Nuclear Processes and Backgrounds



Kate Scholberg, Duke University EDIT School Fermilab, March 2018 This "nuclear processes and backgrounds" topic could mean a lot of things... I decided to pick a few relevant to some of my favorite physics topics

- Part I: Energy loss of particles in matter [generic material relevant for low-energy neutrino detection, but also many other situations
 - ... some you have seen]
- Part II: Examples of signal and background for low-energy neutrinos in underground detectors
 - scintillator
 - water Cherenkov
 - liquid argon

"Nuclear Processes"

Could refer to almost anything involving nuclei...

Radioactive decay



These could be your signal, or your background (or your calibration), possibly all in the same detector, depending on what you are trying to do...

References:

W.R. Leo Techniques for Nuclear and Particle Physics Experiments A How-to Approach

Second Revised Edition



Essential for experimentalists!

2 32. Passage of particles through matter

32. PASSAGE OF PARTICLES THROUGH MATTER

Revised September 2013 by H. Bichsel (University of Washington), D.E. Groom (LBNL), and S.R. Klein (LBNL).

This review covers the interactions of photons and electrically charged particles in matter, concentrating on energies of interest for high-energy physics and astrophysics and processes of interest for particle detectors (ionization, Cherenkov radiation, transition radiation). Much of the focus is on particles heavier than electrons (π^{\pm} , p, etc.). Although the charge number z of the projectile is included in the equations, only z = 1 is discussed in detail. Muon radiative losses are discussed, as are photon/electron interactions at high to ultrahigh energies. Neutrons are not discussed. The notation and important numerical values are shown in Table 32.1.

PDG review (points to online databases)

Part I: Energy loss of particles in matter

Particles lose energy by interactions with atoms as they move through matter (and may also decay into other particles, or create new particles)

particles deposit energy and change direction



	Inelastic collisions w/ atomic electrons	
Common energy-loss processes	Soft (excitations)	Hard (ionization, secondaries)
	Elastic scattering from nuclei	
	Cherenkov radiation	
Rare energy loss processes (but still potentially important)	Nuclear reactions	
	Bremsstrahlung	

First: "Heavy" (heavier than e[±]) charged particles μ^{\pm} , π^{\pm} , K^{\pm} , p, α , ...

In "normal" cases, most energy loss is from **inelastic collisions**,

e.g., ionization of atoms



"stopping power"

 $\frac{dE}{dx}$

as a function of projectile, material, energy, ... in basic approximation can be calculated w/ classical E&M (Jackson)

behaves statistically, but there are many collisions, so fluctuations are typically small

The QM calc for relativistic particles: "Bethe" or "Bethe-Bloch" equation

Mean rate of energy loss

$$\left\langle -\frac{dE}{dx}\right\rangle = Kz^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2}\ln\frac{2m_e c^2 \beta^2 \gamma^2 W_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2}\right] \rho$$

Symbol	Definition	Value or (usual) units
α	fine structure constant	
	$e^2/4\pi\epsilon_0\hbar c$	1/137.035999074(44)
M	incident particle mass	MeV/c^2
E	incident part. energy γMc^2	MeV
T	kinetic energy, $(\gamma - 1)Mc^2$	MeV
W	energy transfer to an electron	MeV
	in a single collision	
$_{k}$	bremsstrahlung photon energy	MeV
$m_e c^2$	electron mass $\times c^2$	0.510 998 928(11) MeV
r_e	classical electron radius	
	$e^2/4\pi\epsilon_0 m_e c^2$	2.817 940 3267(27) fm
N_A	Avogadro's number	$6.02214129(27) \times 10^{23} \text{ mol}^{-1}$
\boldsymbol{z}	charge number of incident parti	icle
Z	atomic number of absorber	
A	atomic mass of absorber	$\rm g\ mol^{-1}$
K	$4\pi N_A r_e^2 m_e c^2$	$0.307075 \ { m MeV} \ { m mol}^{-1} \ { m cm}^2$
Ι	mean excitation energy	eV (Nota bene!)
$\delta(\beta\gamma)$	density effect correction to ioniz	zation energy loss
$\hbar \omega_p$	plasma energy	$\sqrt{\rho \langle Z/A \rangle} \times 28.816 \text{ eV}$
	$\sqrt{4\pi N_e r_e^3} \ m_e c^2/lpha$	$ \rightarrow \rho \text{ in g cm}^{-3} $
N_e	electron density	(units of r_e) ⁻³
w_j	weight fraction of the j th eleme	ent in a compound or mixture
n_j	\propto number of $j{\rm th}$ kind of atoms	in a compound or mixture
X_0	radiation length	$\rm g~cm^{-2}$
E_c	critical energy for electrons	MeV
$E_{\mu c}$	critical energy for muons	GeV
E_s	scale energy $\sqrt{4\pi/\alpha} m_e c^2$	21.2052 MeV
R_M	Molière radius	$\rm g~cm^{-2}$

good to ~% in MeV-GeV range and intermediate Z materials

 $0.1 \lesssim \beta \gamma \lesssim 1000$

The QM calc: "Bethe" or "Bethe-Bloch" equation Mean rate of energy loss $\left\langle -\frac{dE}{dx}\right\rangle = Kz^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 W_{\text{max}}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right] \rho$ $\left\langle \frac{dE}{dx} \right\rangle \propto ho$, the material density

PDG expression for "stopping power" is really

$$\frac{1}{\rho} \left\langle \frac{dE}{dx} \right\rangle \quad \frac{\text{MeV cm}^2/\text{g}}{\text{MeV cm}^2/\text{g}}$$

I will drop the $\rho,$ but in practice you need to remember to multiply by it

A few features of the Bethe-Bloch equation:

Mean rate of energy loss

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R_M	Molière radius	g cm ⁻²		

$$W_{\rm max} = \frac{2m_e c^2 \,\beta^2 \gamma^2}{1 + 2\gamma m_e/M + (m_e/M)^2}$$

(basic kinematics)

Most quantities are basic physics constants, except:

- δ : "density correction" (~measured)
- I: mean excitation energy (measured)

What this function looks like:

usually drawn log-log



What this function looks like:

usually drawn log-log



What this function looks like:

usually drawn log-log



For different materials:



For different incident particles:



Terminology note:

minimum in similar place for given incident particle $\beta\gamma$

"mip": minimum ionizing particle

since relativistic rise is slow, can often estimate energy loss using mip assumption





\begin{aside}



\end{aside}

Be aware: Bethe-Bloch primarily valid for "intermediate" energies



This was for "heavy" particles (i.e., heavier than atomic electrons)

Electrons (and positrons) act differently...



In addition to collisional energy loss, they are easily deflected (accelerated) and they radiate photons (bremsstrahlung) prob $\propto \frac{1}{m^2}$ so brems from μ 's down by $m_e^2/m_\mu^2 = 0.511^2/106^2$ $\sim 4.5 \times 10^{-5}$



At a few tens of MeV (depends on medium) brem energy loss > ionization energy loss: crossover is called the **CRITICAL ENERGY** E_c



Bethe-Heitler approximation

 $E_c \approx \frac{1600m_ec^2}{Z}$

Material	Critical energy	
	[MeV]	
Pb	9.51	
Al	51.0	
Fe	27.4	
Cu	24.8	
Air (STP)	102	
Lucite	100	
Polystyrene	109	
NaI	17.4	
Anthracene	105	
H ₂ O	92	

Another commonly used quantity to characterize radiation of electrons/positrons: **RADIATION LENGTH**, L_{rad}

In the high-energy limit where radiation loss dominates

 $E = E_0 \exp\left(\frac{-x}{L_{\rm rad}}\right)$

Material	[gm/cm ²]	[cm]
Air	36.20	30050
H ₂ O	36.08	36.1
NaI	9.49	2.59
Polystyrene	43.80	42.9
Pb	6.37	0.56
Cu	12.86	1.43
Al	24.01	8.9
Fe	13.84	1.76
BGO	7.98	1.12
BaF ₂	9.91	2.05
Scint.	43.8	42.4

Shorthand thinking: L_{rad} is thickness for which you can expect to get an **electromagnetic shower** (more on this coming shortly)

Energy loss of photons in matter

In our context, this mostly means **x-rays and gamma rays**



photons have no electric charge...
→no Coulomb-induced collisions

4 electromagnetic energy loss mechanisms:

- photoelectric effect
- Compton scattering
- pair production
- (photonuclear effect)

(Rayleigh scattering: scattering off whole atoms; small at energies of interest here) most of these destroy the photons rather than change the energy (attenuation)







Cross section calculated with Klein-Nishina formula (QED)

Compton recoil energy distribution





Electromagnetic showers



An avalanche! Can start with either a photon or e[±]

electron brems $\rightarrow \gamma$ pair-produces $\rightarrow e^{\pm}$ brem ... until energies drop below pair-production threshold and/or E_c for electrons

Neutron energy loss

[later talk by Jeph Wang]

Neutrons interact via the strong force short range force, so rare interactions ... neutrons are penetrating, and will tend to ping around



Mechanism	Reaction	Notes
Elastic scattering from nuclei	A(n,n)A	Main mechanism of energy loss
Inelastic scattering	A(n,n')A [*] , A(n,2n')B,	Deexcitation products or other secondaries
Radiative neutron capture	n+(Z,A) → γ + (Z,A+1)	~ 1/v, so requires low energy
Other nuclear reactions	(n,p), (n, d), (n, α), etc.	Low energies required
Fission		Low energies required
Hadronic showers		High energy (>100 MeV)

There are specialized codes for simulating neutrons (e.g., MCNPX, FLUKA... G4 has a bad rep, but is fine for many applications)

Neutron moderation and capture

Common for low-energy neutrino experiments, e.g. neutron from inverse beta decay

$$\bar{\nu}_e + p \to e^+ + n$$

The neutron must thermalize (E~kT~1/40 eV) before capture ... "moderation" by multiple elastic scattering

 $n + p \rightarrow d + \gamma (2.2 \text{ MeV})$

Elastic kinematics:

$$\left(\frac{A-1}{A+1}\right)^2 E_0 < E < E_0$$

For small A, nucleus takes more energy away per scatter → moderators made out of light materials (hydrogen, carbon...)



Summary of energy loss topics

- charged particles
 - "heavy" (μ , π , p, ...): Bethe-Bloch (ionization)
 - e⁺, e⁻: collisions + radiation (know critical energy/radiation length)
- photons: **PE + Compton + pair production**
- neutrons: **elastic scattering** (+ radiative capture)

Part II:

Low energy neutrino detection: signals and backgrounds

Neutrinos in the few to few tens of MeV range



Example: neutrinos from core collapse

When a star's core collapses, ~99% of the gravitational binding energy of the proto-nstar goes into v's of *all flavors* with **~tens-of-MeV energies**

(Energy *can* escape via v's)

Mostly $v-\overline{v}$ pairs from proto-nstar cooling

Timescale: *prompt* after core collapse, overall Δt~10's of seconds





Information is in the *energy, flavor, time* structure of the supernova burst

Wishlist

Size	~kton detector mass per 100 events @ 10 kpc	
Low energy threshold	~Few MeV if possible	
Energy resolution	Resolve features in spectrum	
Angular resolution	Point to the supernova! (for directional interactions)	
Timing resolution	Follow the time evolution	
Low background	BG rate << rate in burst; underground location usually excellent; surface detectors conceivably sensitive	
Flavor sensitivity	Ability to tag flavor components	
High up-time and longevity	Can't miss a ~1/30 year spectacle!	

Note that many detectors have a "day job"...

Neutrino Interactions with Matter

Neutrinos are aloof but not *completely* unsociable



Produces lepton with flavor corresponding to neutrino flavor

(must have enough energy to make lepton)



Flavor-blind

Supernova-relevant neutrino interactions

	Electrons		
	Elastic scattering		
Charged	$\nu + e^- \to \nu + e^-$		
current	^[¬] _{ve} ·····►		
Neutral current	ve		
	Useful for pointing		

Supernova-relevant neutrino interactions

	Electrons	Protons	
	Elastic scattering	Inverse beta decav	
Charged	$\nu + e^- \to \nu + e^-$	$\bar{\nu}_e + p \to e^+ + n$	
current		γ e ⁺ γ	
		• * e	
	-	n	
	e⁻	Elastic	
Neutral	ν	p	
current		ν	
	Useful for pointing	very low energy recoils	
Supernova-relevant neutrino interactions

	Electrons	Protons	Nuclei
	Elastic scattering $\nu + e^- \rightarrow \nu + e^-$	Inverse beta decay $\bar{\nu}_e + p \rightarrow e^+ + n$	$ \nu_e + (N, Z) \to e^- + (N - 1, Z + 1) $ $ \bar{\nu}_e + (N, Z) \to e^+ + (N + 1, Z - 1) $
Charged current	^[−] _{ve} ·····• √ e [−]	γ e^+ γ $\overline{\nu}_e$ n	n ve e+/- Various possible
Neutral current	v€	Elastic scattering v	$\nu + A \rightarrow \nu + A^{*}$
	Useful for pointing	very low energy recoils	$ \nu + A \rightarrow \nu + A $ Coherent elastic (CEvNS)

Supernova-relevant neutrino interactions

	Electrons	Protons	Nuclei
	Elastic scattering $\nu + e^- \rightarrow \nu + e^-$	Inverse beta decay $\bar{\nu}_e + p \rightarrow e^+ + n$	$ \nu_e + (N, Z) \to e^- + (N - 1, Z + 1) $ $ \bar{\nu}_e + (N, Z) \to e^+ + (N + 1, Z - 1) $
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Neutral current	ve Vuseful for pointing	Elastic scattering p v very low energy recoils	$\nu + A \rightarrow \nu + A^{*}$ $\nu + A \rightarrow \nu + A$ $\nu + A \rightarrow \nu + A$

IBD (electron antineutrinos) dominates for current detectors

Neutrino interaction thresholds



Backgrounds

Same energy loss processes as the signal!

Radiologicals

- alpha, beta, gamma, fission
- intrinsic to your detector, or ambient

Cosmic rays and cosmogenics

- showers (neutrons) near the surface, penetrating muons underground
- spallation products, activation



(Sometimes you can use your backgrounds for calibration!)

Cosmic rays



Beams are usually **pulsed..** so you know when the v's arrive

Primary cosmic rays electromagnetic Mont Bland (4807 m)

"duty factor": pulse rate * pulse width (fraction of time beam is on = rejection factor for CR bg)

The weather is always fine underground

Overburden enables collection of neutrinos with no beam trigger: proton decay, atmospheric v's, astrophysical v's,... (and make beam neutrino samples cleaner too!)

Muons are the penetrating particles



mwe = "meters-water-equivalent" (scale by density)

Large (multi-kton) detector technologies for low energies

Water Cherenkov





Cheap material, proven at very large scale Liquid scintillator





Low threshold, good energy resolution

Liquid Argon





Good particle reconstruction

+ some other detector types for specific uses

GeV-scale events: handsome and distinctive







MeV-scale events: crummy little stubs







hungry for visible dE/dx!

Scintillation detectors



Liquid scintillator (C_nH_{2n}) volume surrounded by photomultipliers

- lots of photons: few 100 pe/MeV
 →low threshold (<1 MeV), good energy resolution (3-8%/√E)
- little pointing capability

 (light is ~isotropic
 even if interaction were
 directional...)
- can also dope with Gd





First neutrinos ever detected were from a nuclear reactor; Reines & Cowan, 1956

10 µsec

Large Underground Scintillation Detectors



Liquid hydrocarbon (C_nH_{2n}) that emits (lots of) photons when charged particles lose energy in it

Will see supernova electron antineutrinos, with good energy resolution

$$\bar{\nu}_e + p \to e^+ + n$$

Many examples worldwide of current and future detectors













Example: Borexino Experiment

Gran Sasso, Italy



Go after recoil electrons from the ⁷Be line





Heroic (and successful) struggle with radioactive (ambient & cosmogenic) backgrounds



Even more heroic extraction of pp rates:



its all about the backgrounds

Water Cherenkov Detectors

Charged particles produced in neutrino interactions emit Cherenkov radiation if β >1/n



- Low light yield, but directional signal is helpful for reconstruction
- Loss of heavy/low energy particles due to Cherenkov threshold
- Possible enhancement with Gd for inverse beta decay tagging (more later)

Photomultiplier tubes (PMTs) detect single photons





Fig. 7. Schematic view of a 50 cm PMT.

 Photons → photoelectrons
 → amplified PMT pulses
 → digitize charge, time
 → reconstruct vertex, energy, direction

Water Cherenkov detectors for supernova neutrinos





- See Cherenkov light from the positron (~positron is isotropic) Can't see 0.511 MeV γ 's (why not?)
- Limited by photocoverage (SK: $\sim 40\% \rightarrow \sim 6$ pe/MeV)

Neutron tagging in water Cherenkov detectors

$$\bar{\nu}_e + p \to e^+ + n \quad \blacksquare$$

- especially useful for DSNB (which has low signal/bg)
- also useful for disentangling flavor content of a burst (improves pointing, and physics extraction)

R. Tomas et al., PRD68 (2003) 093013 KS, J.Phys.Conf.Ser. 309 (2011) 012028; LBNE collab arXiv:1110.6249 R. Laha & J. Beacom, PRD89 (2014) 063007

"Drug-free" neutron tagging

$$n + p \rightarrow d + \gamma (2.2 \text{ MeV})$$

~200 μs thermalization & capture, observe Cherenkov radiation from γ Compton scatters

→ with SK-IV electronics,
 ~18% n tagging efficiency

SK collaboration, arXiv:1311.3738;



Enhanced performance by doping! (common strategy use gadolinium to capture neutrons for scintillator) J. Beacom & M. Vagins, PRL 93 (2004) 171101 Gd has a huge n capture cross-section: 49,000 barns, vs 0.3 b for free protons $n + Gd \rightarrow Gd^* \rightarrow Gd + \gamma$ $\sum E_{\gamma} = 8 MeV$ **Gd-loaded** water Number of Events H. Watanabe et al.. 35 Astropart. Phys. 31, $E = 4.3 \pm$ 320-328 (2009) 30 0.1 MeV Bar: Data 25 Hatched: MC 20 MeV cascade About 4 MeV 15 visible energy 10 per capture; 5 ~67% efficiency 0 2 3 4 5 6 8 Q in SK Energy [MeV] EGADS: test tank in the Kamioka mine for R&D Going forward as **"SK-Gd"**

Low-energy backgrounds in Super-K



- again, showing for solar sample



strongly threshold-dependent

3.49-3.99 MeV bin mostly radioactivity from wall

Liquid argon time projection chambers



fine-grained trackers sensitive to **electron neutrinos** (as opposed to antineutrinos)

 $\nu_e + {}^{40}\mathrm{Ar} \rightarrow e^- + {}^{40}\mathrm{K}^*$





MicroBooNE (USA) 0.2 kton





SBND

(USA)

0.112 kton



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Can we tag v_e CC interactions in argon using nuclear deexcitation γ 's?



20 MeV v_e , 14.1 MeV e⁻, simple model based on R. Raghavan, PRD 34 (1986) 2088 Improved modeling based on ⁴⁰Ti (⁴⁰K mirror) β decay measurements in progress **Direct measurements (and theory) needed!**

... in fact there can be transitions to intermediate states, adding to the cross section (and complicating the γ-tag)



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The final state can be complicated... some energy is lost



Modeling is improving, but still need nuclear theory help !

Radiologicals in DUNE



J. Reichenbacher, J. Stock





Summary of Part II

At low energy (<100 MeV):

- Still want energy (quantity/resolution), angular resolution
- Still want **flavor tagging**... but can only distinguish ν_e vs $\bar{\nu}_e$ vs ν_x
- Interactions w/ nuclei poorly understood; details of nuclear physics matter
- Background is critical must be deep & clean
 it's all about the backgrounds

Water: cheap, proven, directional, OK reconstruction, but low light yield, hard to go <few MeV, neutron tagging w/Gd

Scintillator: proven, non-directional, good light yield →energy resolution, low threshold, neutron tagging

LArTPC: good reconstruction, directional, still work to be done on tagging!





Extras/backups

Coherent elastic neutrino-nucleus scattering (CEvNS)

$$v + A \rightarrow v + A$$

A neutrino smacks a nucleus via exchange of a Z, and the nucleus recoils as a whole; **coherent** up to $E_v \sim 50$ MeV





Nucleon wavefunctions in the target nucleus are **in phase with each other** at low momentum transfer

For $QR \ll 1$, [total xscn] ~ A² * [single constituent xscn]

The only experimental signature of CEvNS:

tiny energy deposited by nuclear recoils in the target material



→ WIMP dark matter detectors developed over the last ~decade are sensitive to ~ keV to 10's of keV recoils

Now, *detecting* the tiny kick of the neutrino...

This is just like the tiny thump of a WIMP; we benefit from the last few decades of low-energy nuclear recoil detectors



"Quenching Factors" (QF)

Fraction of deposited energy that is detectable in a given channel; usually specified with respect to electron energy loss

Observable nuclear recoil energy loss tends to be **"quenched"** with respect to electron energy loss



Nuclear recoil energy: **keVr** "Electron-equivalent energy": **keVee**

"Quenching Factors" (QF)

Understanding of quenching factors is critical for interpretation of data... need to be measured target by target



G. Rich thesis
CsI quenching factor measurements w/ neutrons





And going even farther out: we are awash in a sea of '*relic'* or diffuse SN v's (DSNB), from ancient SNae ...



Energy (MeV)

In water: $\overline{v}_e + p \rightarrow e^+ + n$



LAr? Electron flavor, but low rate... bg unknown Scintillator? Good IBD tagging, but NC bg...



Particle ID using dE/dx



A common technique: if you know p and dE/dx, you can determine the particle type

This was mean energy loss... what about **distribution** of energy loss?

> Depends on thickness of absorber... no. of collision events N determines fluctuation behavior



"Thin" absorbers

Central limit theorem does not apply... single collisions can matter



$$\kappa = \bar{\Delta}/W_{\rm max}$$

determines the behavior; thin absorber corresponds to

 $\kappa < 10$

Landau distribution



 $\Delta_{\rm most\ probable} < \Delta$

Vavilov/Symon distributions are refinements to the Landau (function of κ)



What about very thick absorbers? ... complicated, particle slows down... → in practice, use a Monte Carlo code



- Geant4 is the standard open-source detector simulation code
- Can specify desired materials, geometry, incident particles, physics processes
- May need tweaks for specialized applications

Electromagnetic shower size estimate

(in radiation lengths)

- Start with energy E₀
- Photon will convert after ~1 radiation length
 → E₀/2 for each of e⁺, e⁻
- Divide energy per particle again by 2 after another radiation length
- After t radiation lengths,

$$N \sim 2^t$$
 so $E \sim E_0/2^t$ for each particle
 $E(t_{\max}) = E_0/2^{t_{\max}} = E_c$
 $\rightarrow I_{\max} = \frac{\ln(E_0/E_c)}{\ln 2}$

Hadronic showers also relevant for high energies (initiated by protons, neutrons,..)





