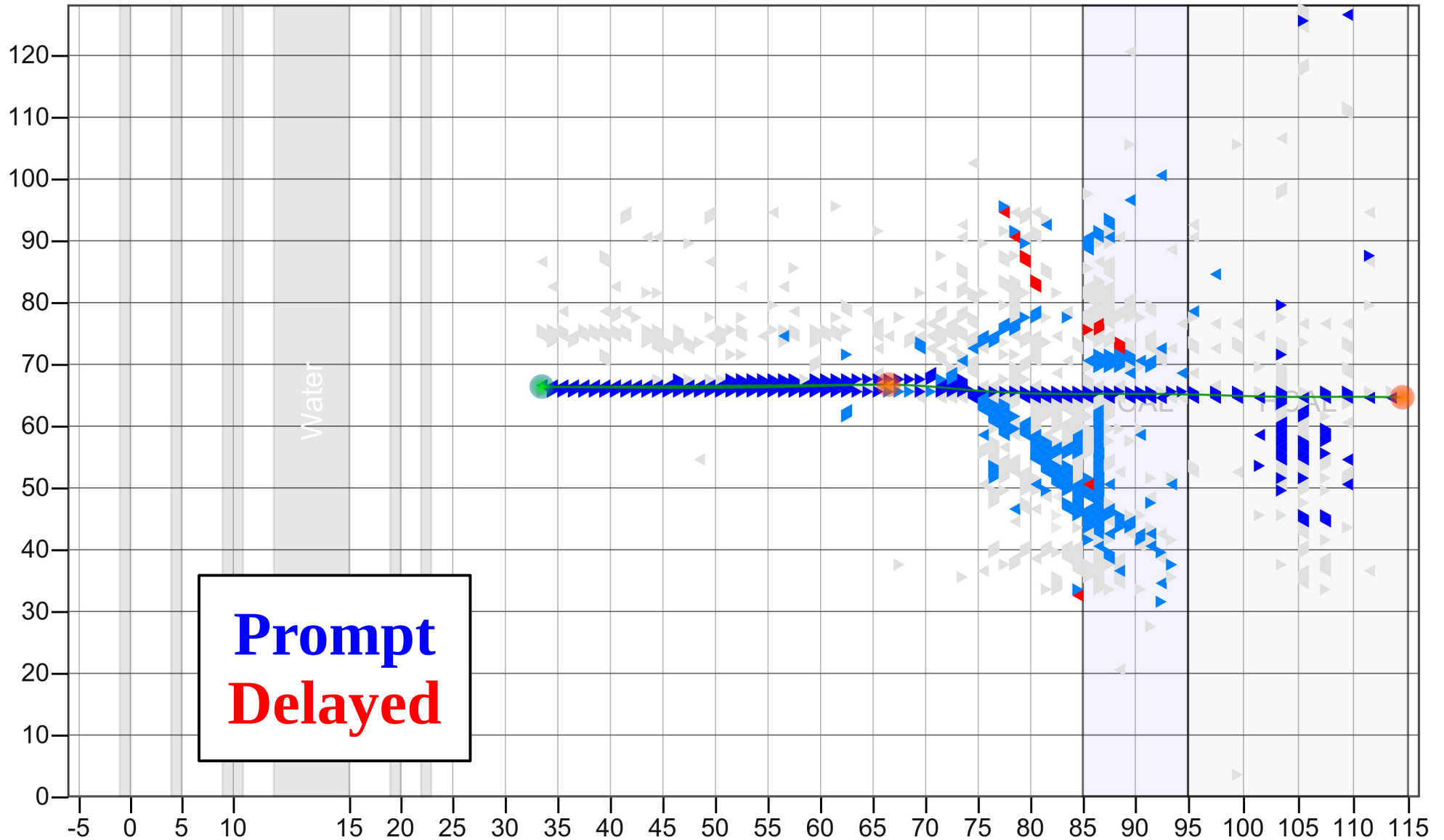


π^0 scan: keeper #1



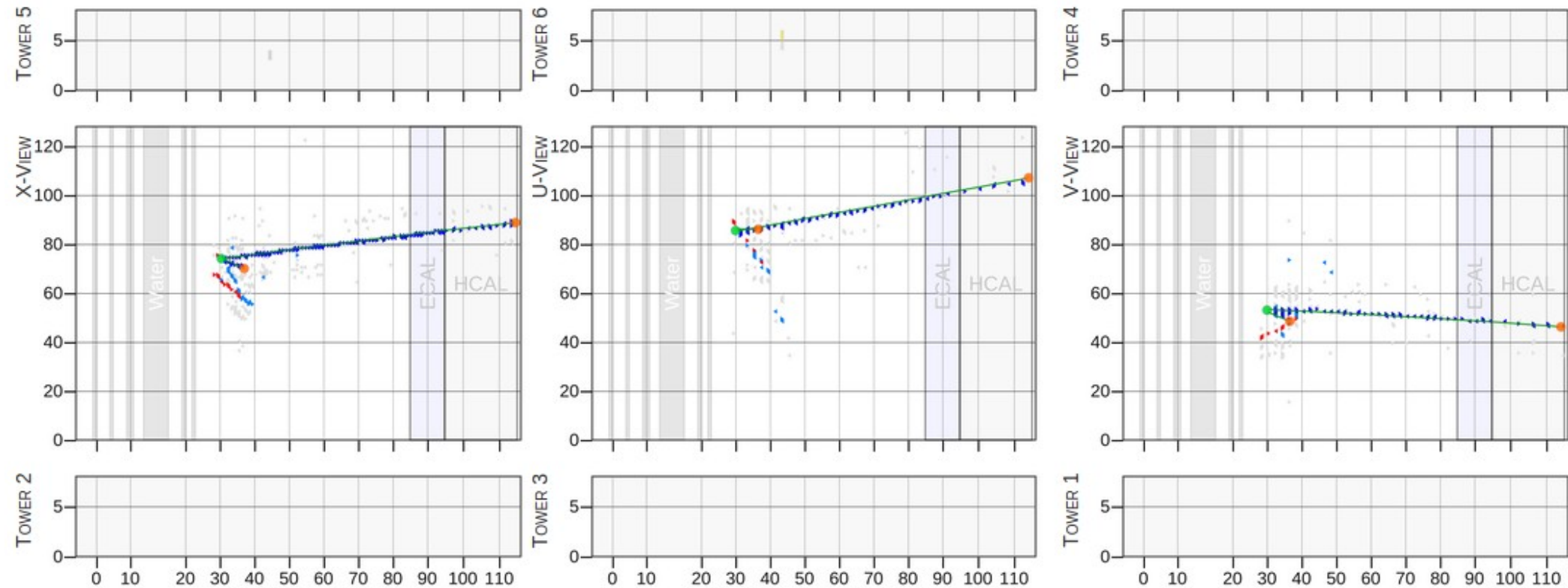
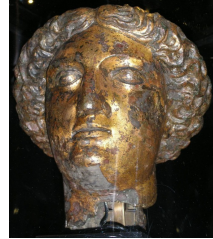


π^0 scan: keeper #2



Prompt
Delayed

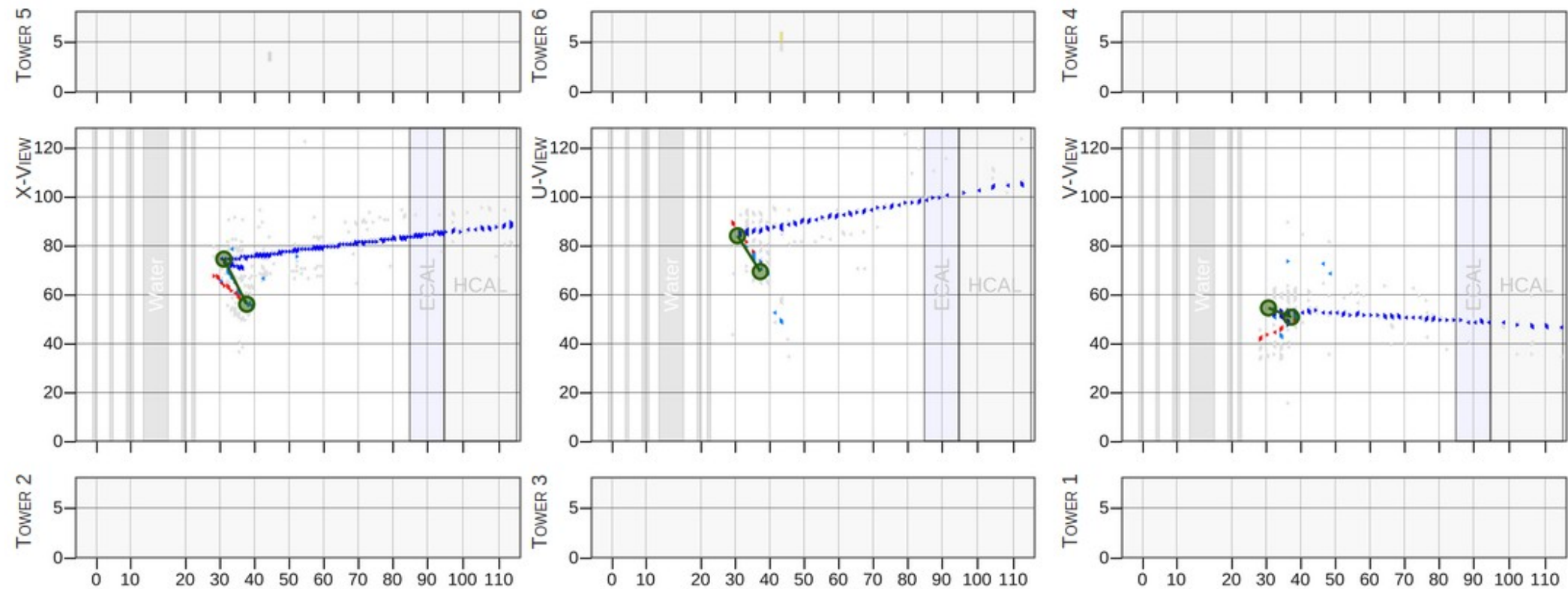
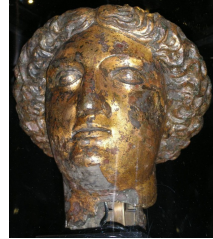
Including low-energy kaons



$\mu^- K^+ \Lambda$ final state, π^- from Λ decay is tracked, but K^+ is not



Scan for the range



In U view, decay μ^+ overlaps the vertex, but a human with some training can make an excellent range measurement