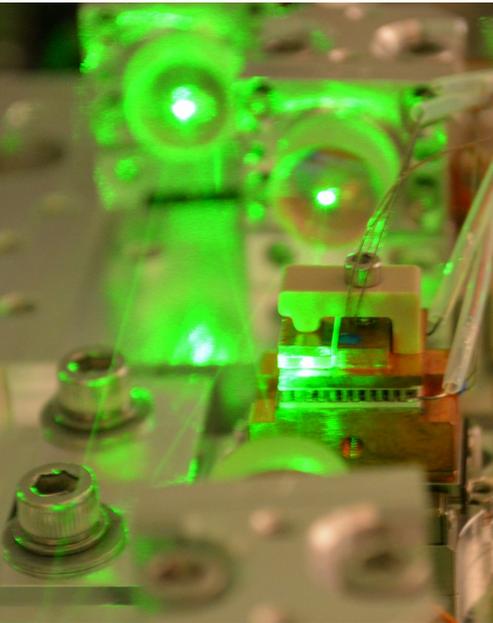




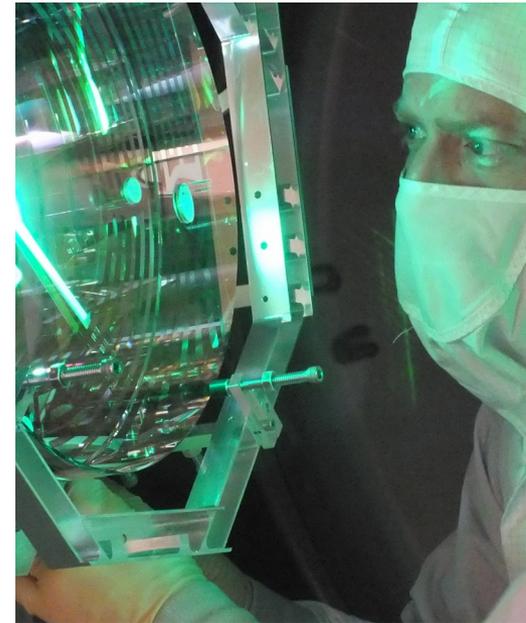
LIGO

Quantum Squeezing and Quantum Correlations in advanced LIGO



Lee McCuller, MIT
for the SQZ team
(LIGO Laboratory, in collaboration with ANU)

Fermilab Colloquium
17 Feb. 2020



LIGO's optical
Parametric amplifier

How strongly can we
probe the LIGO mirrors?

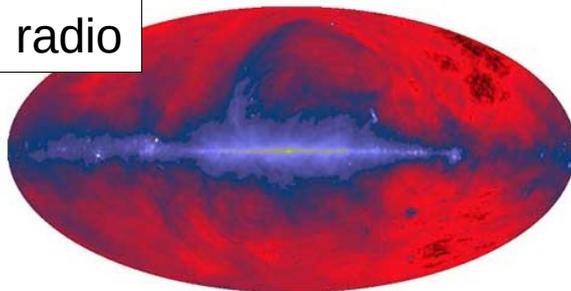
Every New *Wavelength*

In 1610, Galileo pointed a telescope to the sky, and changed the way we learn about our Universe

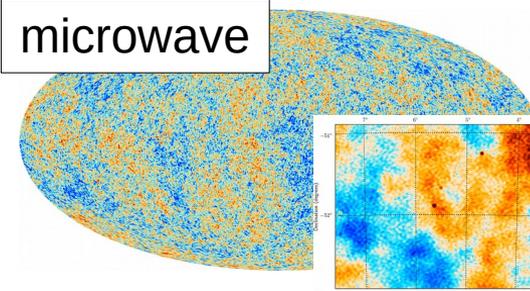
Since then, every new wavelength **discovers new objects, maps new populations, probes new physics**



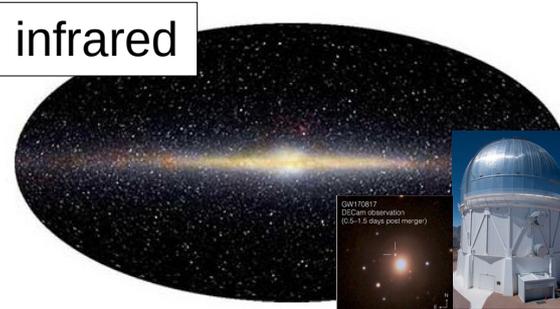
radio



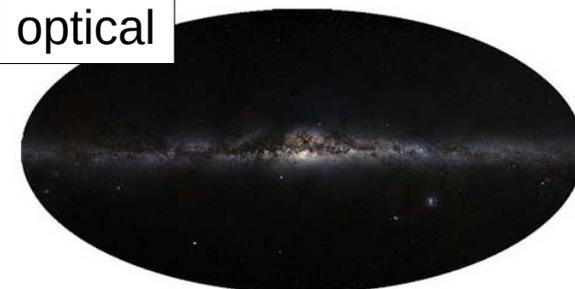
microwave



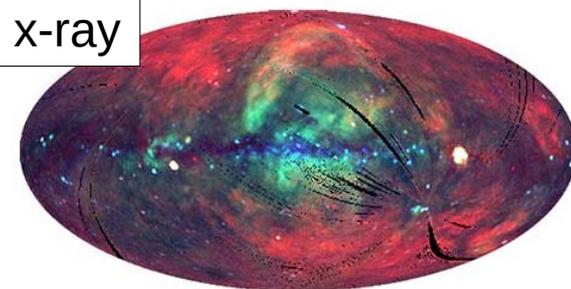
infrared



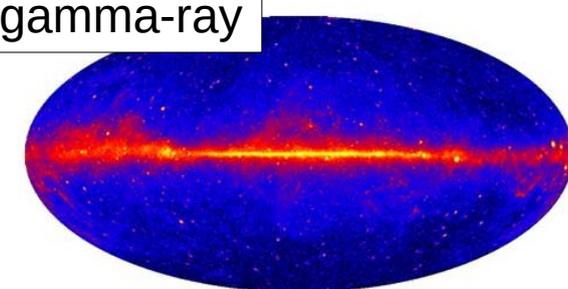
optical



x-ray

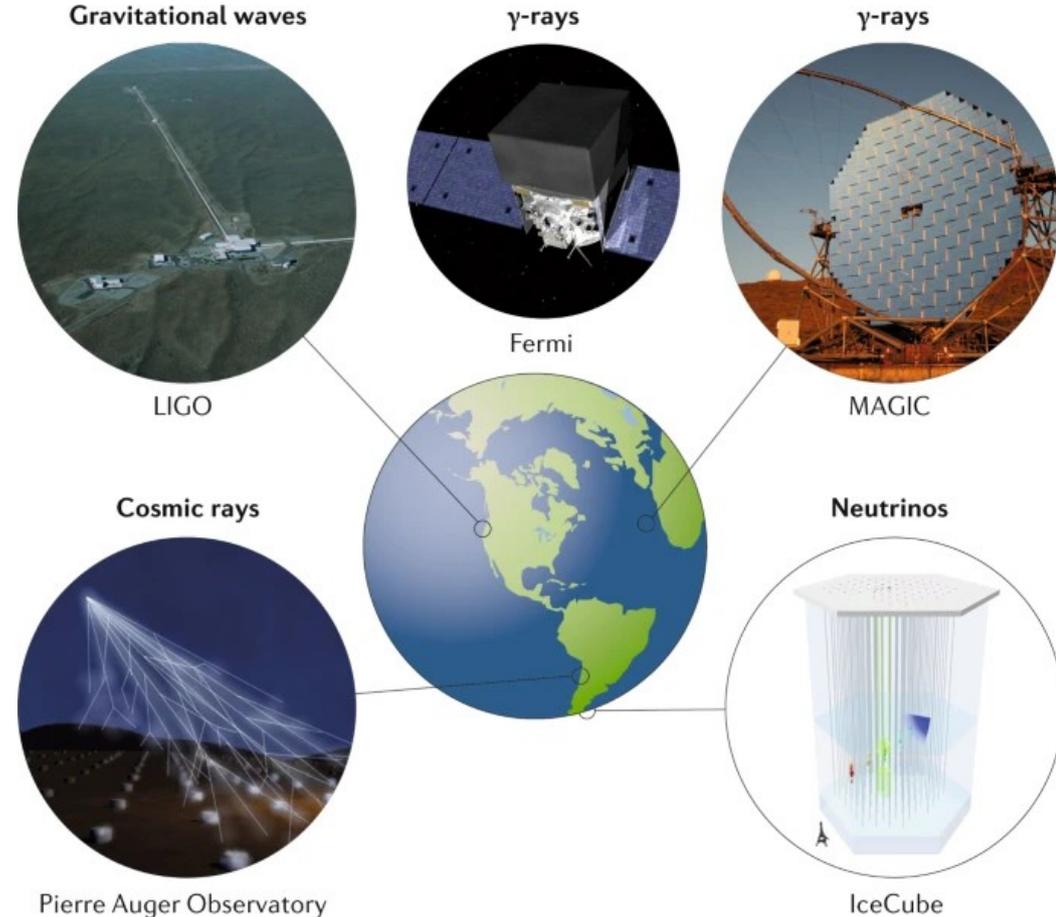


gamma-ray



Every new *Messenger*

- New *modalities* from astro-particle physics and gravitational waves
- Each modality observes in a new way, is a new *messenger*
- *Complementary observations* with electromagnetic imaging
- The dawn of multi-messenger astrophysics



Mészáros, P., Fox, D. B., Hanna, C. & Murase, K.
Multi-messenger astrophysics. *Nature Reviews Physics* 1, 585–599 (2019).

Gravitational Waves from the Cosmic Collider

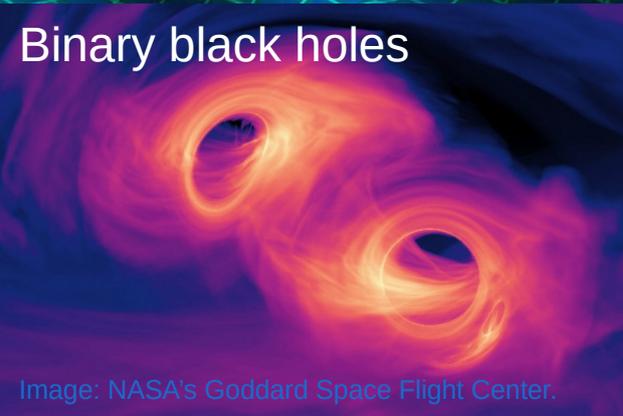
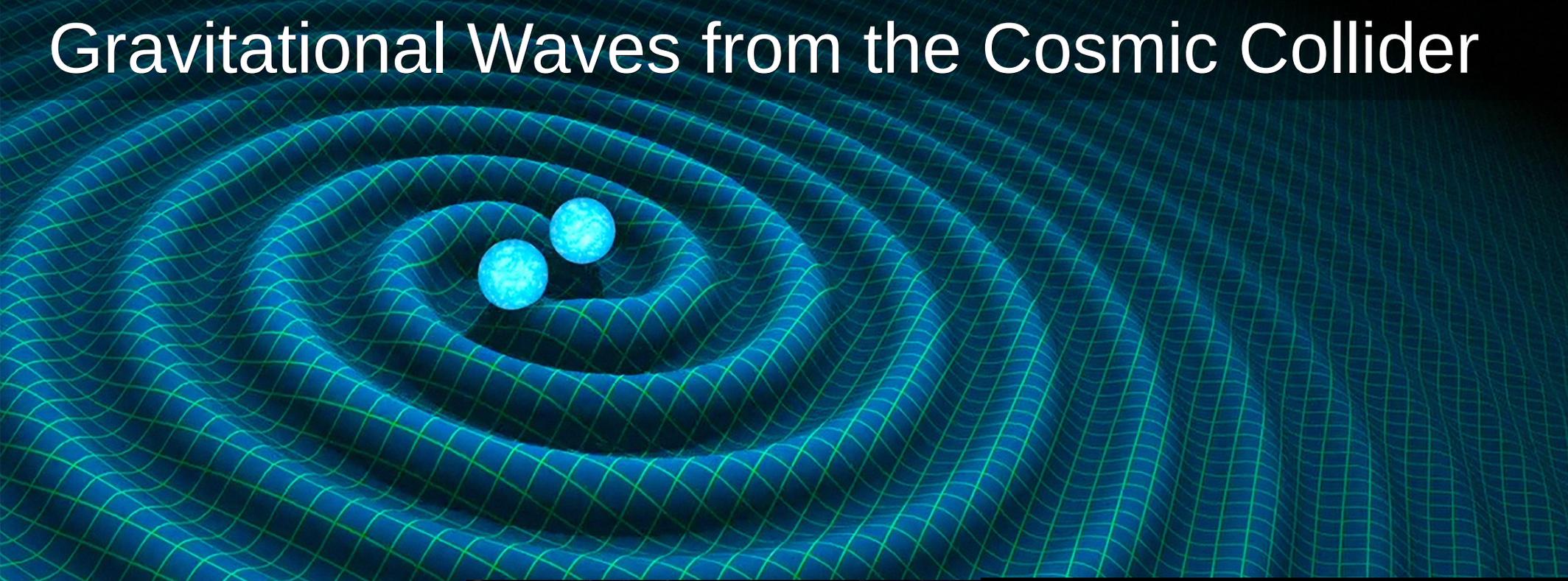


Image: NASA's Goddard Space Flight Center.

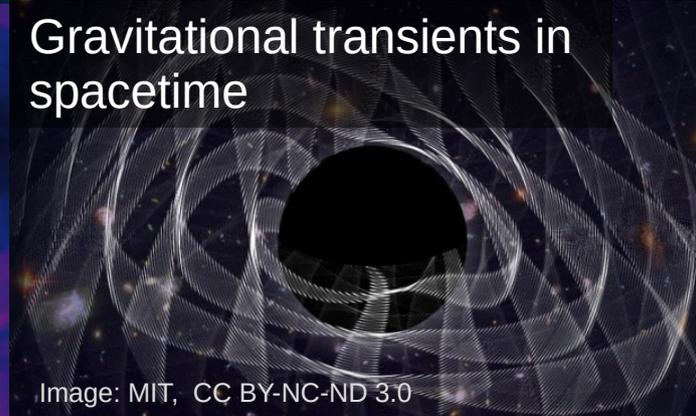


Image: MIT, CC BY-NC-ND 3.0

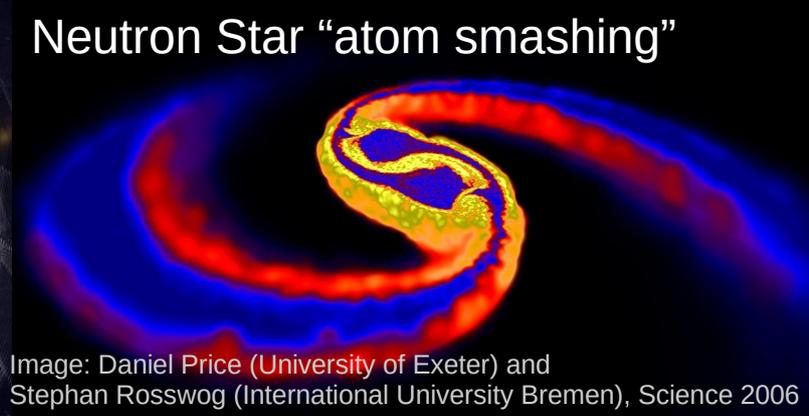
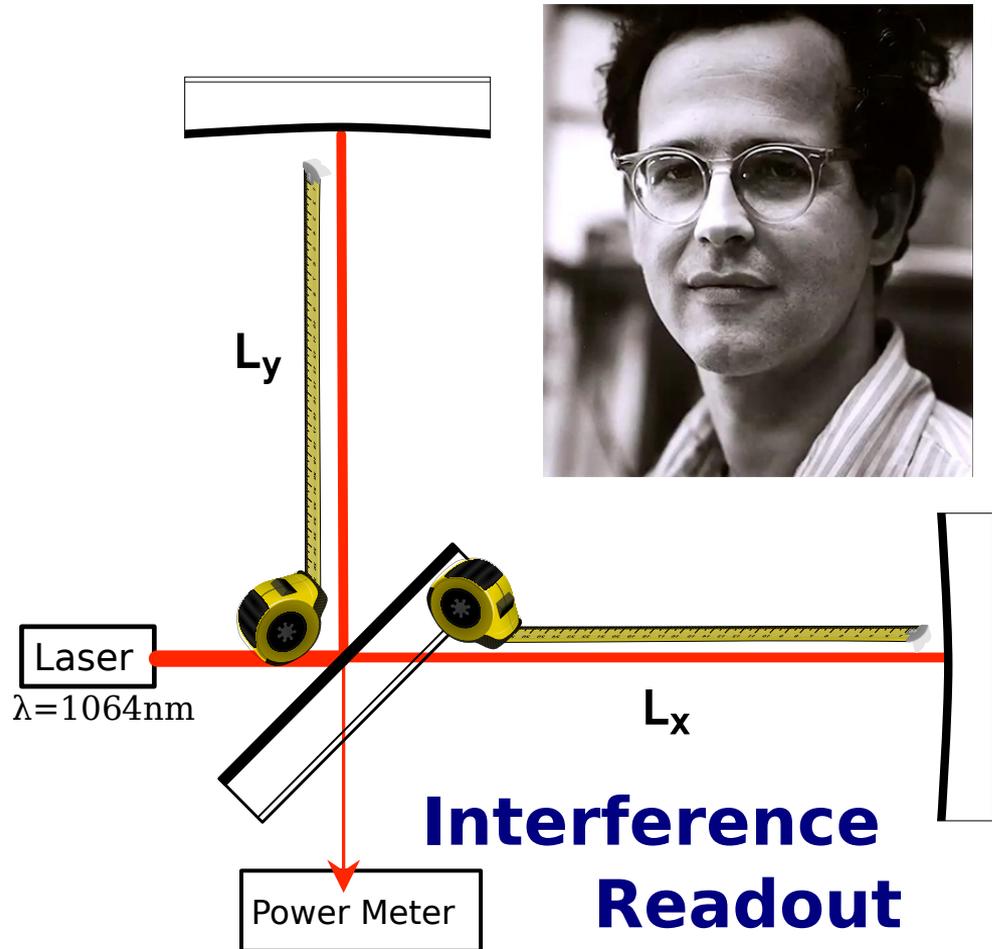


Image: Daniel Price (University of Exeter) and Stephan Rosswog (International University Bremen), Science 2006

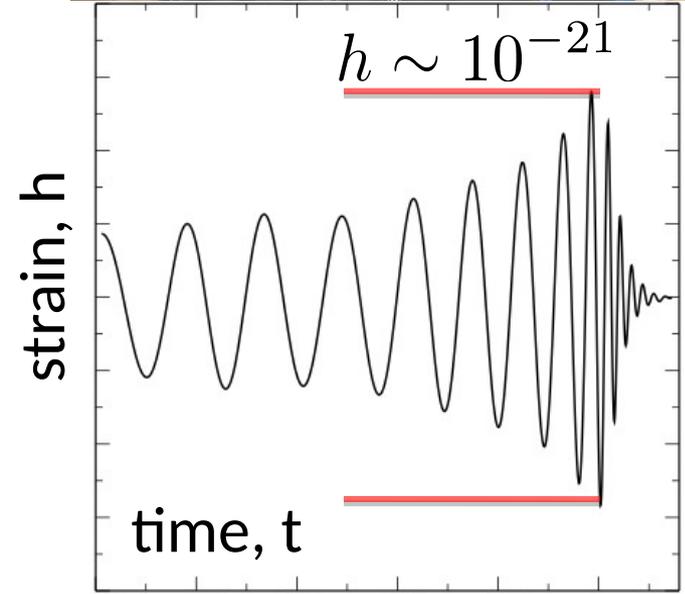
Gravitational Wave Detectives



Prof. Rainer Weiss
(MIT)



Prof. Kip Thorne
(Caltech)

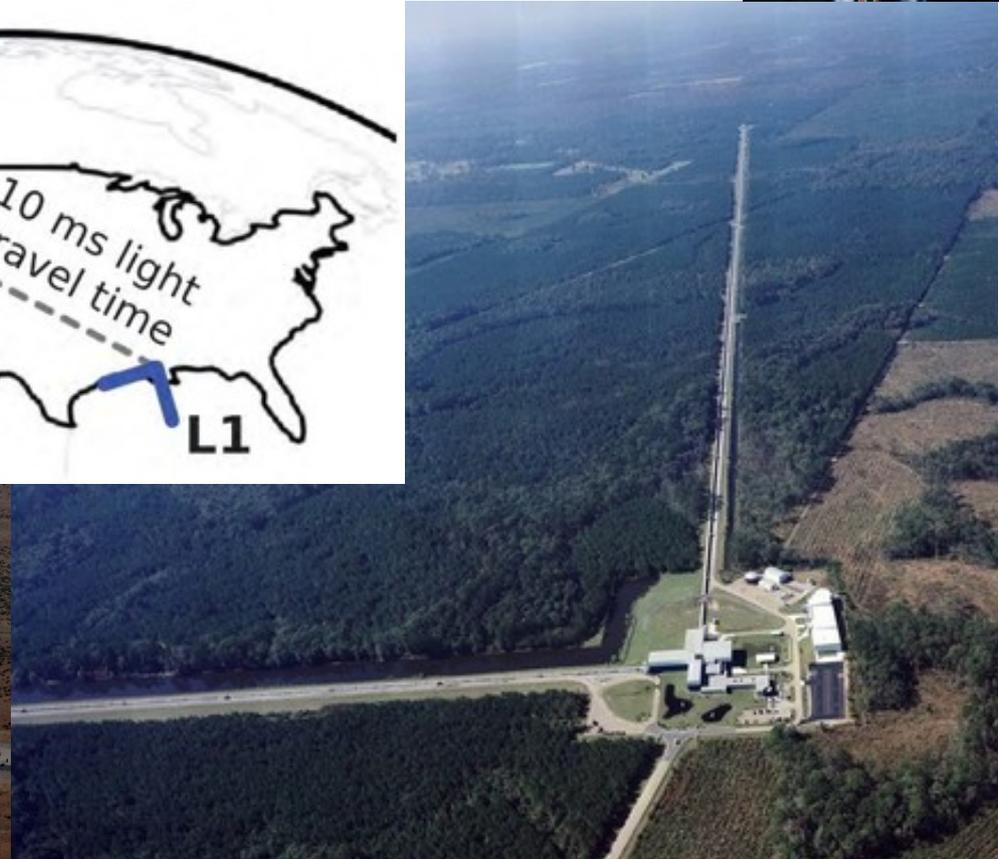
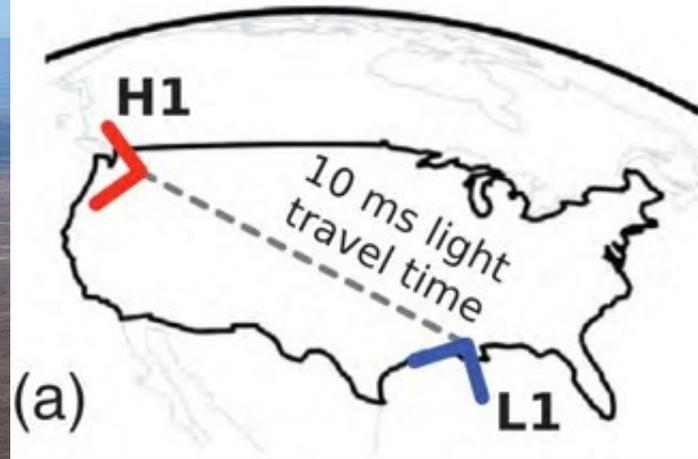
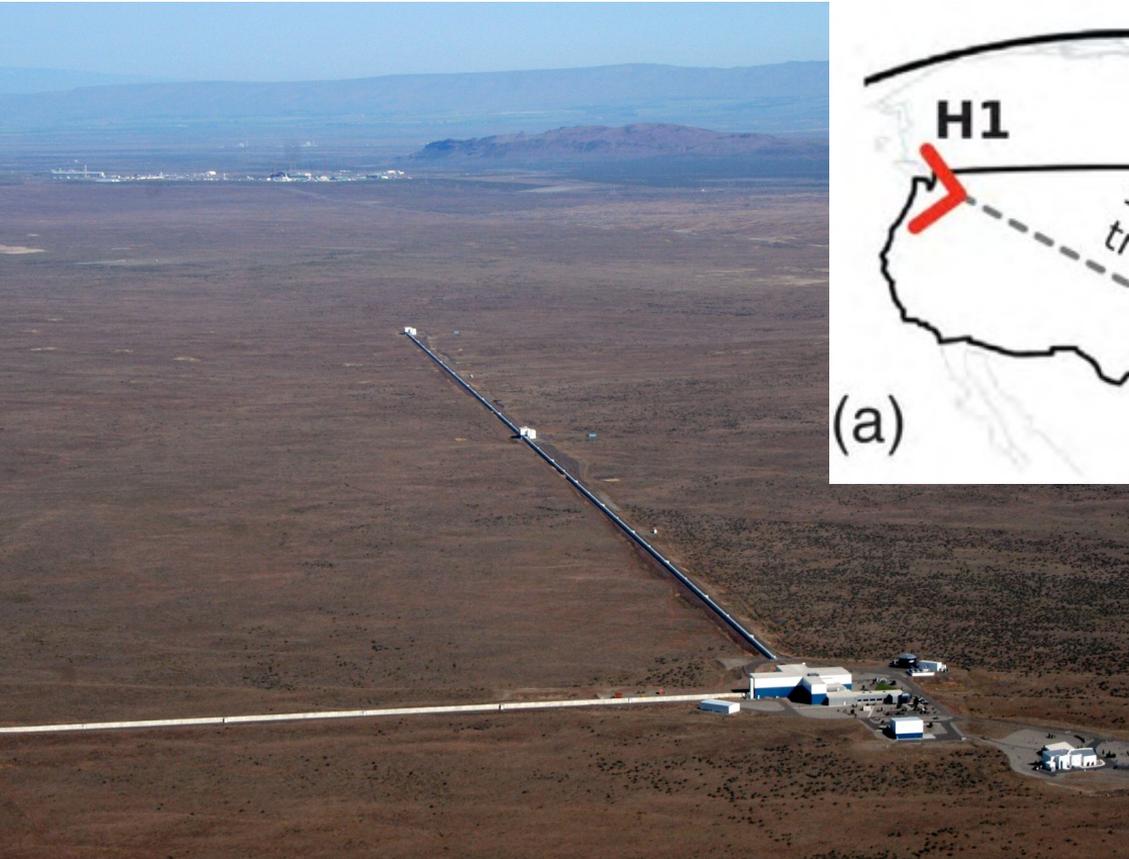
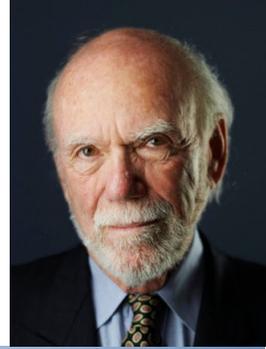


Two LIGO Observatories

each one a
laser interferometer with 4 km arms

Prof. Barry Barish (Caltech)

Image Credit: Nobel



Observatory Network



LIGO Hanford



GEO600



KAGRA



LIGO Livingston



VIRGO

LIGO India



Operational
Under Construction
Planned

Gravitational Wave Observatories

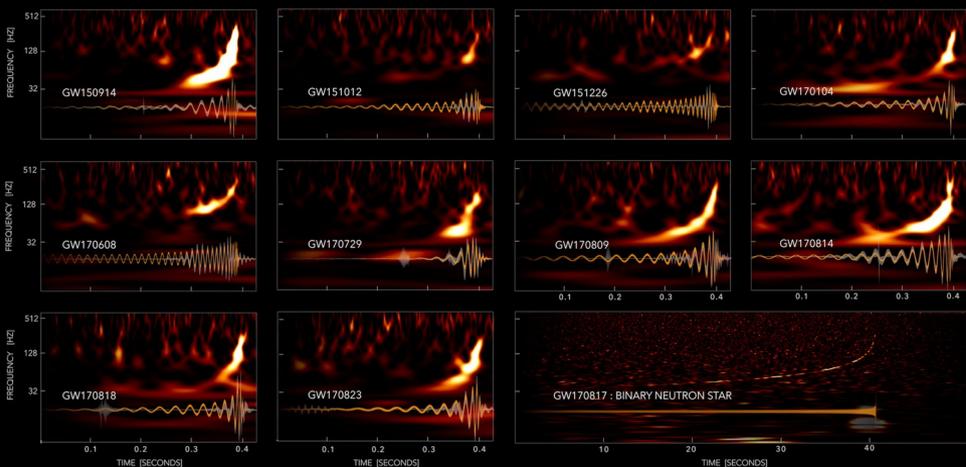
Detections, Physics, Astrophysics

The zoo or orrery exhibits a population.

The population is made of individuals.
each is exciting!

GRAVITATIONAL-WAVE TRANSIENT CATALOG-1

LIGO VIRGO Georgia Tech



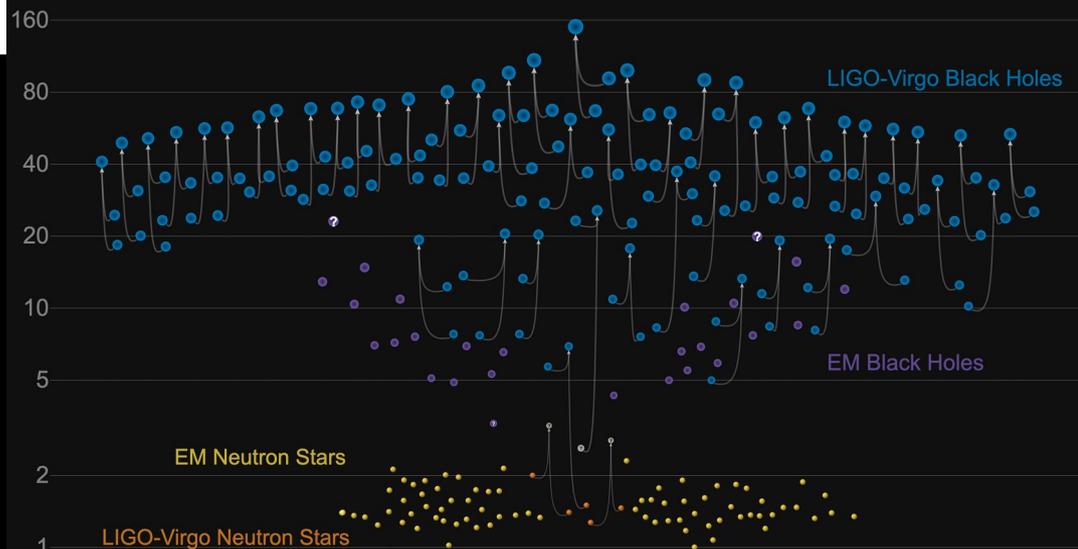
LIGO-VIRGO DATA: [HTTPS://DCC.LIGO.ORG/10.7935/82H3-H423](https://dcc.ligo.org/10.7935/82H3-H423)

WAVELET (UNMODELED) EINSTEIN'S THEORY

S. GHONGE, K. JANI | GEORGIA TECH

Observing Run 2 Catalog GWTC-1
Phys. Rev. X 9, 031040

Masses in the Stellar Graveyard *in Solar Masses*



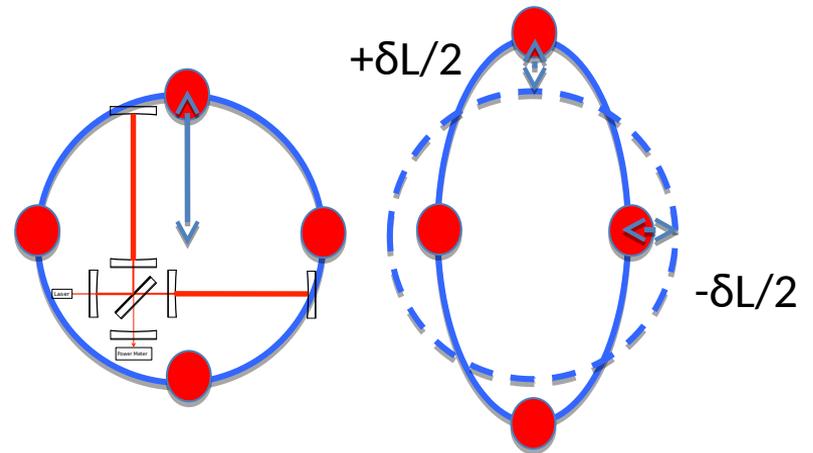
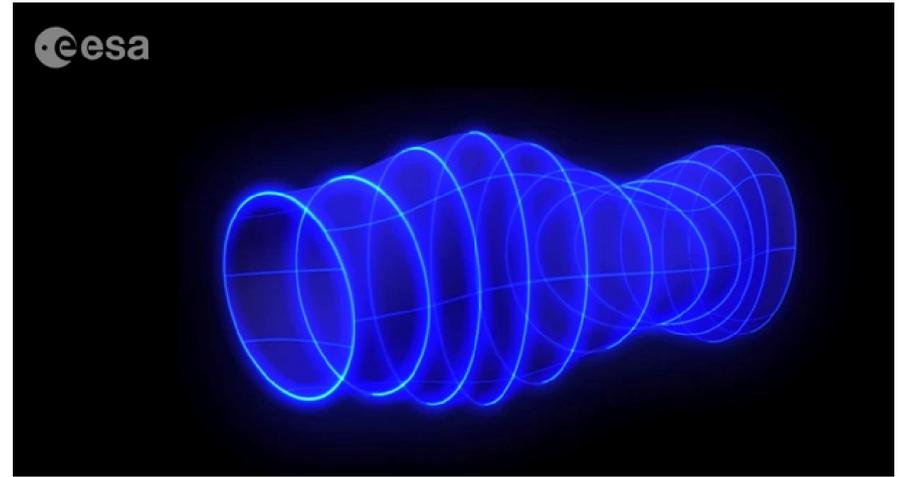
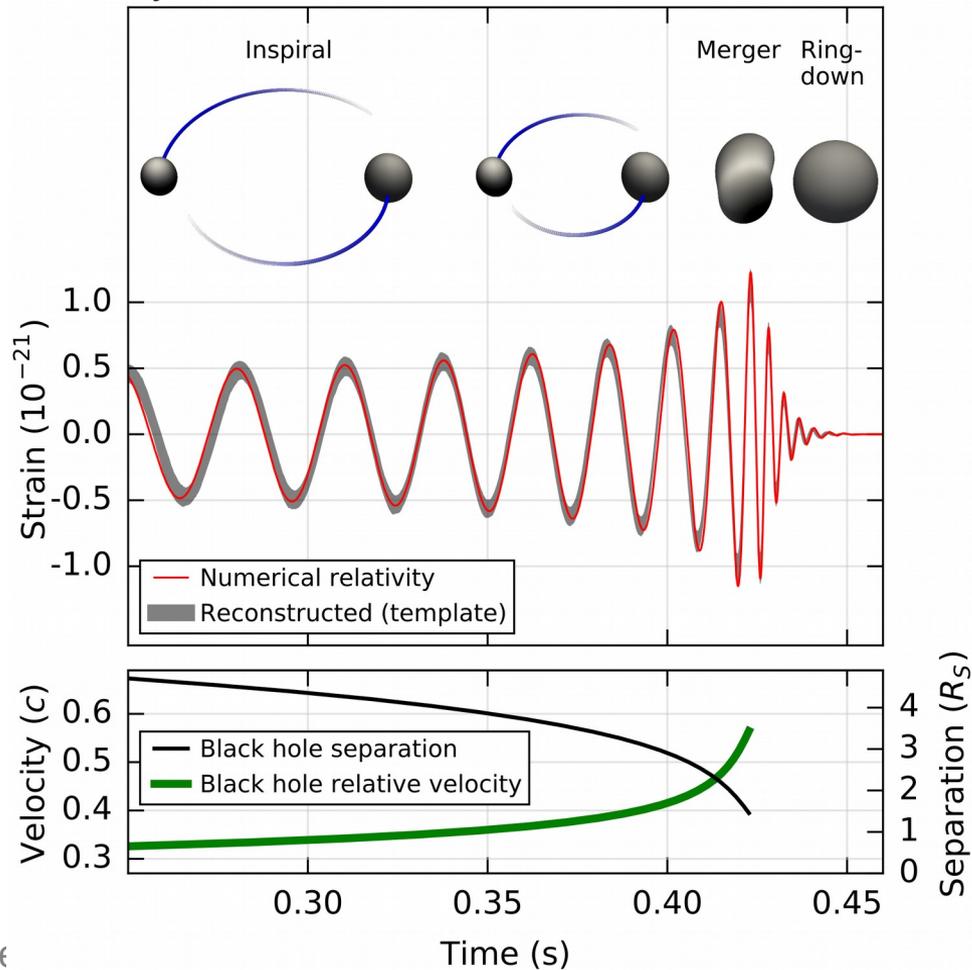
GWTC-2 plot v1.0

LIGO-Virgo | Frank Elavsky, Aaron Geller | Northwestern

Observing Run 3a Catalog: GWTC-2
[arXiv:2010.14527](https://arxiv.org/abs/2010.14527) [gr-qc]

Gravitational Strain Transduction

Phys. Rev. Lett. 116, 061102



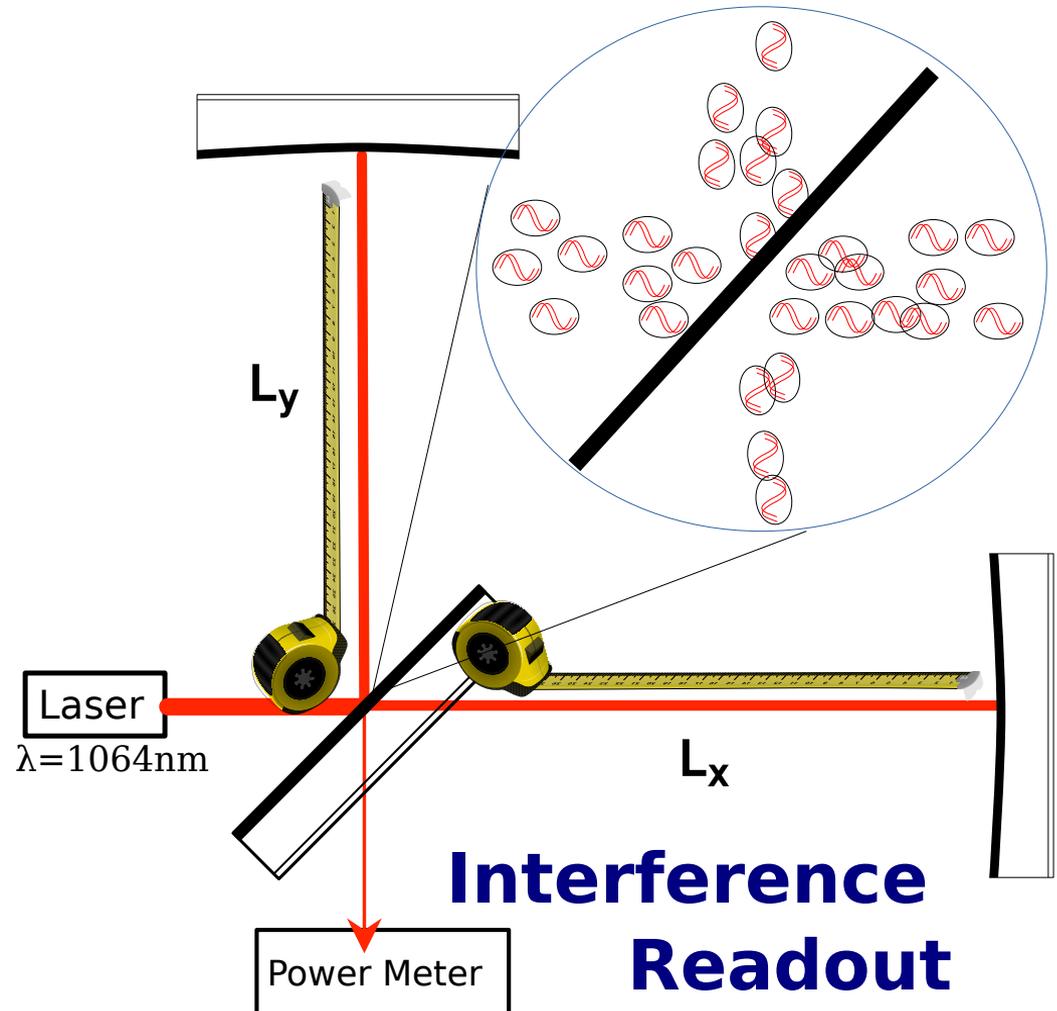
The Michelson Interferometer

Each photon gives
 $1064\text{nm}/2\pi$ measurement

minimum measurable length
variance from counting photons

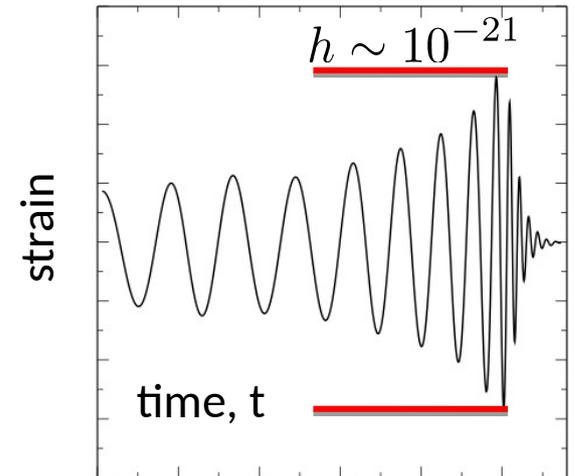
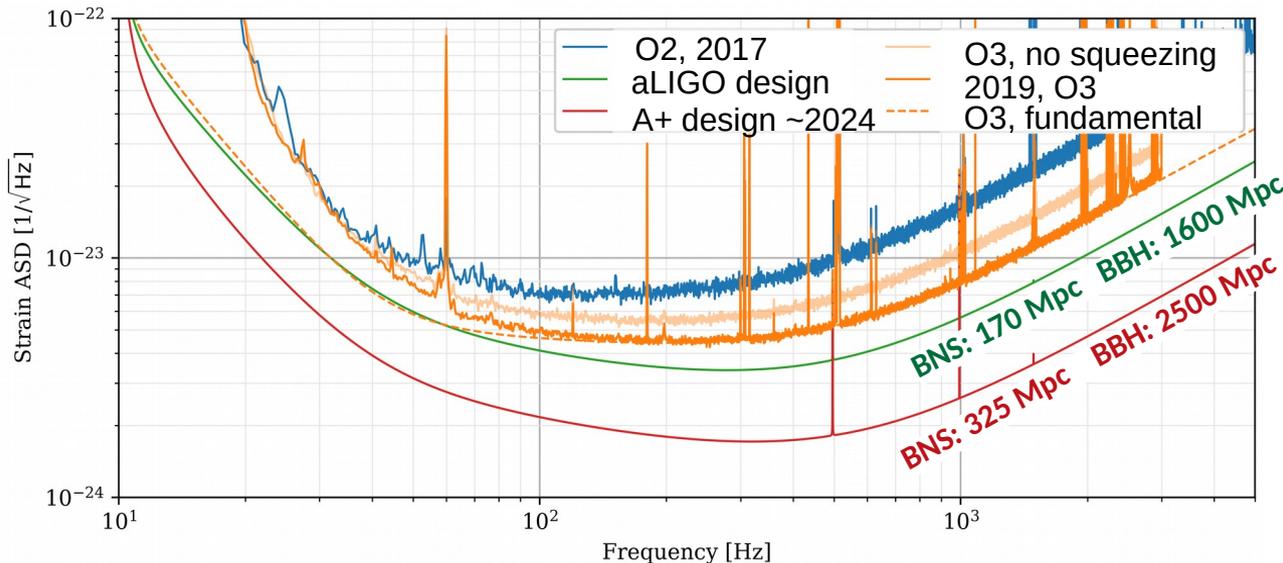
$$\Delta x \propto \frac{1}{\sqrt{N_{\text{photons}}}}$$

$\sim 10^{19}$ photons/s in
1 Watt of 1064nm light



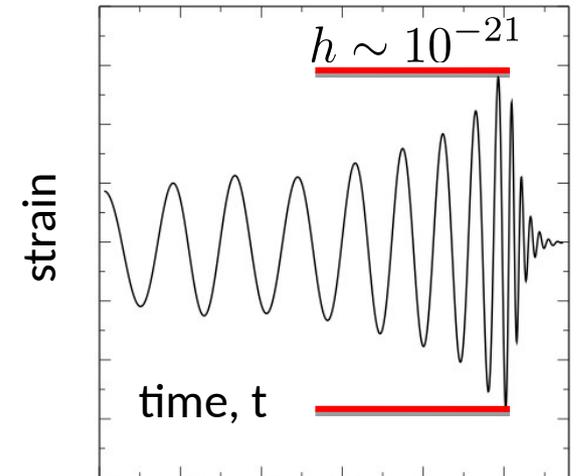
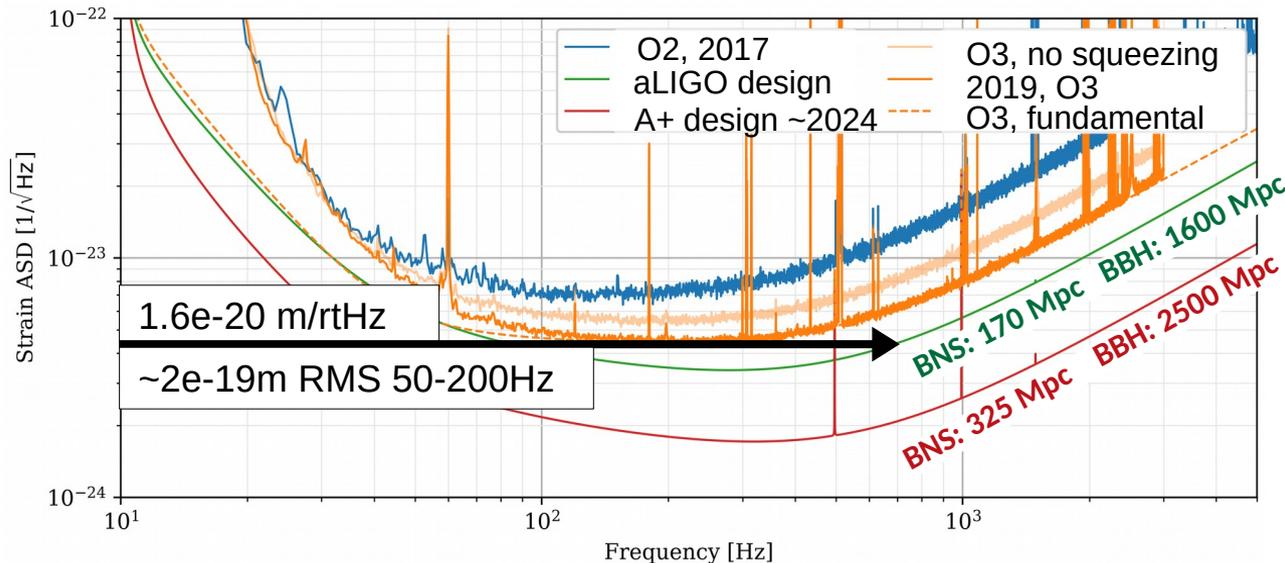
advanced LIGO Sensitivity

- 1) **Strain Noise Spectrum:** Interferometers measure GW timeseries chirping through frequency. this is the **standard deviation error density**, at each frequency
- 2) **Inspiral Range:** The distance to which fiducial 1.4/1.4 Msol binary neutron star coalescence is detectable, on average.
 - 1 Mpc \approx 3e6 light-years
 - The **event-rate** scales with the **volume**, we're talking *cubic giga-parsecs*
- 3) **RMS Strain or displacement:** the measurement error averaged over the most sensitive band



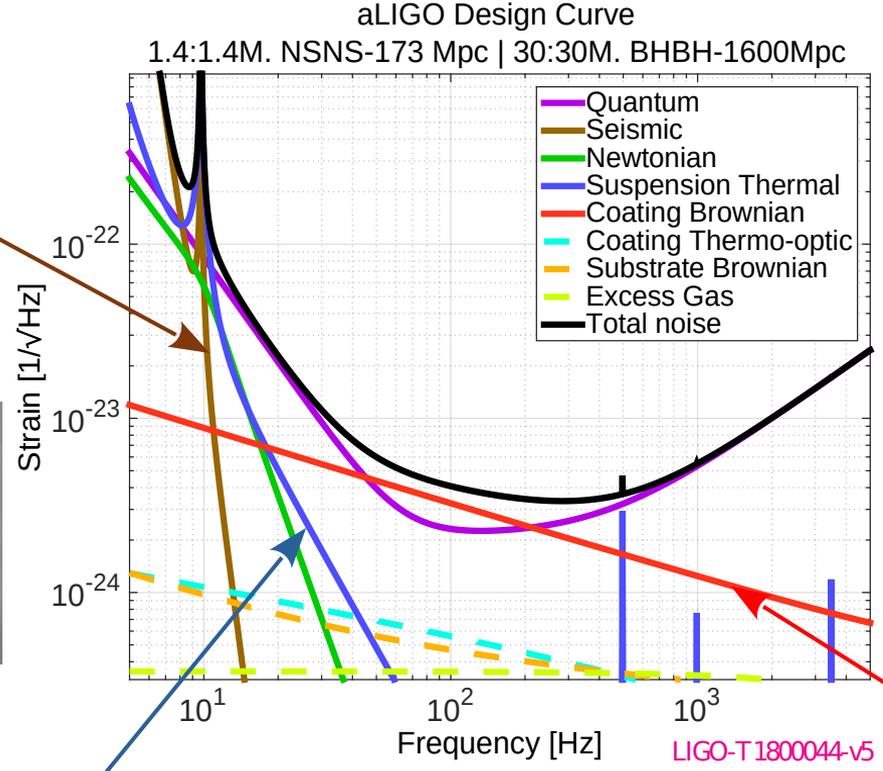
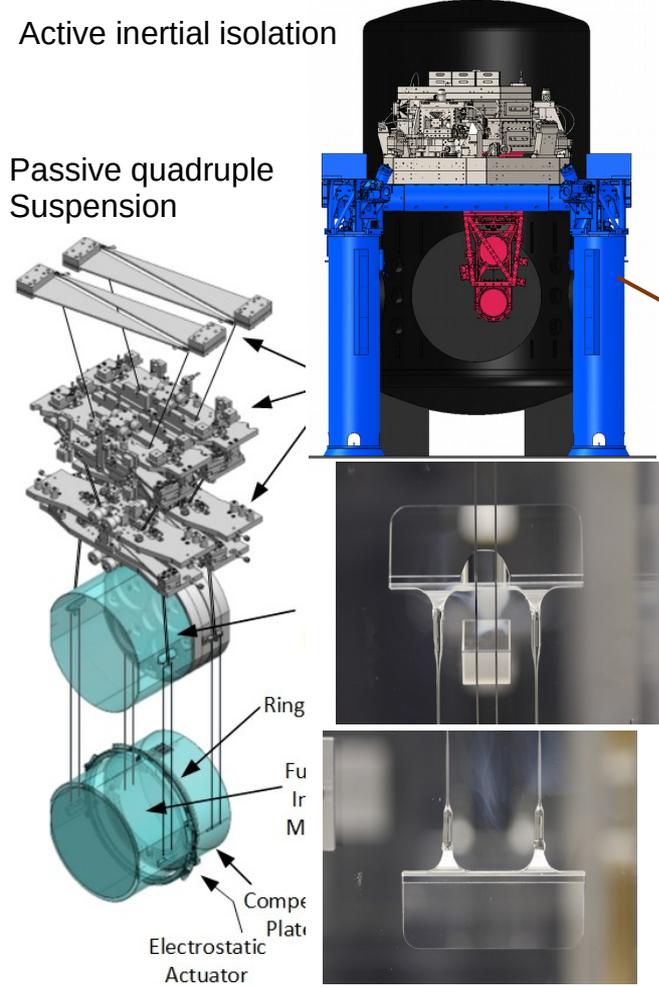
advanced LIGO Sensitivity

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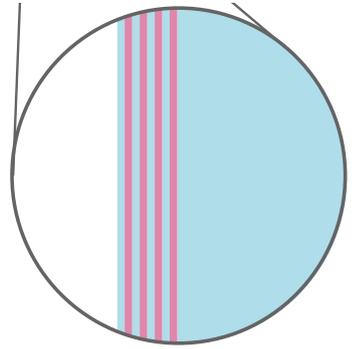
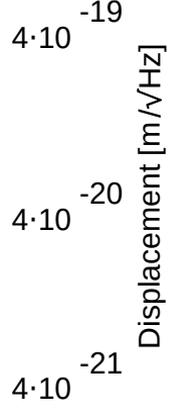
advanced LIGO's noise sources

2nm smooth core optics,
~40ppm loss on 6cm beam

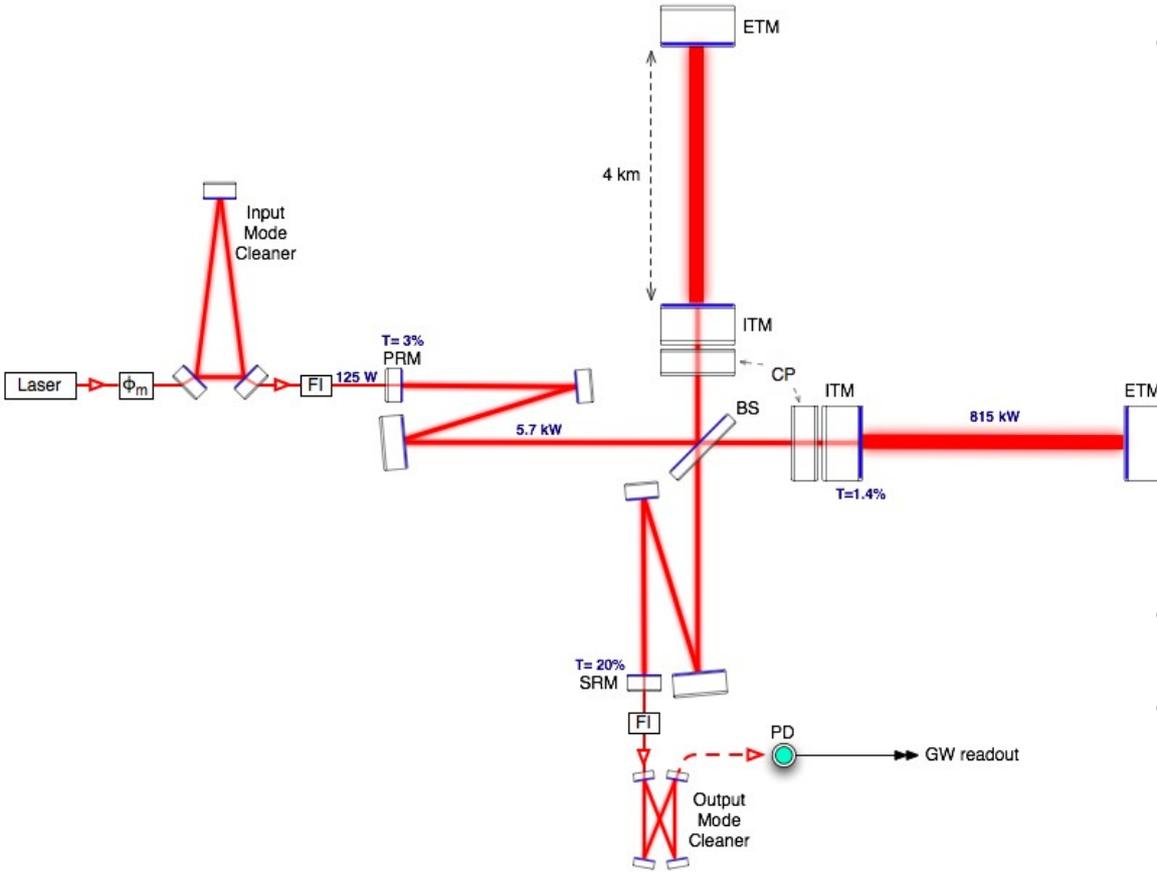


Fused Silica Suspension
Q~1 billion, 2 week ringdown

Coating materials minimize
Structural loss contributions
To thermal noises



LIGO's Optical Layout



- Michelson Interferometer with cavity enhancements
 - Power recycling mirror for higher power
 - Arm cavities enhance power *and* signal
 - Signal extraction to enhance bandwidth
- 200W Laser \rightarrow 4kW \rightarrow 800kW
- $\lambda = 1064\text{nm}$ from Nd:YAG NPRO seed laser (highly stabilized)

Scales

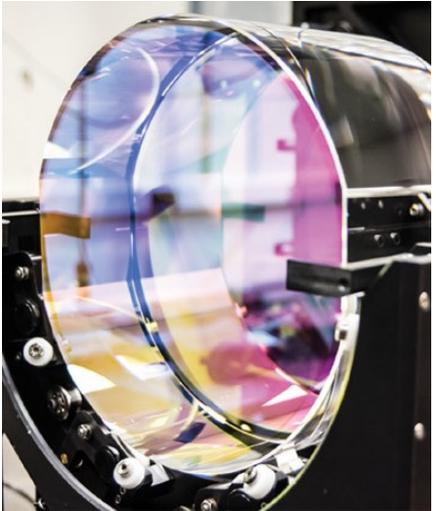
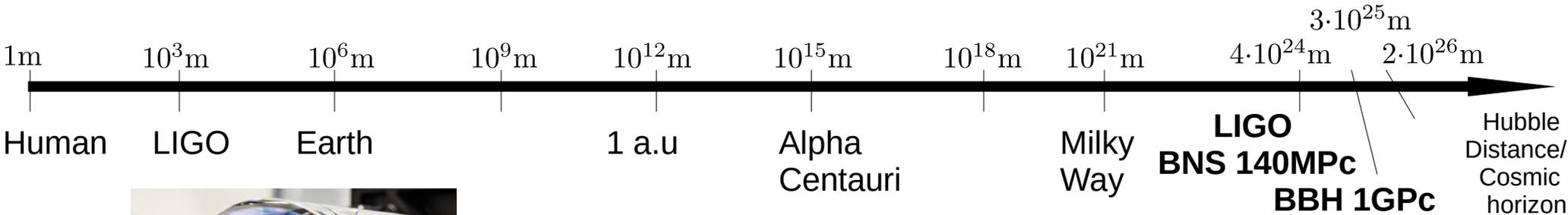
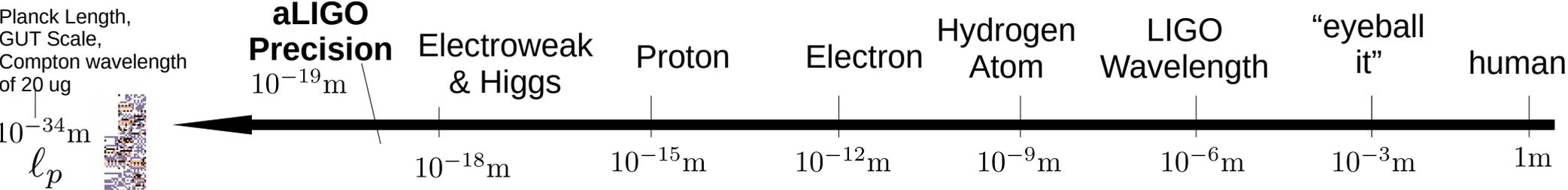
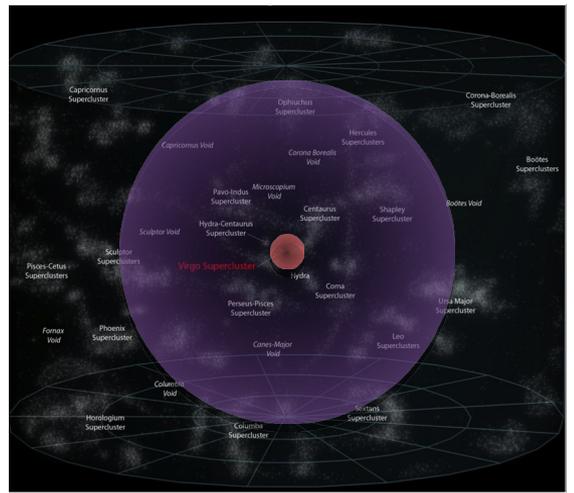
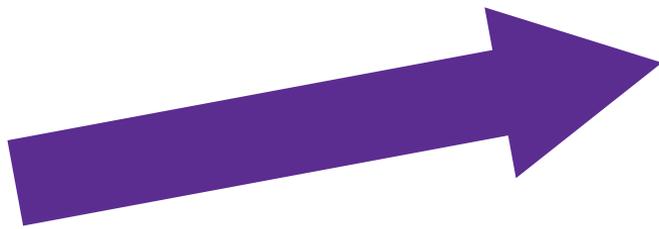


Image: Caltech LIGO Lab



Continuous Measurements

This argument
by *Braginsky*

Measurement 1

$$\hat{x}(t)$$

Measurement 2

$$\hat{x}(t + \Delta t)$$

Measurement 2b

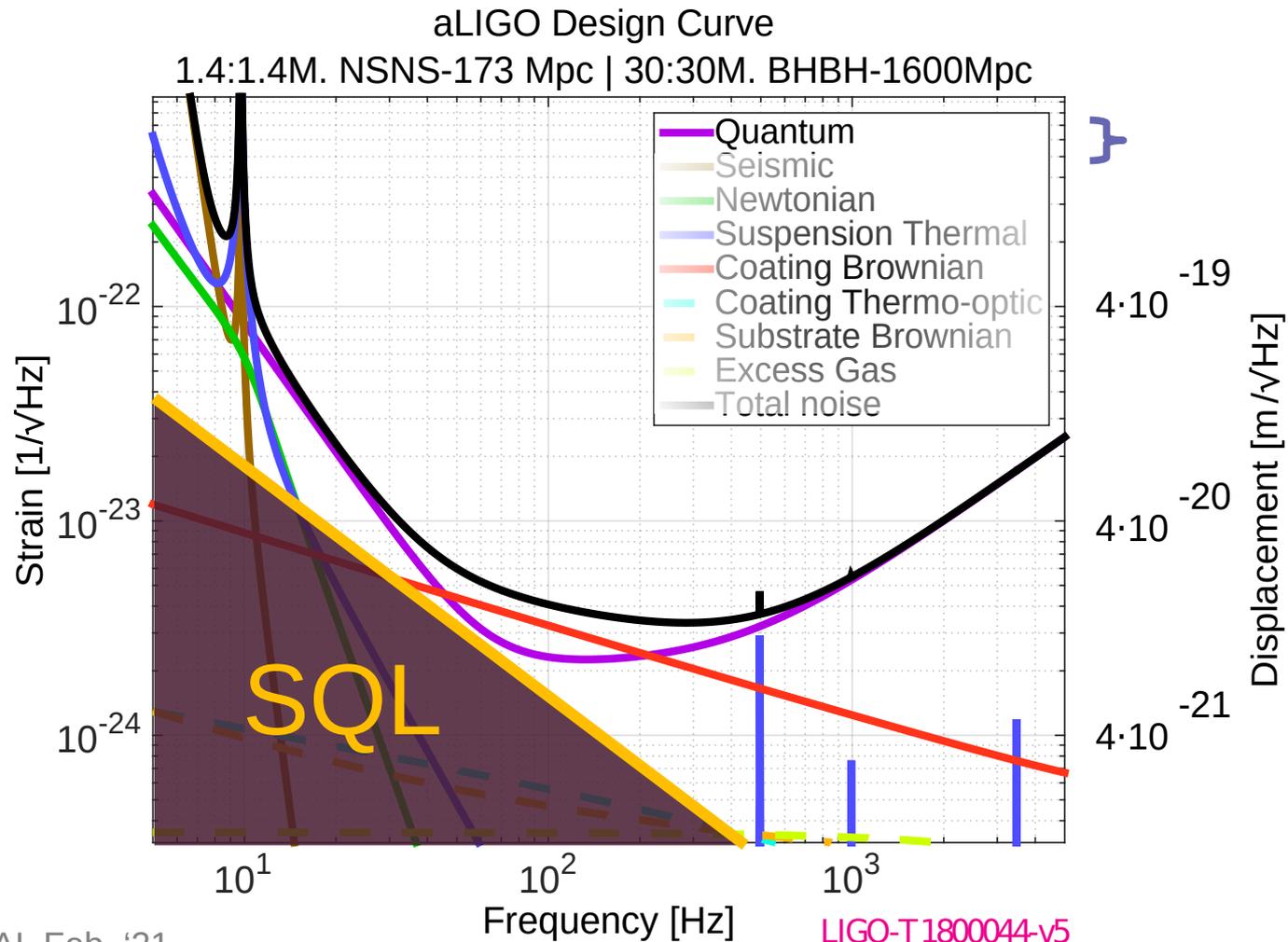
$$\dot{\hat{x}}(t) \propto \hat{p}$$

$$\Delta \hat{x} \Delta \hat{p} \geq \frac{\hbar}{2} \quad \Rightarrow \quad \Delta x_{\text{sys}} = \underbrace{\frac{\hbar}{2 \Delta x_{\text{probe}}}}_{\Delta p} \frac{\Delta t}{M}$$

Add system and probe uncertainty, convert to frequency domain

$$\Delta x_{\text{meas}}^2(\Omega) \geq \Delta x_{\text{probe}}^2(\Omega) + \Delta x_{\text{sys}}^2(\Omega)$$

The Standard Quantum Limit



What *is* measurement here?

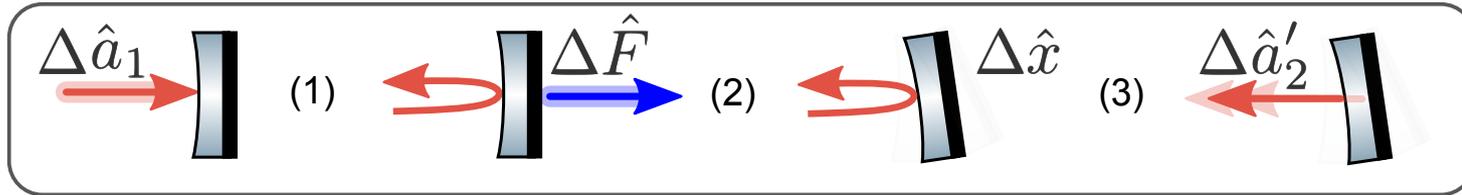
Interferometers measure \hat{x} using optical light.

Light here must be responsible for the noisy consequences of uncertainty + “collapse”

It is the quantization of the optical light that enforces uncertainty for continuous measurement: the Standard Quantum Limit

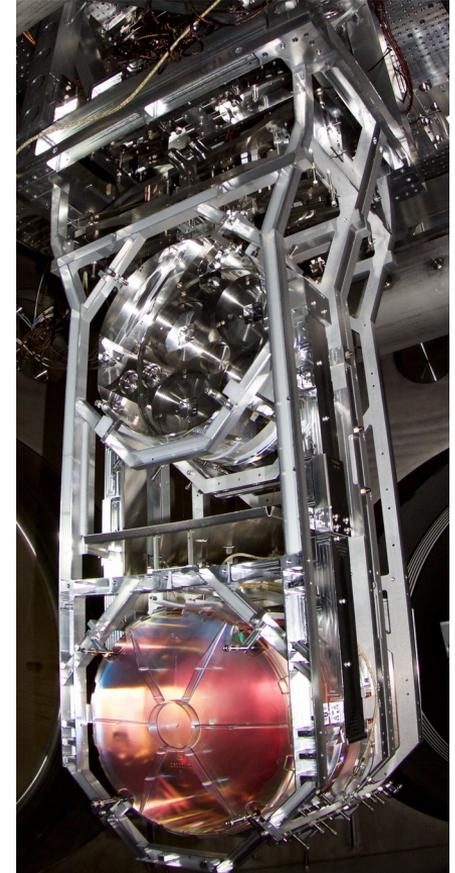
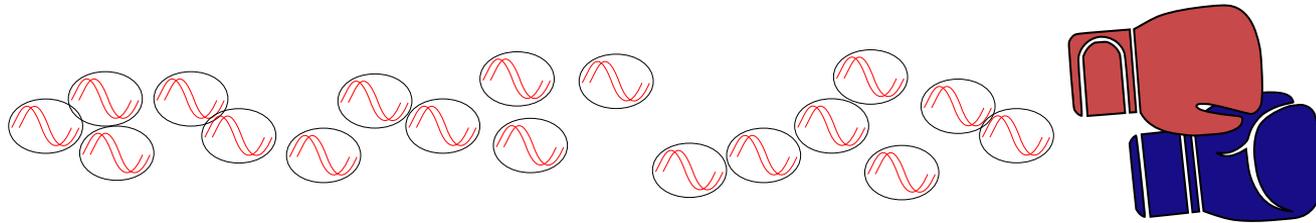
Cartoon: Particle Picture

Amplitude → Force → Displacement → Phase:



LIGO Mirrors are suspended 40kg glass cylinders

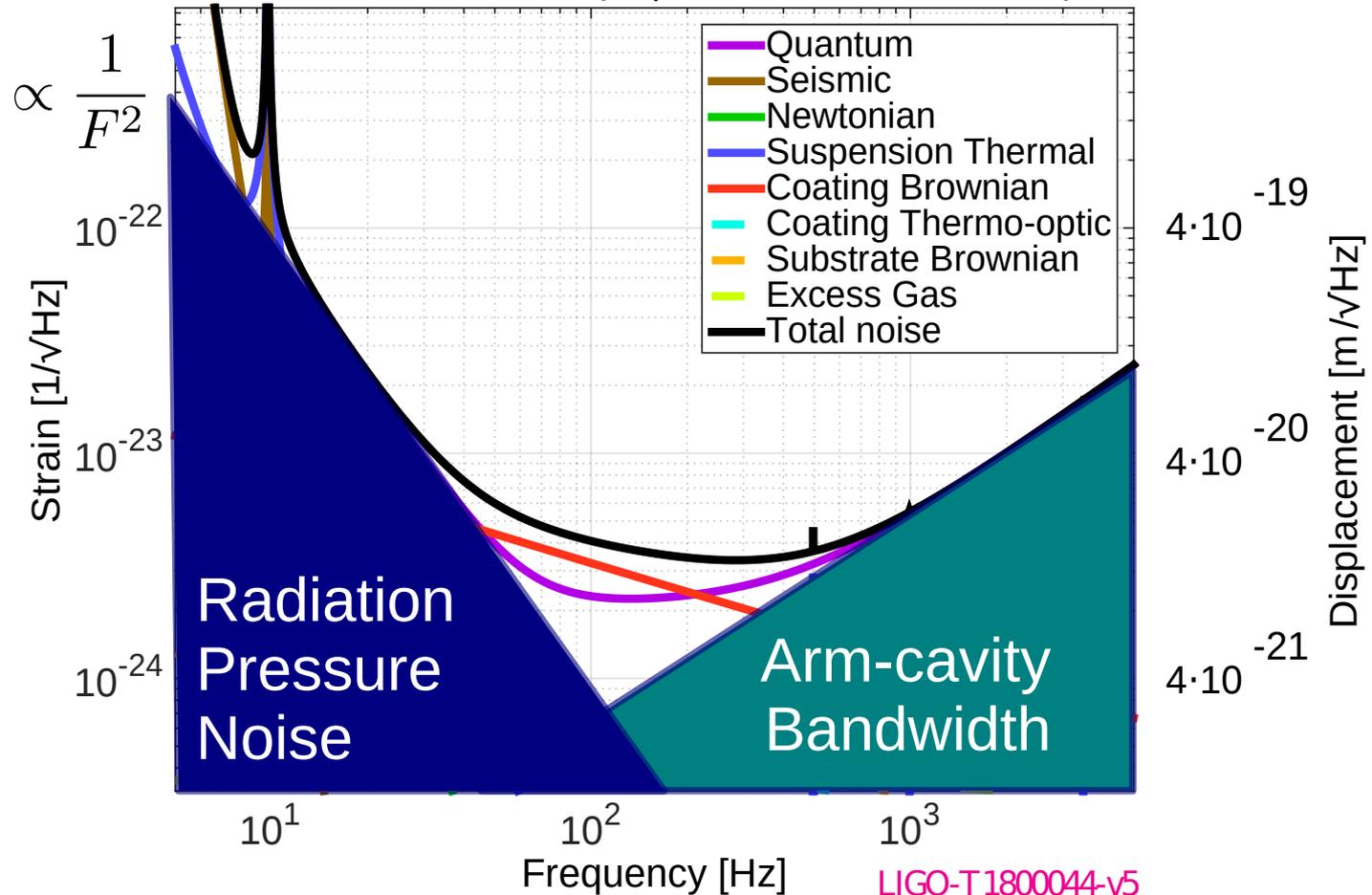
photon shot noise causes *momentum transfer* → femto-N punches



Quantum Noise Contributors

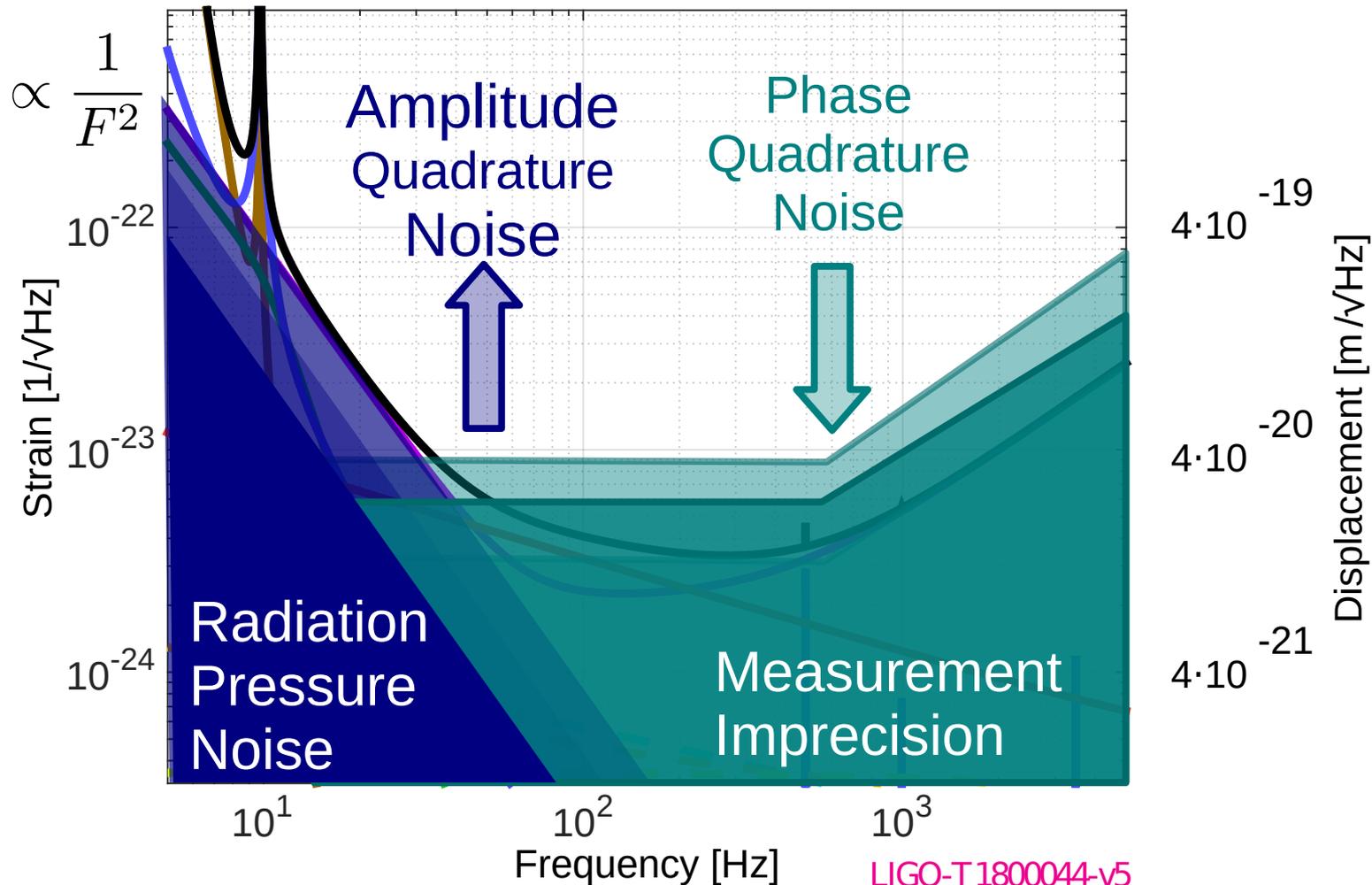
aLIGO Design Curve

1.4:1.4M. NSNS-173 Mpc | 30:30M. BHBH-1600Mpc



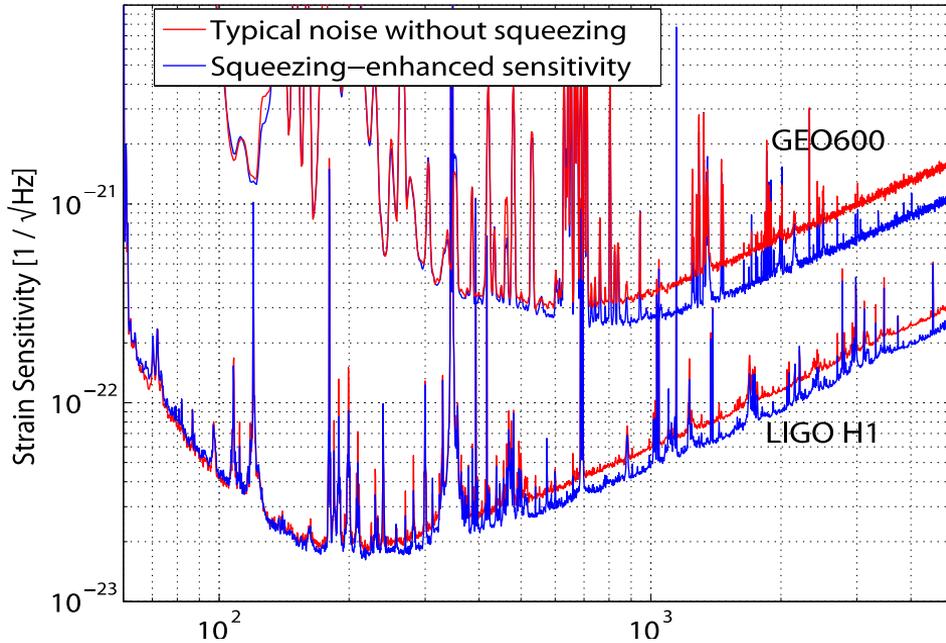
Power Dependence

The cartoon photon picture shows a necessary power dependence
The SQL derivation indicates a *probe-strength* dependence



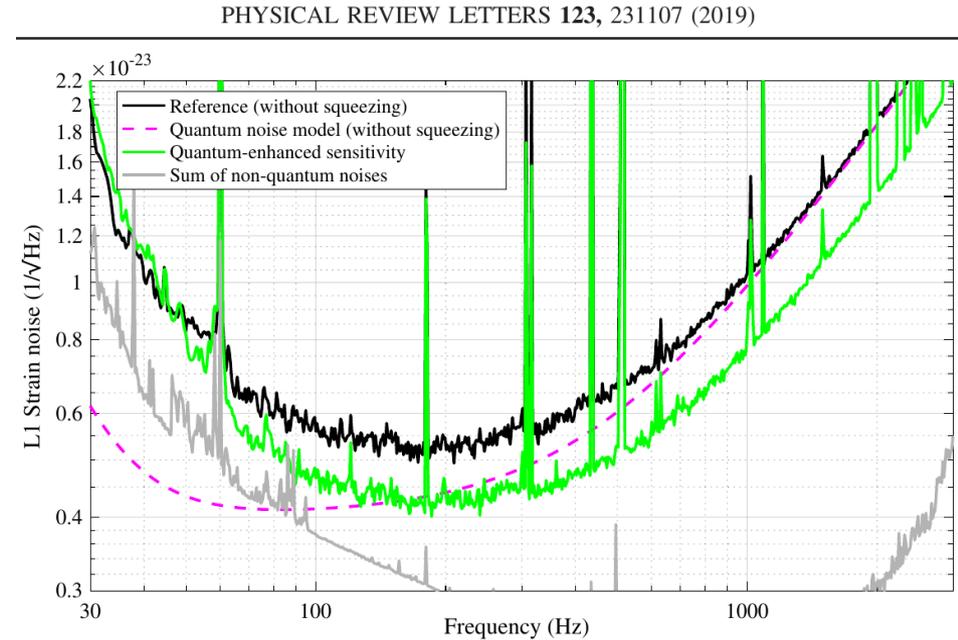
Measurement and Squeezing in LIGO

Squeezing's first at-scale demonstrations



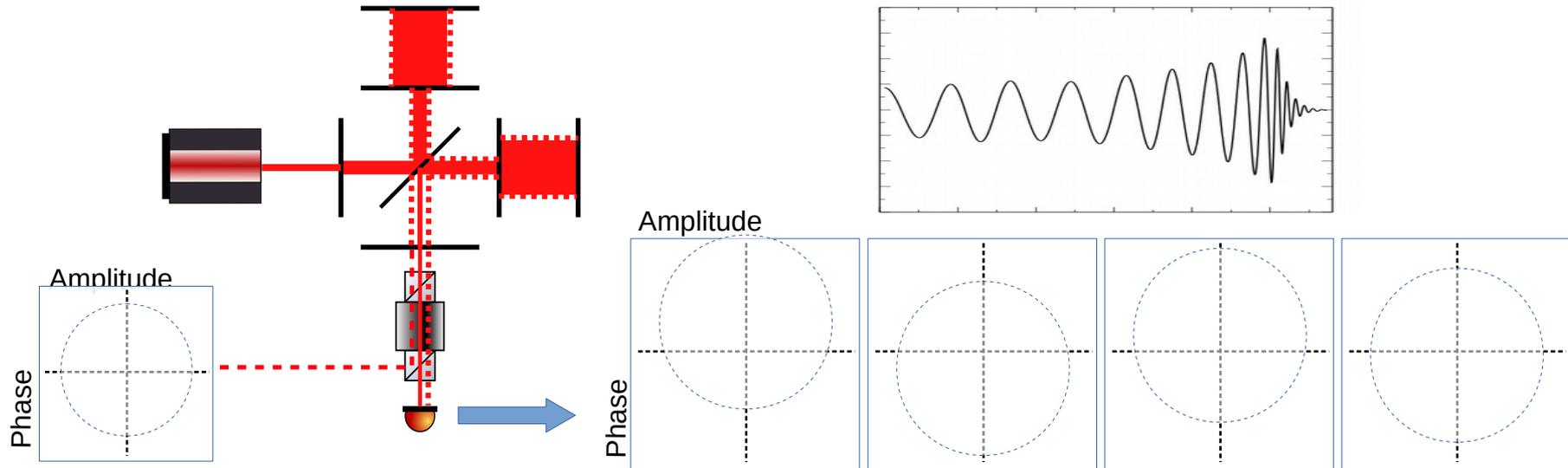
Nature Physics 7, 62–965 (2011),
Nature Photonics 7, 613–619 (2013)

Squeezing in the era of GW discovery



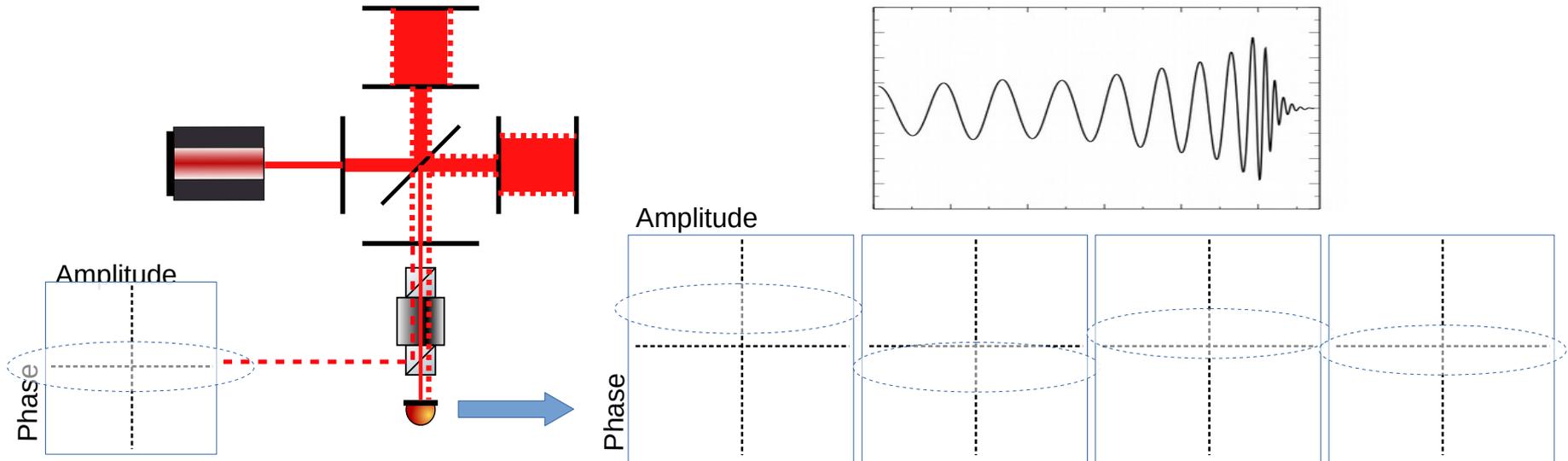
The Measurement Process

- Caves' "Quantum-mechanical Noise in an interferometer," PRD 1981 makes the leap that **the *quantum state* responsible for noise is from the *unused port***
- A more modern interpretation is that the interferometer simply applies a displacement operation to its signal state
 - The "default" signal state is vacuum
- What is "a state" here – need sampling definition (will elide, but important)



The Measurement Process

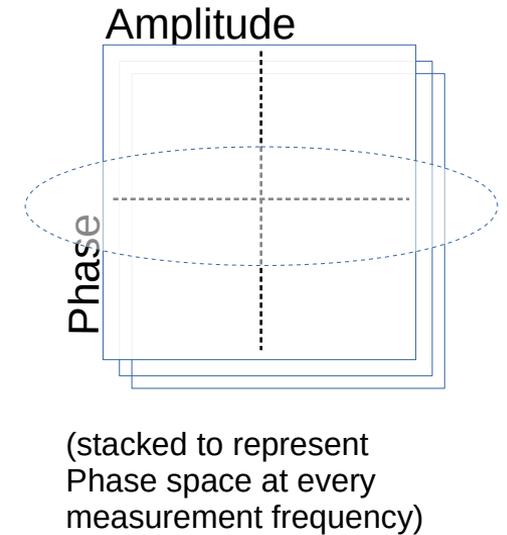
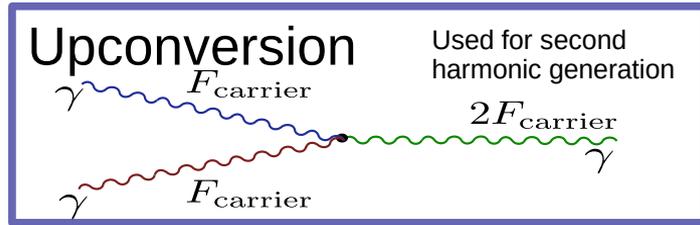
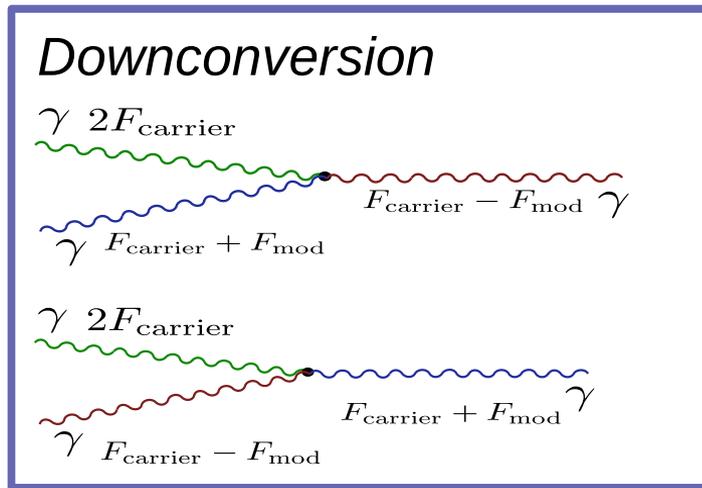
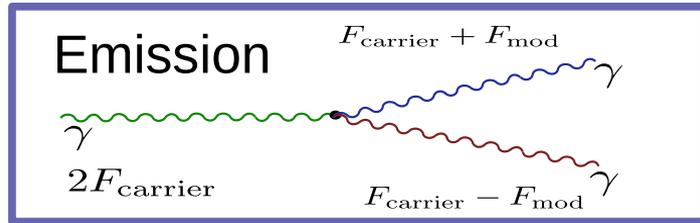
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 - The "default" signal state is vacuum
- What is "a state" here – need sampling definition (will elide, but important)



Quantum Process of Squeezing

Nonlinear $\chi^{(2)}$ crystal activates a Three-Photon interaction (vertex)

$$\mathcal{H}_{\text{int}} = \kappa b^\dagger a a + \text{c.c.}$$

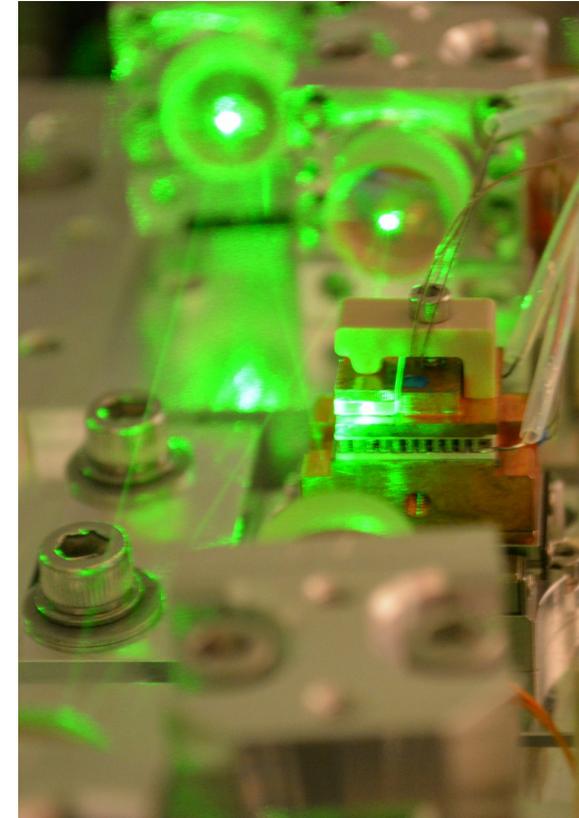
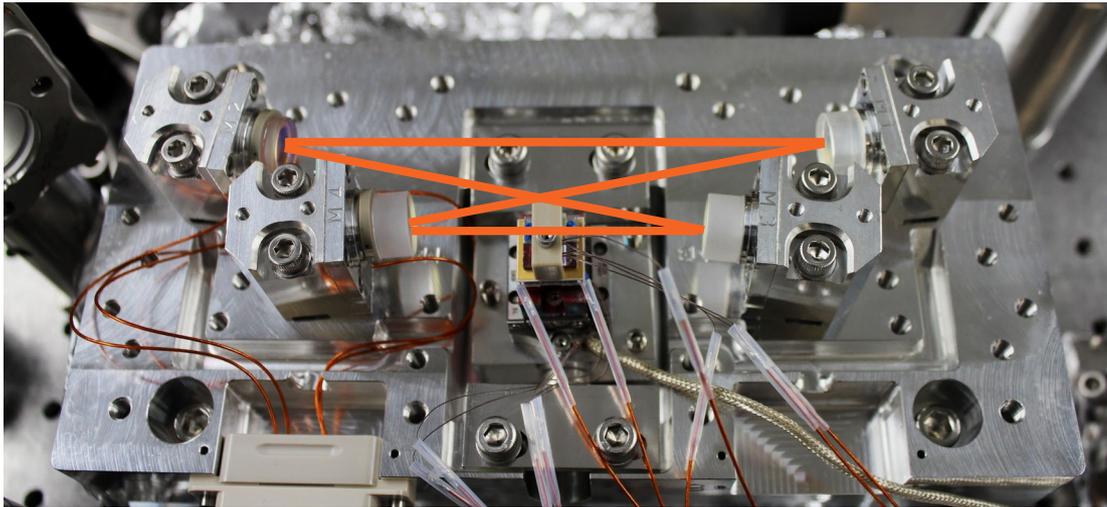


Convert from sideband/ladder operators
To quadrature/Hermitian operators

Crystal Optical Parametric Amplifier

nonlinear crystal driven by second harmonic (532nm) + oven + phase control

bowtie cavity
strengthens interaction
isolates backscatter



Wade, A. R. et al. Optomechanical design and construction of a vacuum-compatible optical parametric oscillator for generation of squeezed light. *Review of Scientific Instruments* 87, 063104 (2016).

Oelker, E. et al. Ultra-low phase noise squeezed vacuum source for gravitational wave detectors. *Optica*, *OPTICA* 3, 682–685 (2016).

Stefszky, M. et al. An investigation of doubly-resonant optical parametric oscillators and nonlinear crystals for squeezing. *J. Phys. B: At. Mol. Opt. Phys.* 44, 015502 (2010).

The Livingston in-vacuum Platform

Even with a femto-watt of light leaking to the squeezer, you need sub-angstrom noise

The platform is installed on an active inertial In-vacuum optics table, near the readout



above, Maggie Tse operates on the platform

Degradations in Squeezing

Be aware of this distinction:

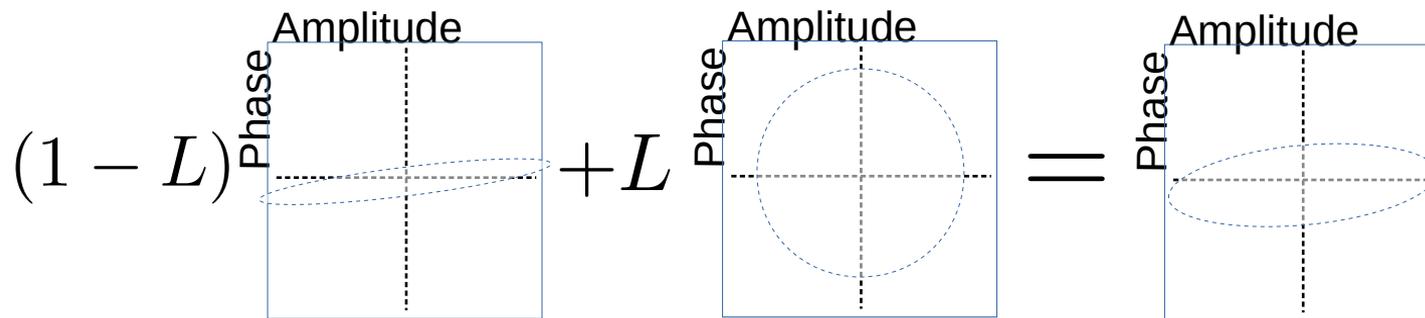
Generated or Injected squeezing

- can be determined from calibration measurements
- Perfect relation between squeezing and antisqueezing (saturates Heisenberg)

Measured squeezing

Measured Antisqueezing

- Degraded by loss and dephasing
- Different effects in each characterizes degradation



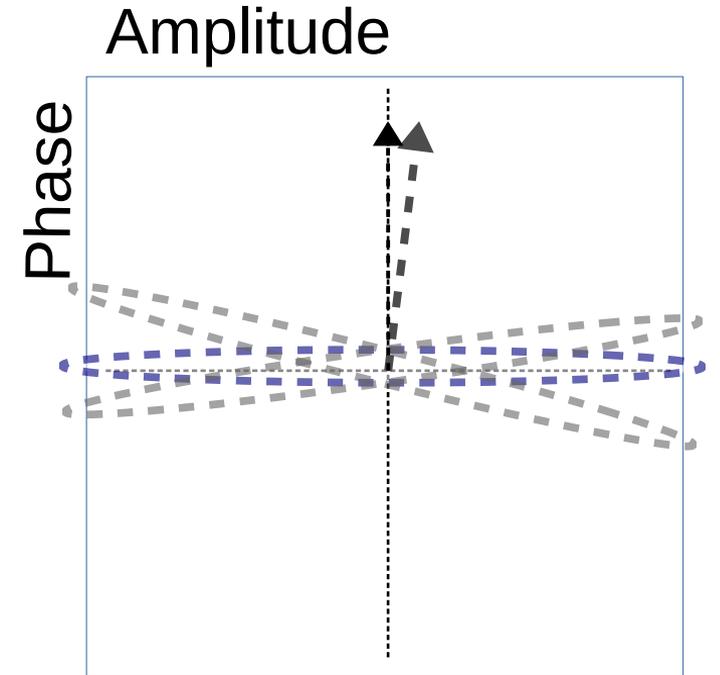
$$(1-L) \begin{bmatrix} e^{-2r} & 0 \\ 0 & e^{2r} \end{bmatrix} 2E_\lambda + L \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \frac{\hbar\omega}{2} \xrightarrow{r=\infty} \begin{bmatrix} L & 0 \\ 0 & e^{2r} \end{bmatrix} \frac{\hbar\omega}{2}$$

Phase Noise in Squeezing

- Squeezing Follows independent path
- Fluctuations rotate noise matrix
- Quadratic Effect, but significant at large squeezing

$$\Xi = E \left[\sin^2(\hat{\theta}) \right] \quad 0 \leq \Xi \leq \frac{1}{2}$$

$$(1 - \Xi) \begin{bmatrix} e^{-2r} & 0 \\ 0 & e^{2r} \end{bmatrix} \frac{\hbar\omega}{2} + \Xi \begin{bmatrix} e^{2r} & 0 \\ 0 & e^{-2r} \end{bmatrix} \frac{\hbar\omega}{2}$$



Technical Limits of Squeezing

- Phase noise implies point of optimal generated squeezing
- also point of maximum observable squeezing

- In the limit

- Low phase noise

- low loss

$$\theta_{\text{rms}} = \sqrt{\Xi} \ll 0.5$$

$$L \ll 1$$

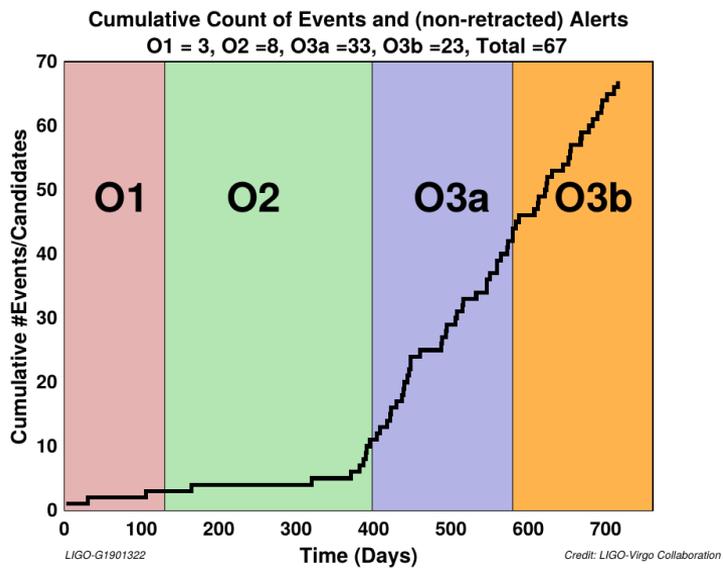
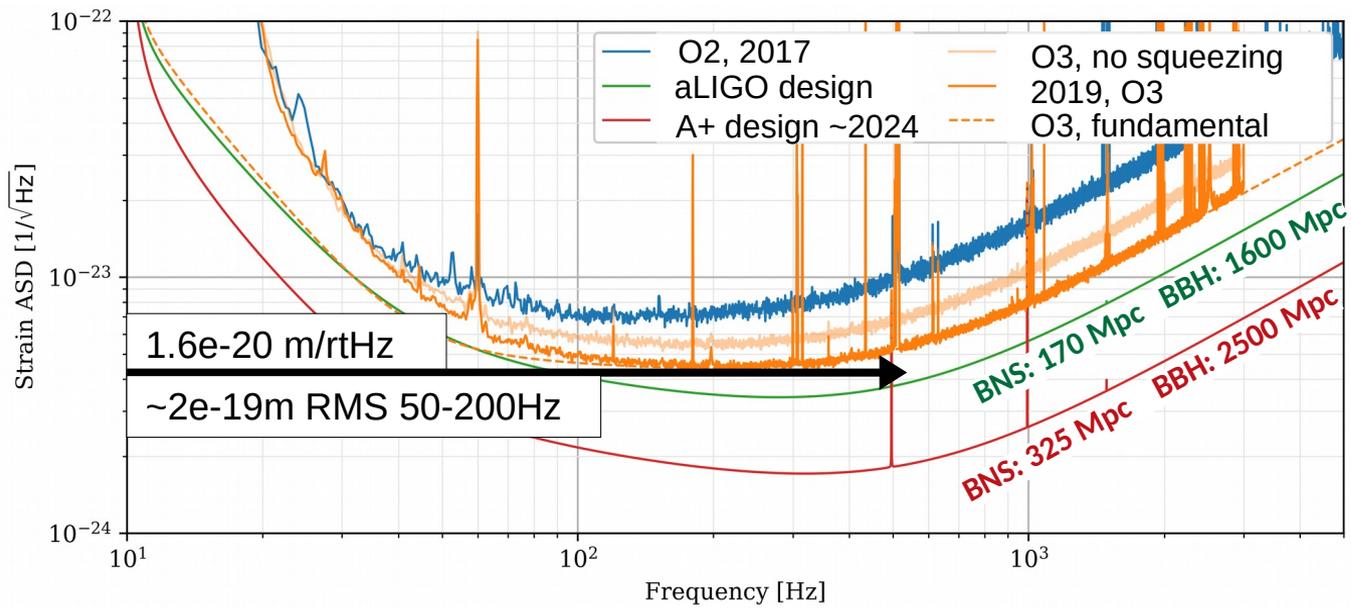
Best Shot noise reduction is: [db]

$$10\text{Log}_{10}(2\theta_{\text{rms}} + L)$$

Squeezing in Observing Run 3

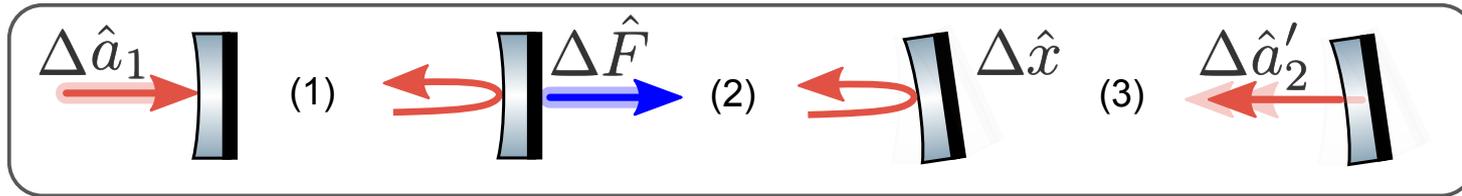
- O3 saw *many improvements*:
Power level, scatter, duty cycle, *grounding*, laser noises, angular and auxiliary control, glitch and data analysis
- The detectors have become *impressively* quantum limited: 120Mpc
- Enter Squeezing, 3db @ ~30% losses 120 → 140Mpc
→ 50% rate increase on top of everything else

Buikema, A. et al.
Sensitivity and performance of the Advanced LIGO detectors in the third observing run.
Phys. Rev. D 102, 062003 (2020).



Cartoon: “Wave” Picture

Amplitude → Force → Displacement → Phase:

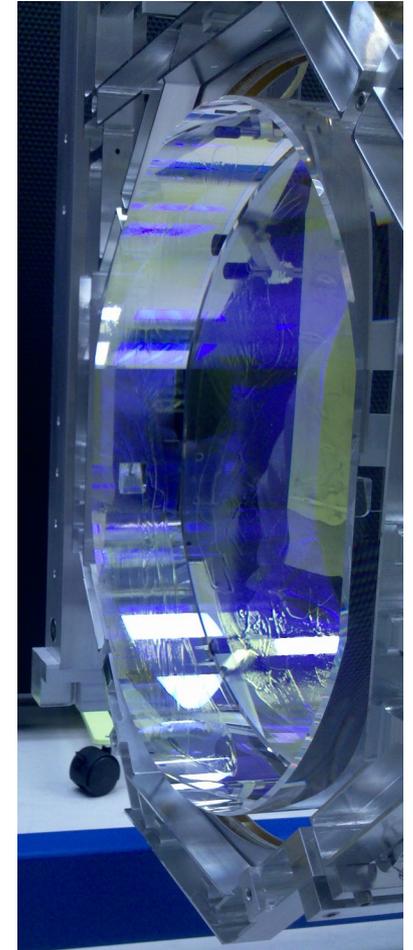


Mechanics cause a shear action on the optical phase-space

Due to radiation pressure & mechanical susceptibility

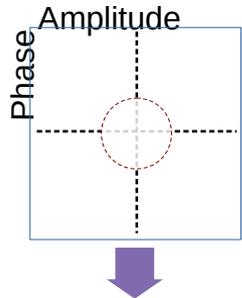
$$\begin{bmatrix} \Delta \hat{a}'_1 \\ \Delta \hat{a}'_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ -\mathcal{K}(F) & 1 \end{bmatrix} \begin{bmatrix} \Delta \hat{a}_1 \\ \Delta \hat{a}_2 \end{bmatrix}$$

Shear = rotation * squeezing * rotation

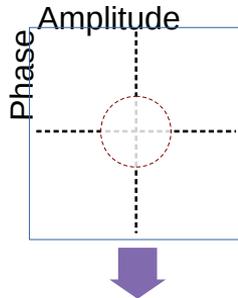


Standard Quantum Limit, optics picture

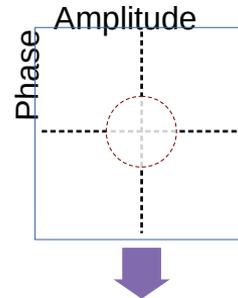
$F \ll 60\text{Hz}^*$



$F = 60\text{Hz}^*$

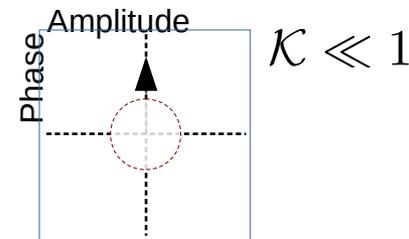
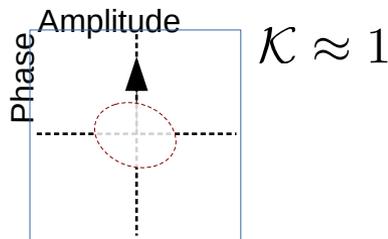
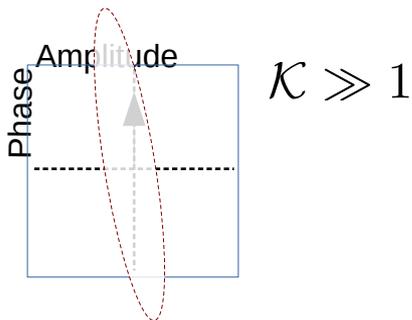


$F \gg 60\text{Hz}^*$



Amplitude → **Force** → **Displacement** → **Phase**:
Phase-space Shear

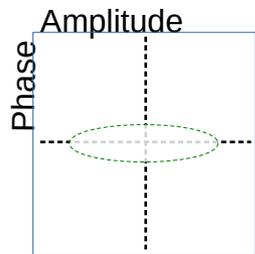
$$\begin{bmatrix} \Delta \hat{a}'_1 \\ \Delta \hat{a}'_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ -\mathcal{K}(F) & 1 \end{bmatrix} \begin{bmatrix} \Delta \hat{a}_1 \\ \Delta \hat{a}_2 \end{bmatrix}$$



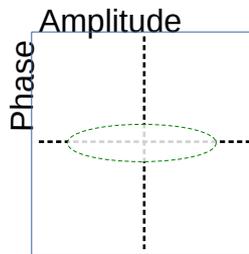
* ~60Hz is approximate crossover only in aLIGO full power design

Squeezing Probes Harder

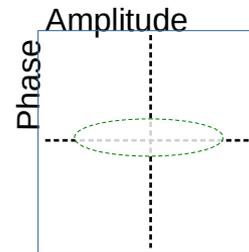
$F \ll 60\text{Hz}^*$



$F = 60\text{Hz}^*$

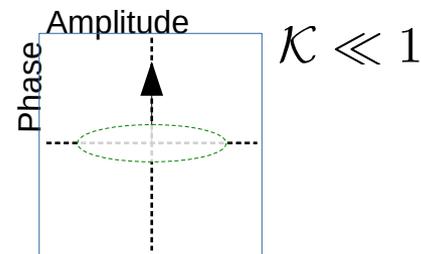
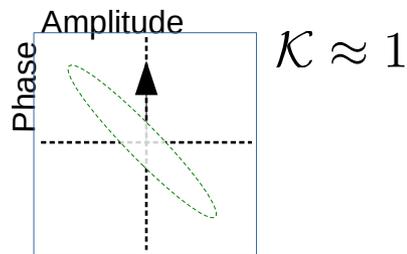
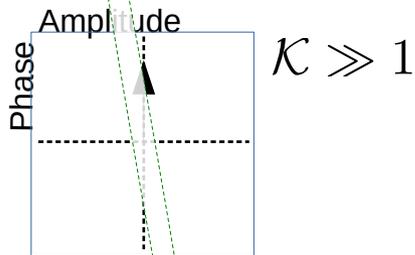


$F \gg 60\text{Hz}^*$



Amplitude → **Force** → **Displacement** → **Phase:**
Phase-space Shear

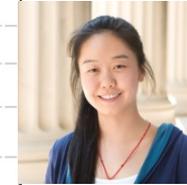
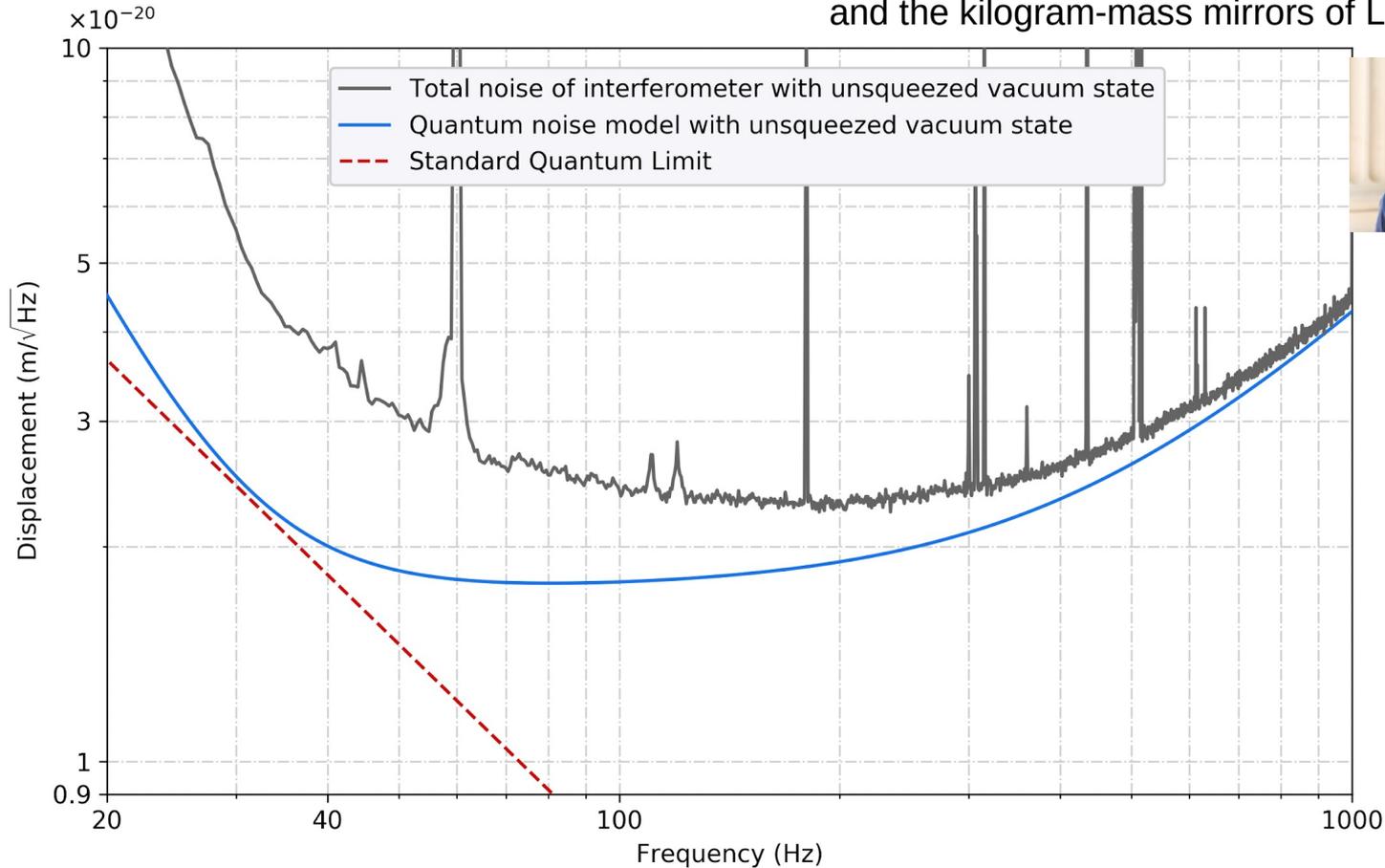
$$\begin{bmatrix} \Delta \hat{a}'_1 \\ \Delta \hat{a}'_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ -\mathcal{K}(F) & 1 \end{bmatrix} \begin{bmatrix} \Delta \hat{a}_1 \\ \Delta \hat{a}_2 \end{bmatrix}$$



* ~60Hz is approximate crossover only in aLIGO full power design

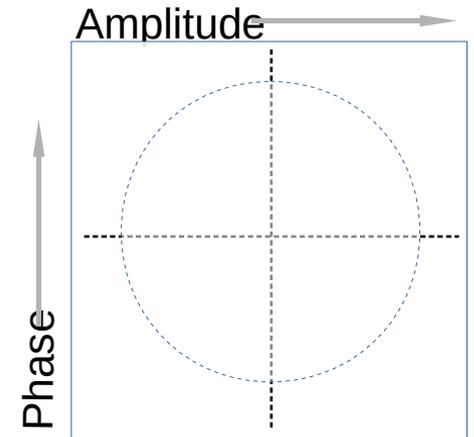
Testing the SQL

Haocun Yu, McCuller, L. et al. Quantum correlations between light and the kilogram-mass mirrors of LIGO. Nature 583, 43–47 (2020).



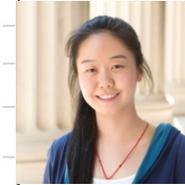
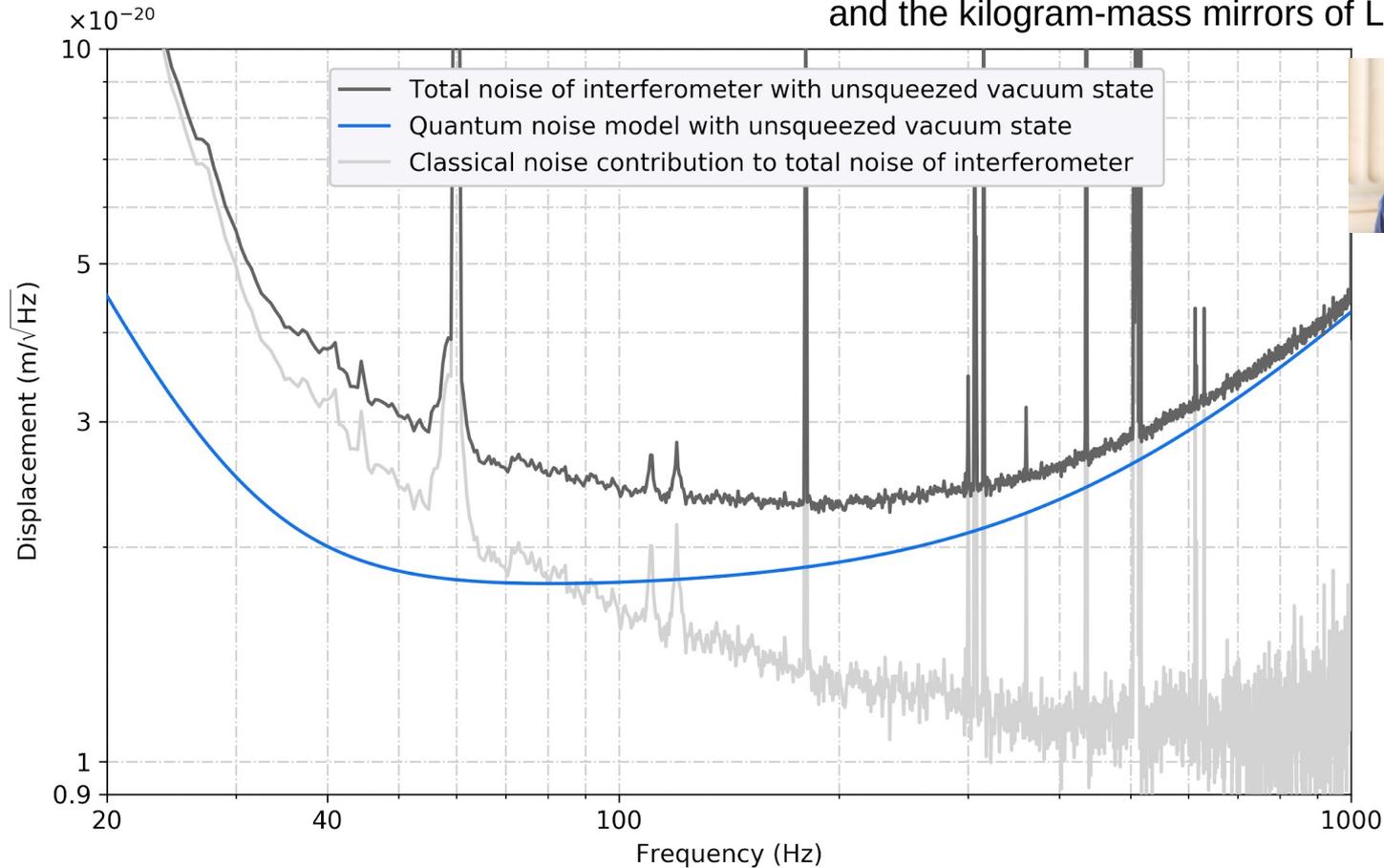
Left: measurements performed by Haocun Yu

No injected squeezing



Determine Instrument Noise

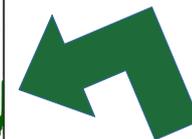
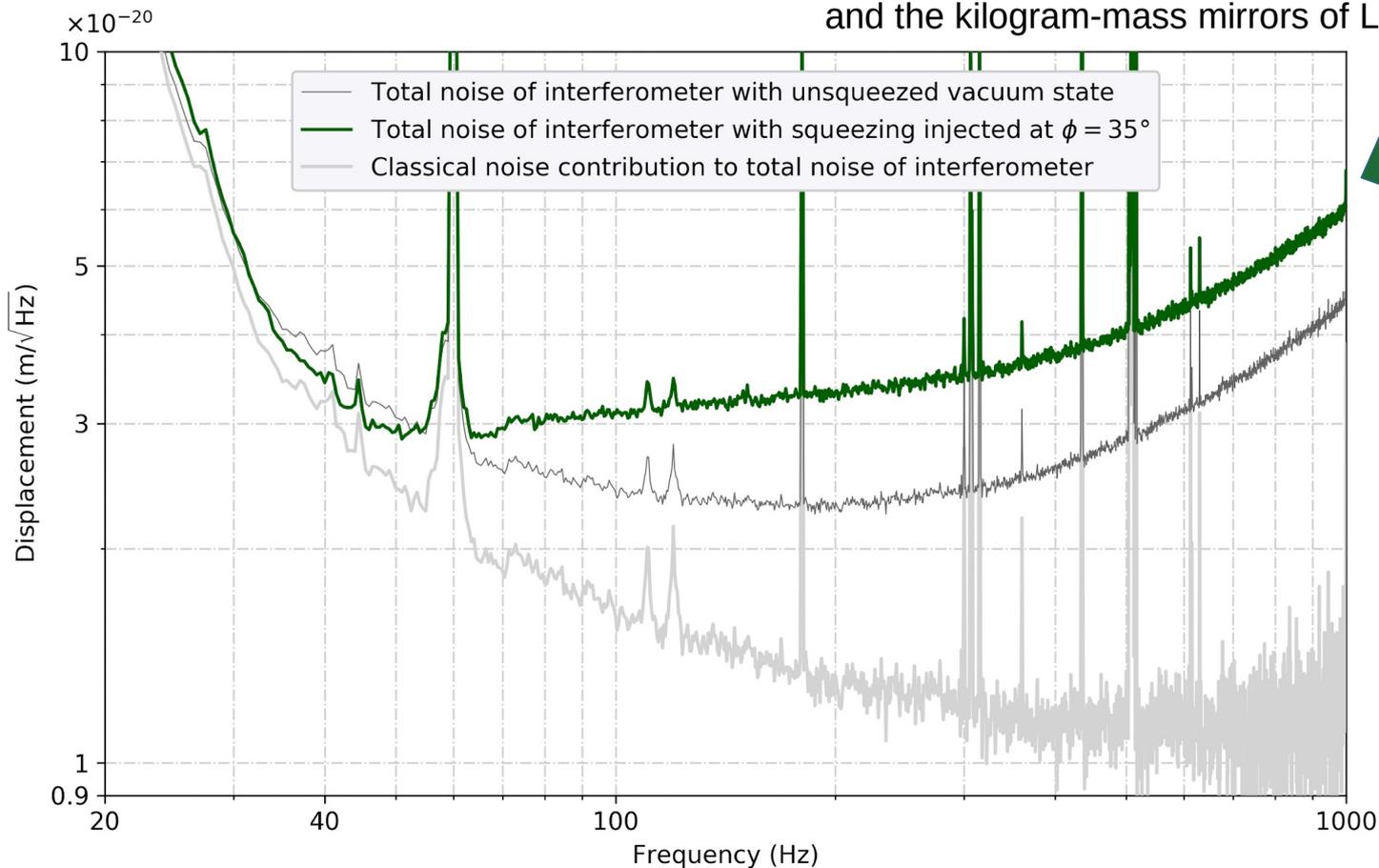
Haocun Yu, McCuller, L. et al. Quantum correlations between light and the kilogram-mass mirrors of LIGO. *Nature* 583, 43–47 (2020).



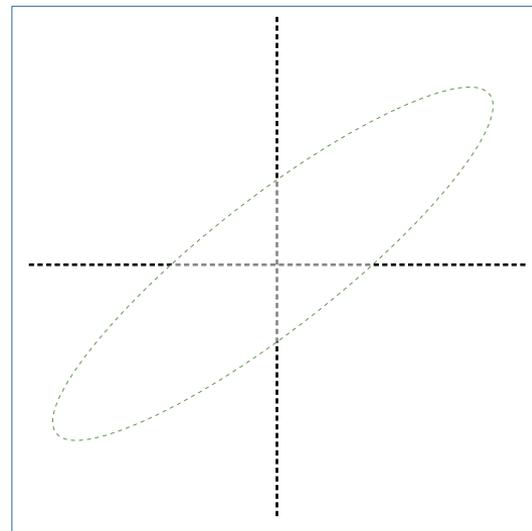
Left: measurements performed by Haocun Yu

Inject Squeezing at an Angle

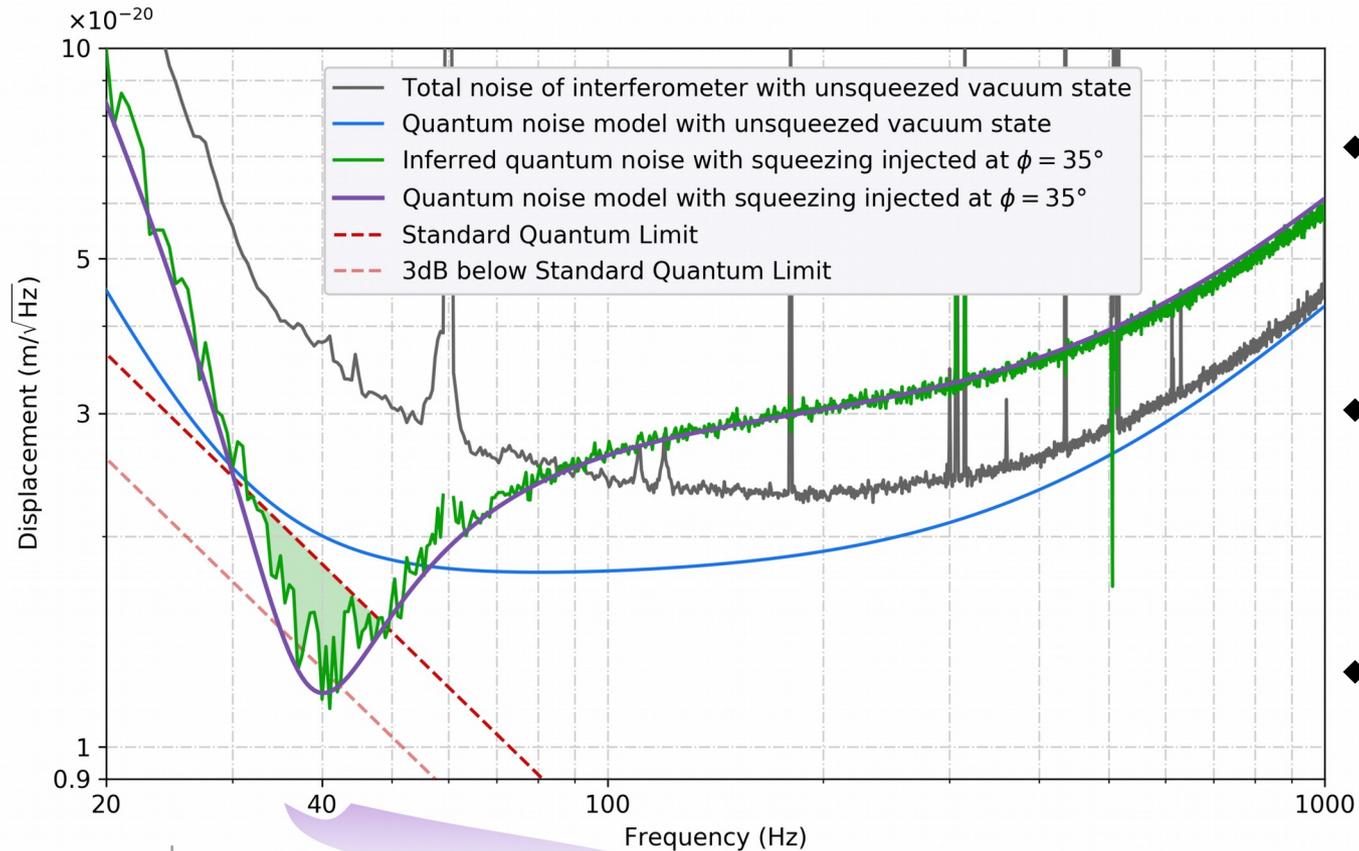
Haocun Yu, McCuller, L. et al. Quantum correlations between light and the kilogram-mass mirrors of LIGO. Nature 583, 43–47 (2020).



Squeezing
at 33deg injected

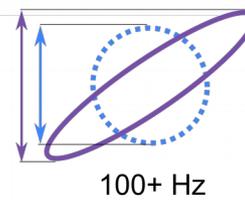
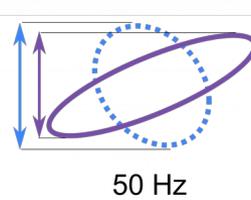
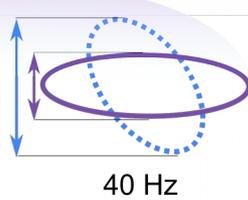
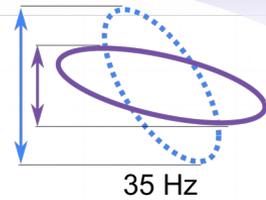
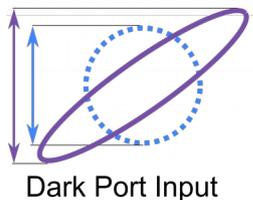


Sub-SQL Quantum Noise in 40kg



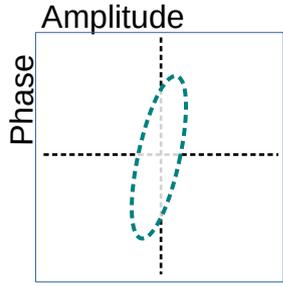
Nature 583, 43–47 (2020).

- ◆ Shows that the vacuum indeed pushes the mirrors: **quantum radiation pressure noise**
- ◆ Shows that the SQL is not a limit → mirror motion creates and maintains quantum correlations
- ◆ ~billion-times heavier than recent sub-SQL measurements, **human scale! Room temp.!**

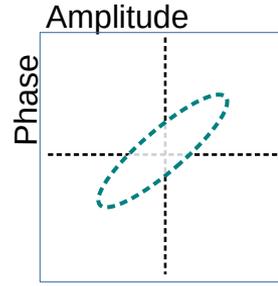


But I want more Squeezing *and* more Astrophysics

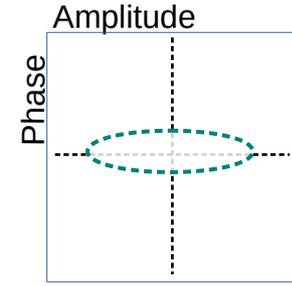
$$F \ll 60\text{Hz}^*$$



$$F = 60\text{Hz}^*$$

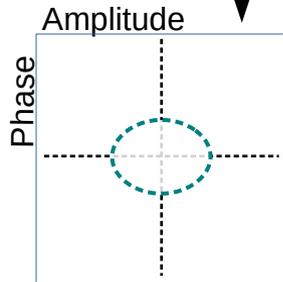


$$F \gg 60\text{Hz}^*$$

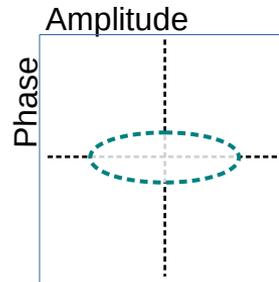


merely
unsqueezes

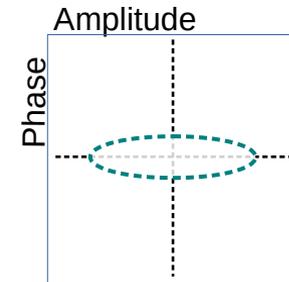
Frequency Dependent Squeezing



$$\mathcal{K} \gg 1$$



$$\mathcal{K} \approx 1$$



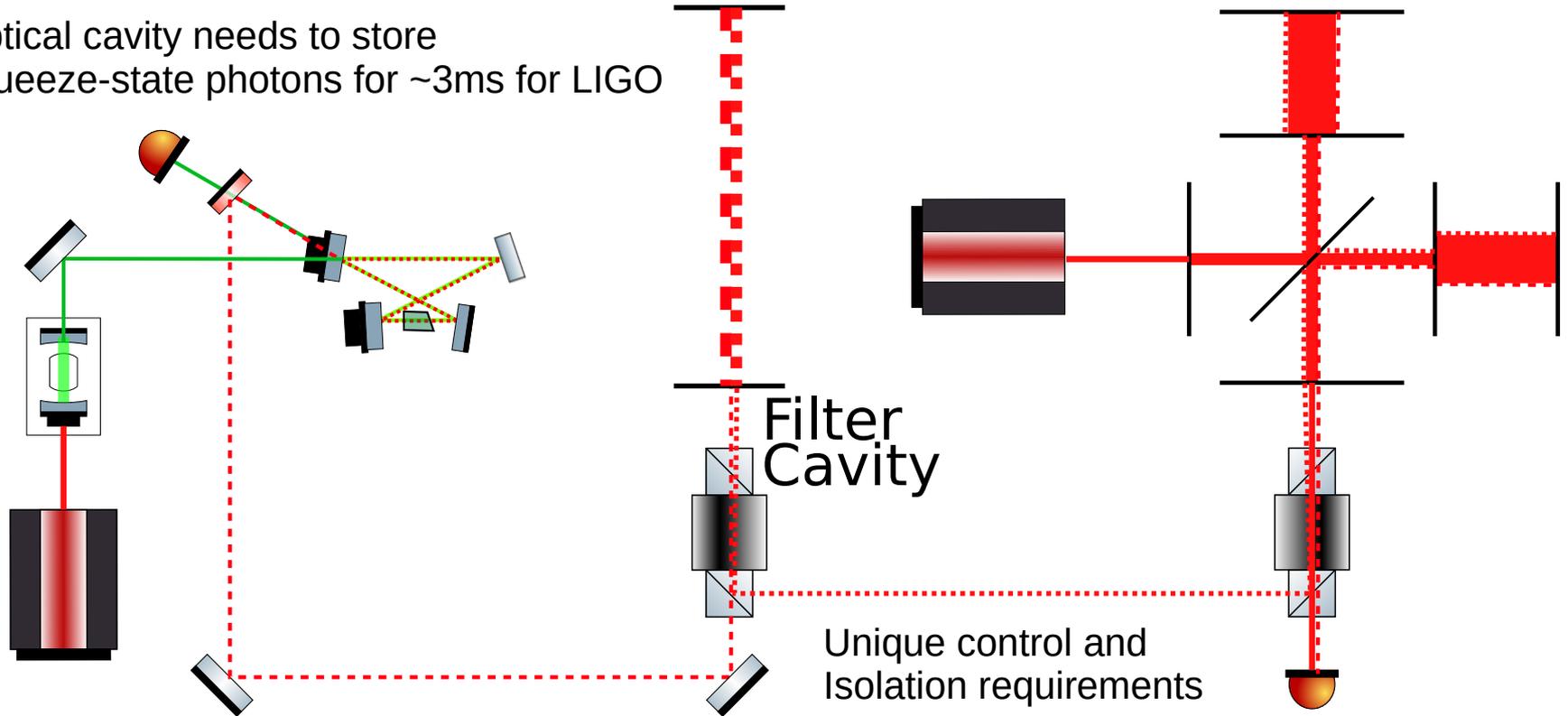
$$\mathcal{K} \ll 1$$

Quantum Filter Cavity

McCuller, L. et al. Frequency-Dependent Squeezing for Advanced LIGO. Phys. Rev. Lett. 124, 171102 (2020).

Zhao, Y. et al. Frequency-Dependent Squeezed Vacuum Source for Broadband Quantum Noise Reduction in Advanced Gravitational-Wave Detectors. Phys. Rev. Lett. 124, 171101 (2020).

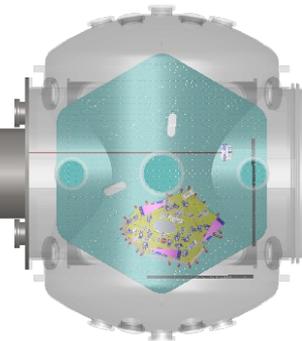
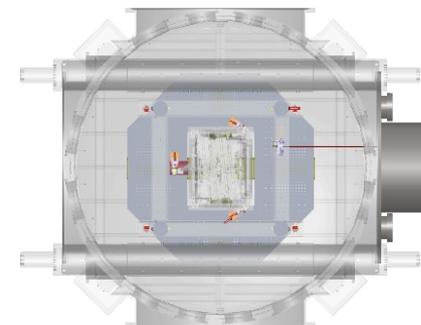
Optical cavity needs to store squeeze-state photons for $\sim 3\text{ms}$ for LIGO



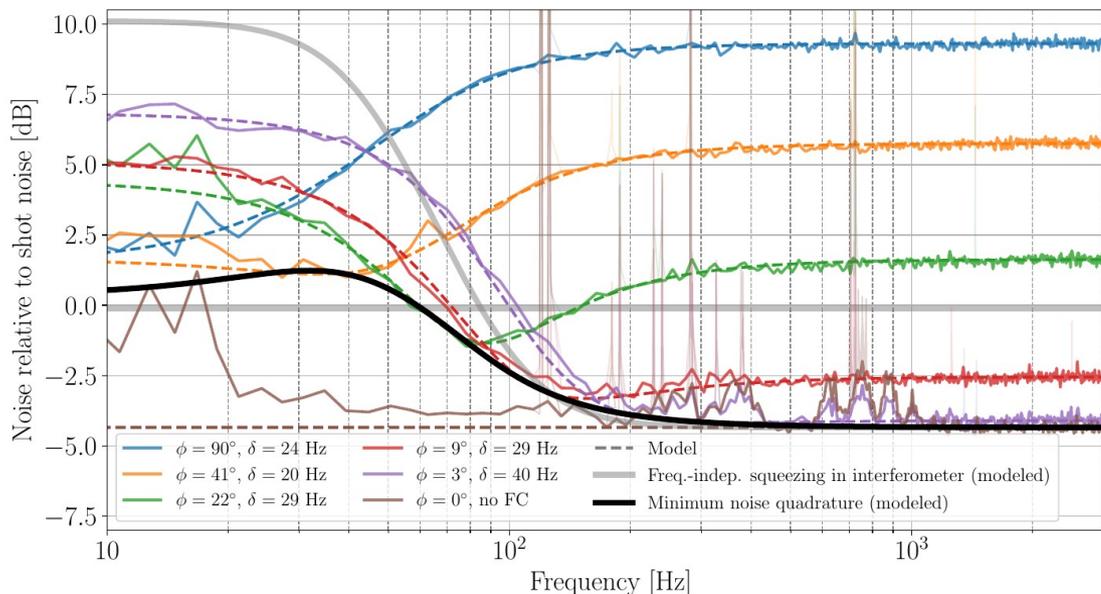
MIT 16m Filter Cavity

Finesse 80,000 \rightarrow \sim 100Hz linewidth \rightarrow photons travel \sim 1000km

McCuller, L. et al. Frequency-Dependent Squeezing for Advanced LIGO. Phys. Rev. Lett. 124, 171102 (2020).

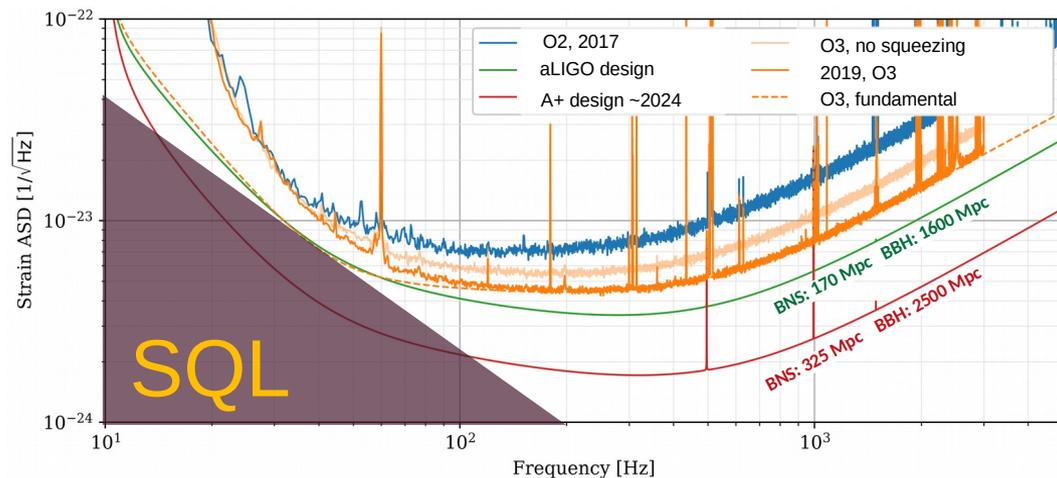
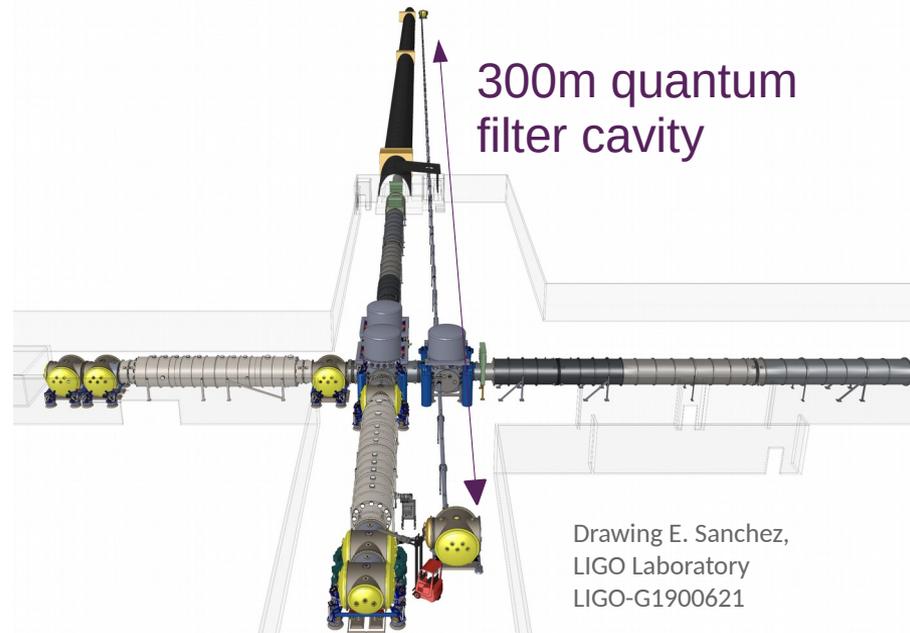


Chris Whittle,
Dhruva Ganapathy
and
Kentaro Komori



The A+ Upgrade

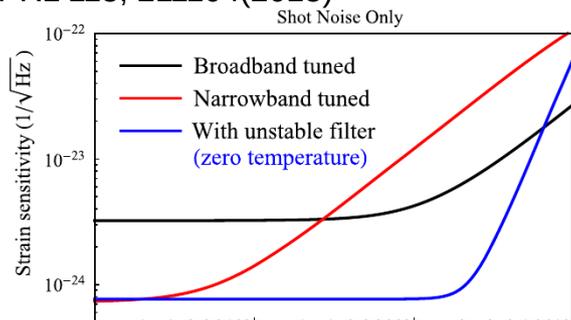
- 6db of frequency-dependent squeezing
 - Early install, aiming at 4.5db in Run 4
 - Sub-SQL during observations!
- 2x improved coating thermal noise
 - Still researching, but good leads
- Active wavefront control
 - Lowers squeezing loss
- Balanced homodyne readout
 - Multiple benefits
- Bigger Beamsplitter



Quantum Physics for Fundamental Physics

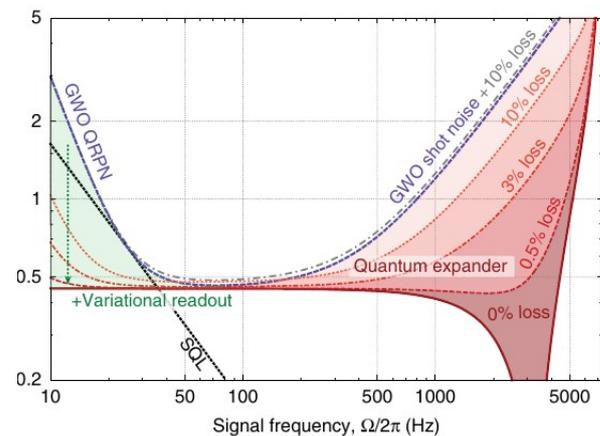
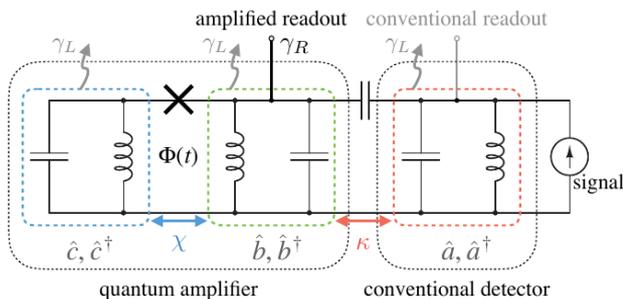
- Now solidly in the NISQ-era of quantum metrology
 - Squeezed states are Gaussian states
 - Limited by loss: $10\text{Log}_{10}(2\theta_{\text{rms}} + L)$
- Can we do better?

Unstable Cavities
PRL 115, 211104(2015)



GW and axion
PT-symmetric
unstable cavity
realizations:
[arXiv:2012.00836](https://arxiv.org/abs/2012.00836)

Intracavity Squeezing
(quantum expanders)
Korobko et al.
Light: Science & Applications (2019)



nonGaussian states...?!

the Third Generation of Detectors

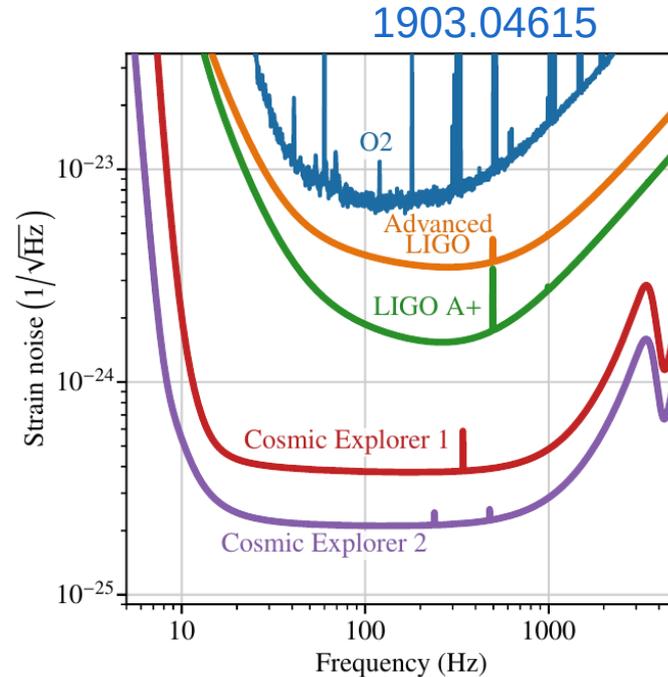
- Cosmic Explorer (US) and Einstein Telescope (EU)

- 10-40km observatories
(conceptual designs)
- 10x more optical power
- 10db squeezing
- Larger suspensions
- Lower frequencies

- Probe cosmological history of gravitational-wave astronomy

- High event rates – far detections
- Extreme signal-to-noise – near detections

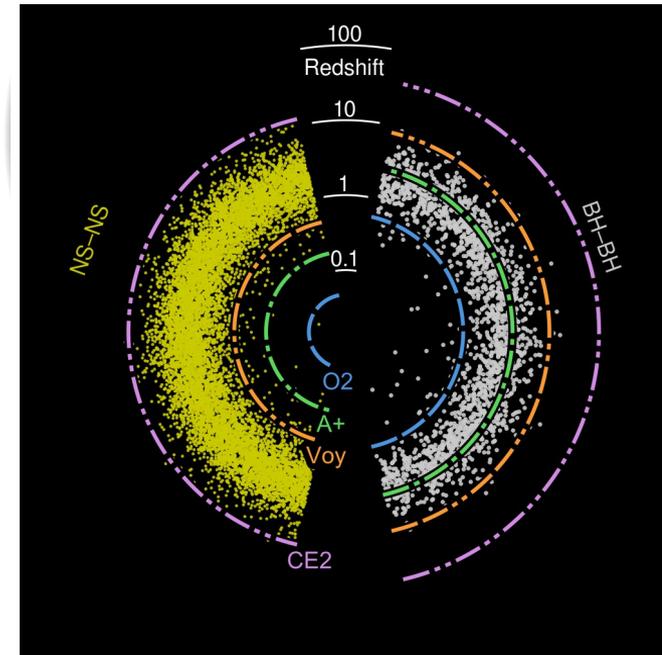
- What will the landscape be for multi-messenger observatories and complementarities?



Join the consortium

<https://cosmicexplorer.org/>

See nearly all binary neutron star events (left) and see black hole events to before BH's exist

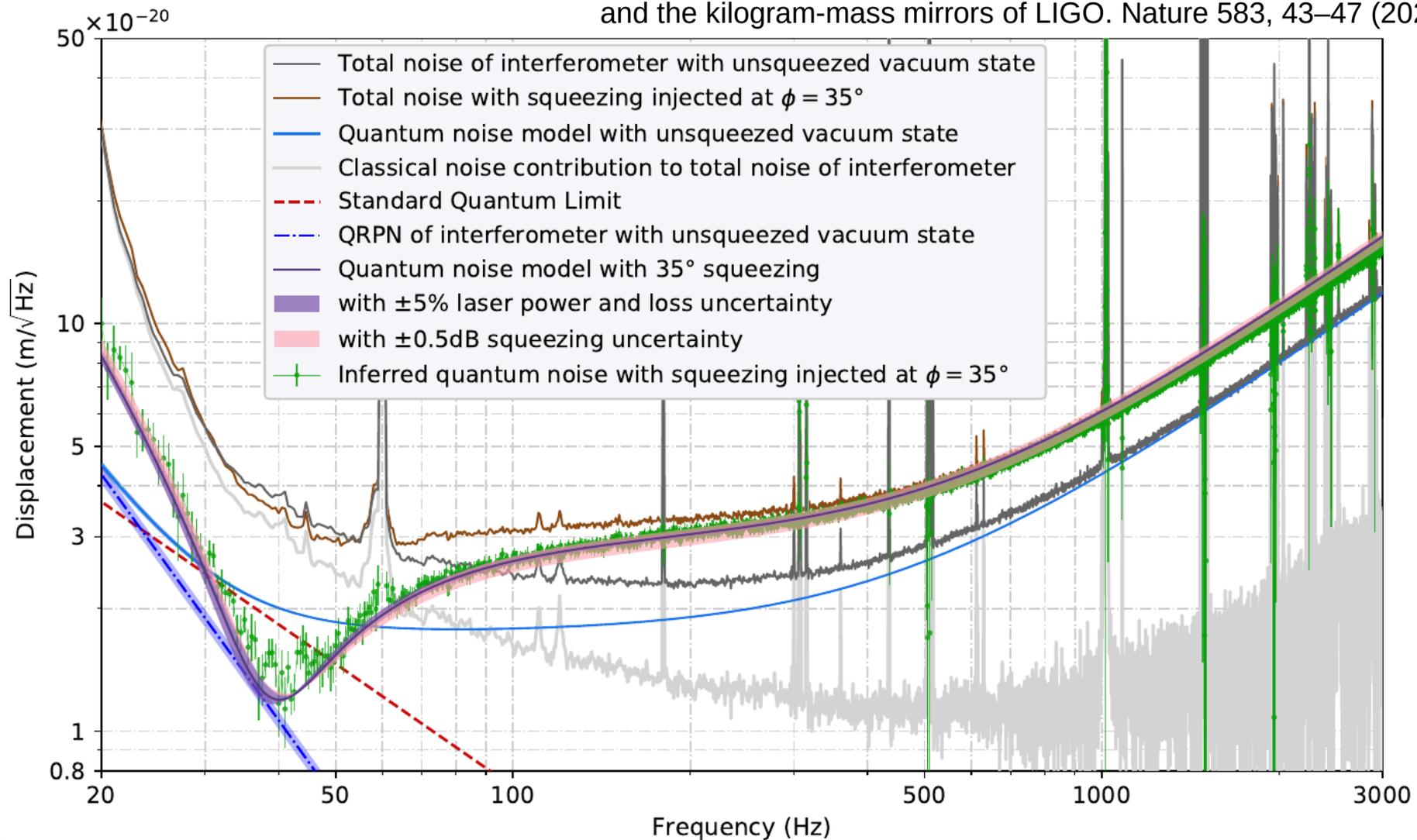


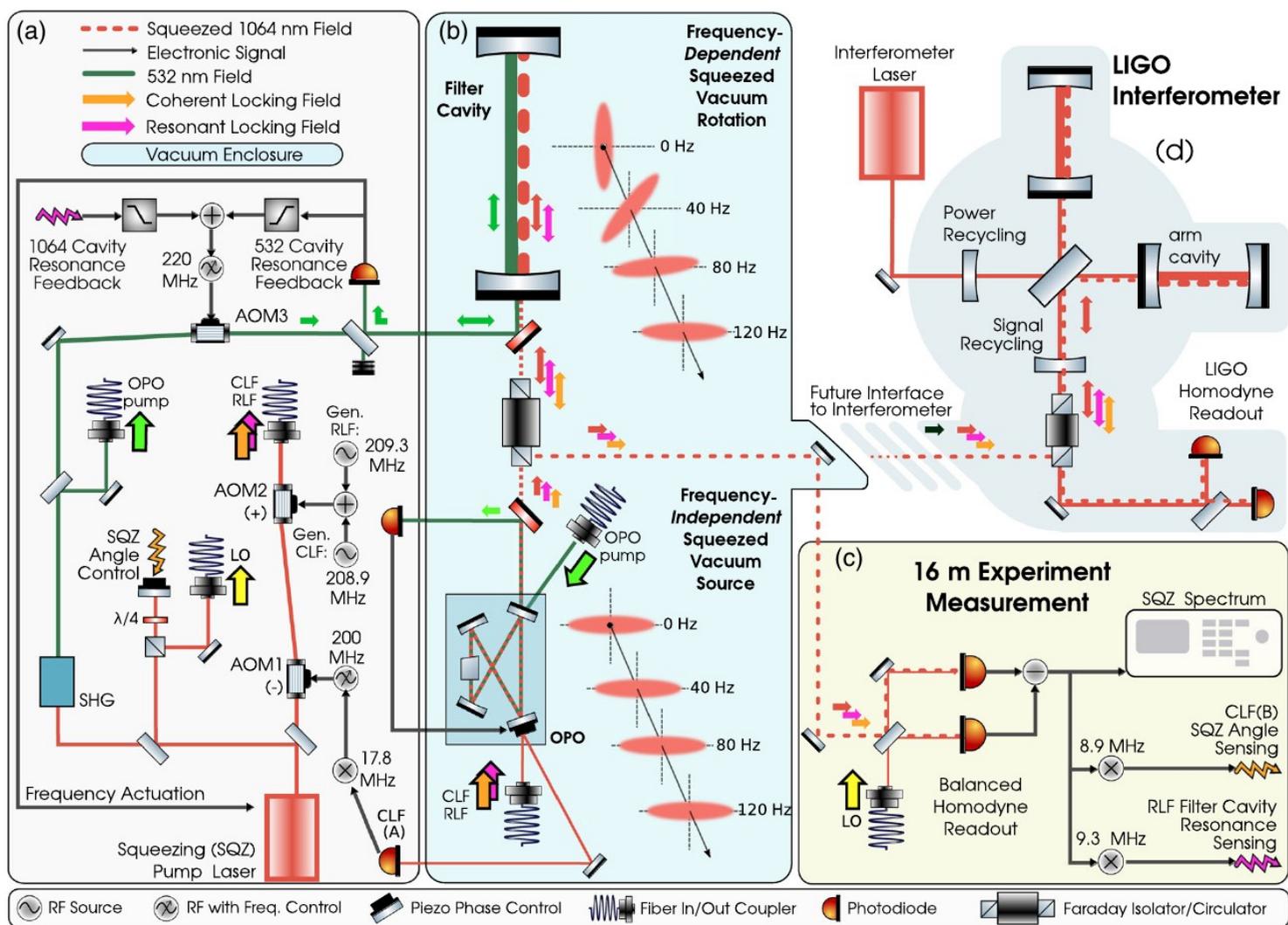
- LIGO, VIRGO, and GEO600 are now all *quantum-enhanced* in the *GW detection era*
- 40kg testmasses are quantum objects at 300K
 - The vacuum pushes mirrors → radiation pressure noise
 - this causes the *Standard Quantum Limit*
 - Not a limit when squeezing due to *quantum correlations*
- The A+ upgrades will improve the LIGO detectors ~8x in rate
 - Sub-SQL observations using frequency-dependent squeezing
 - separately demonstrated both of the necessary experimental components
 - Actively installing *now* for O4



(a personal proud moment)

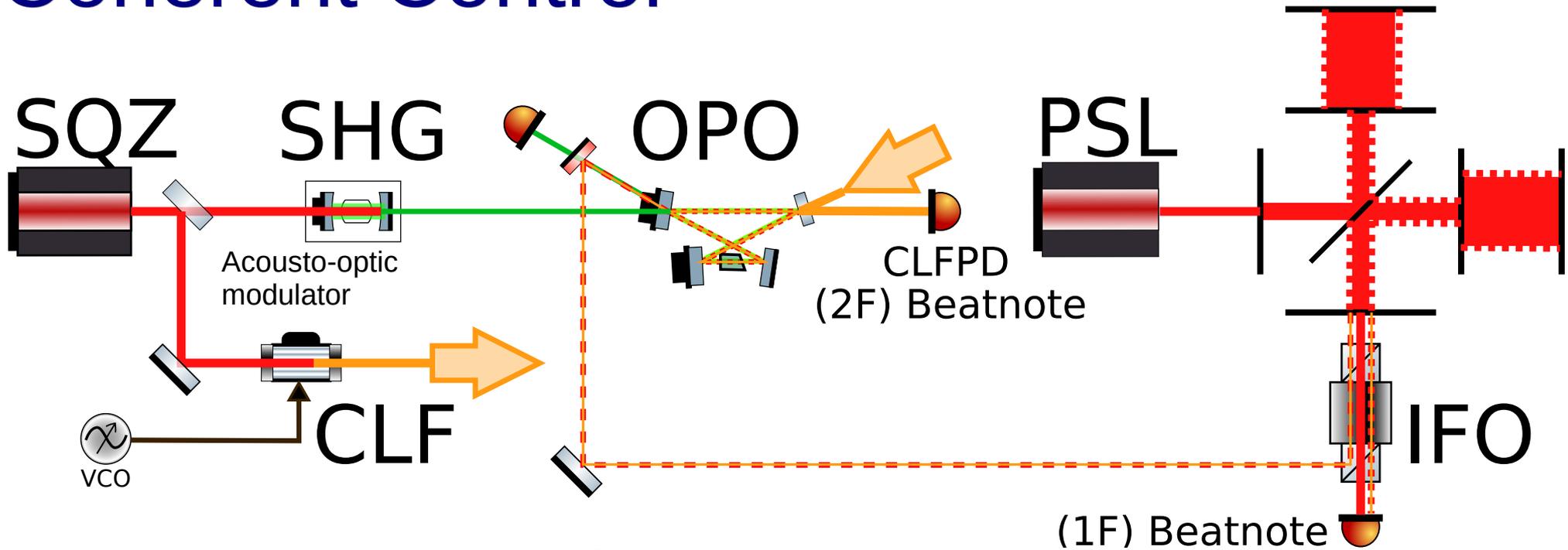
solving SQZ laser amplitude and phase noise excess at 600kHz.
400ns of cable
RF skills I developed at
FNALE990





McCuller, L. et al. Frequency-Dependent Squeezing for Advanced LIGO. Phys. Rev. Lett. 124, 171102 (2020).

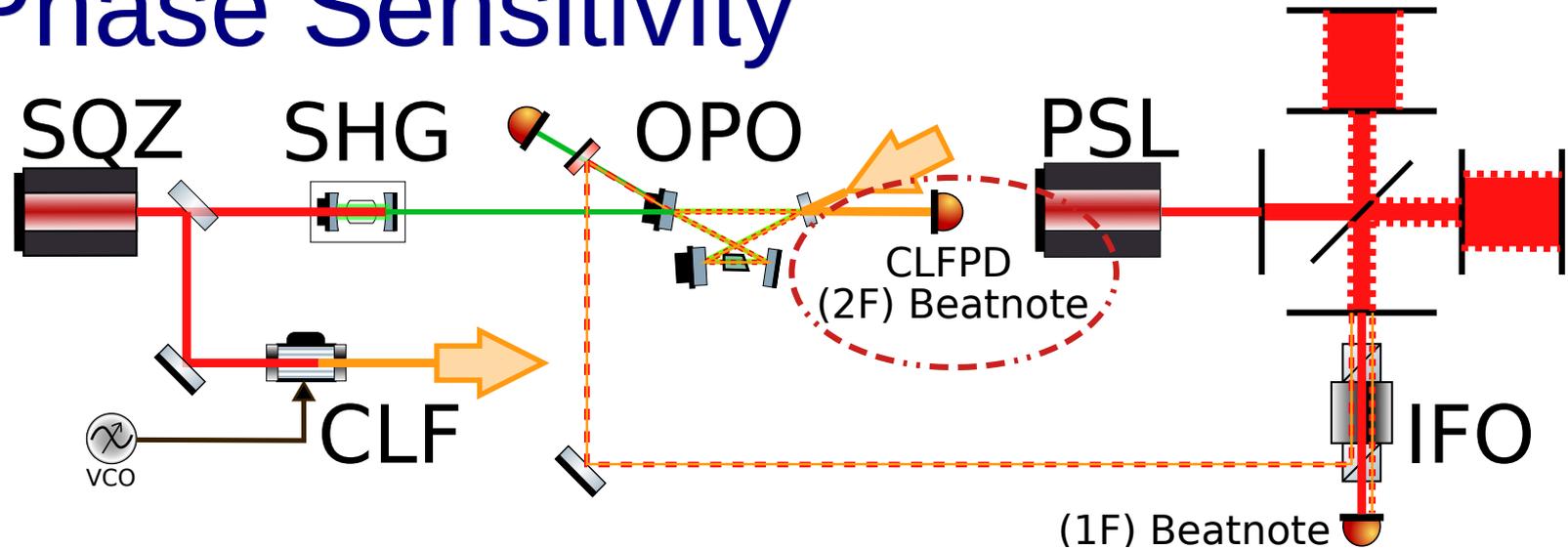
Coherent Control



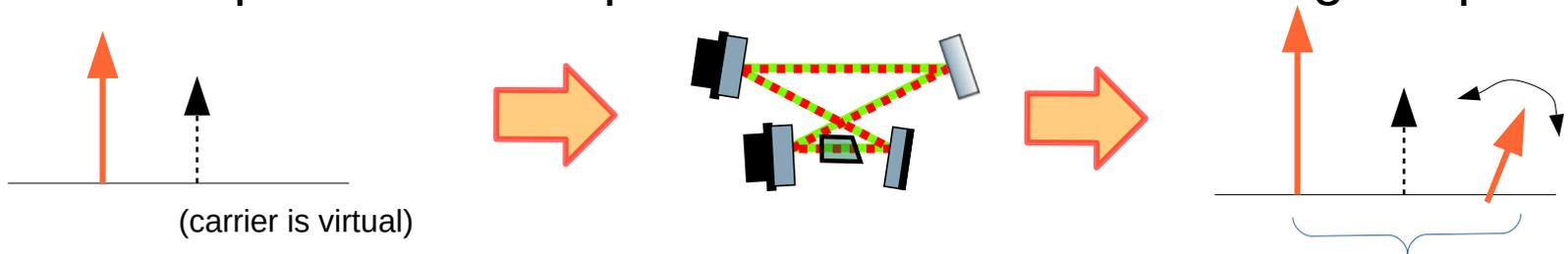
Coherent Locking Field (CLF)

RF single sideband created with acousto-optic modulator, added to squeezed light
Sees the nonlinear gain, co-propagates with the squeezing.
Also called the coherent control field.

CLF Phase Sensitivity

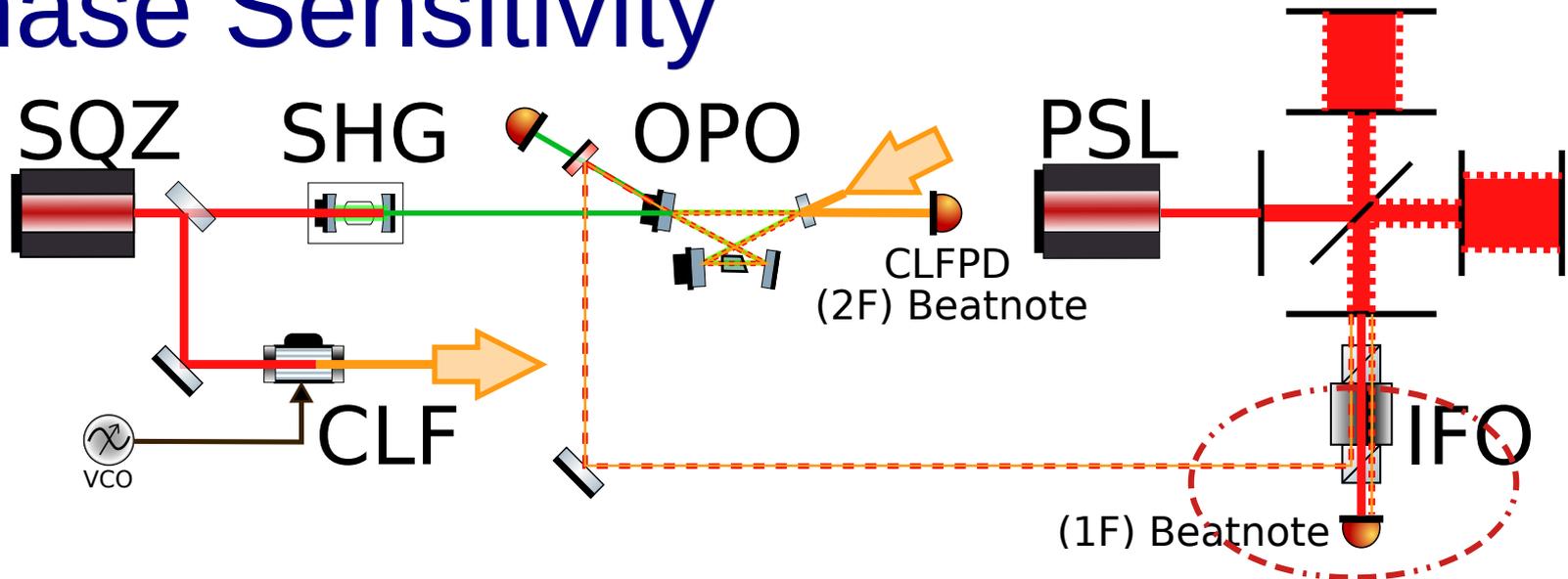


Phase-sensitive parametric amplification is used for sensing the pump phase

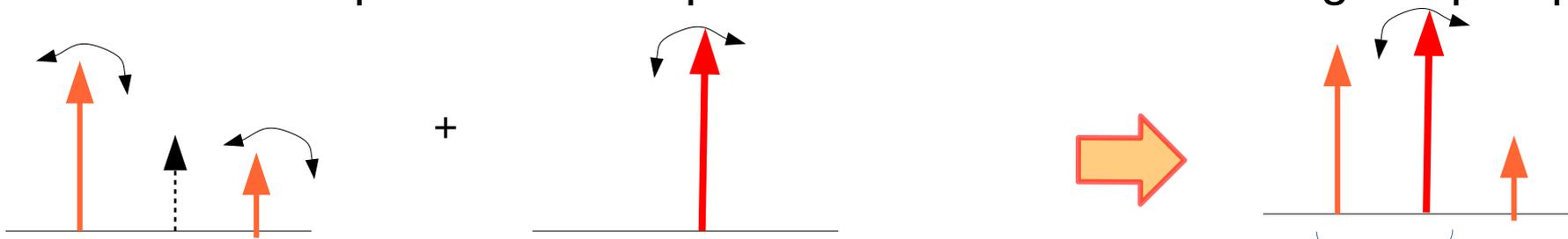


The CLF PD measures the beatnote of these two beams, senses the difference between the pump phase and the CLF optical phase

CLF Phase Sensitivity



Phase-sensitive parametric amplification is used for sensing the pump phase

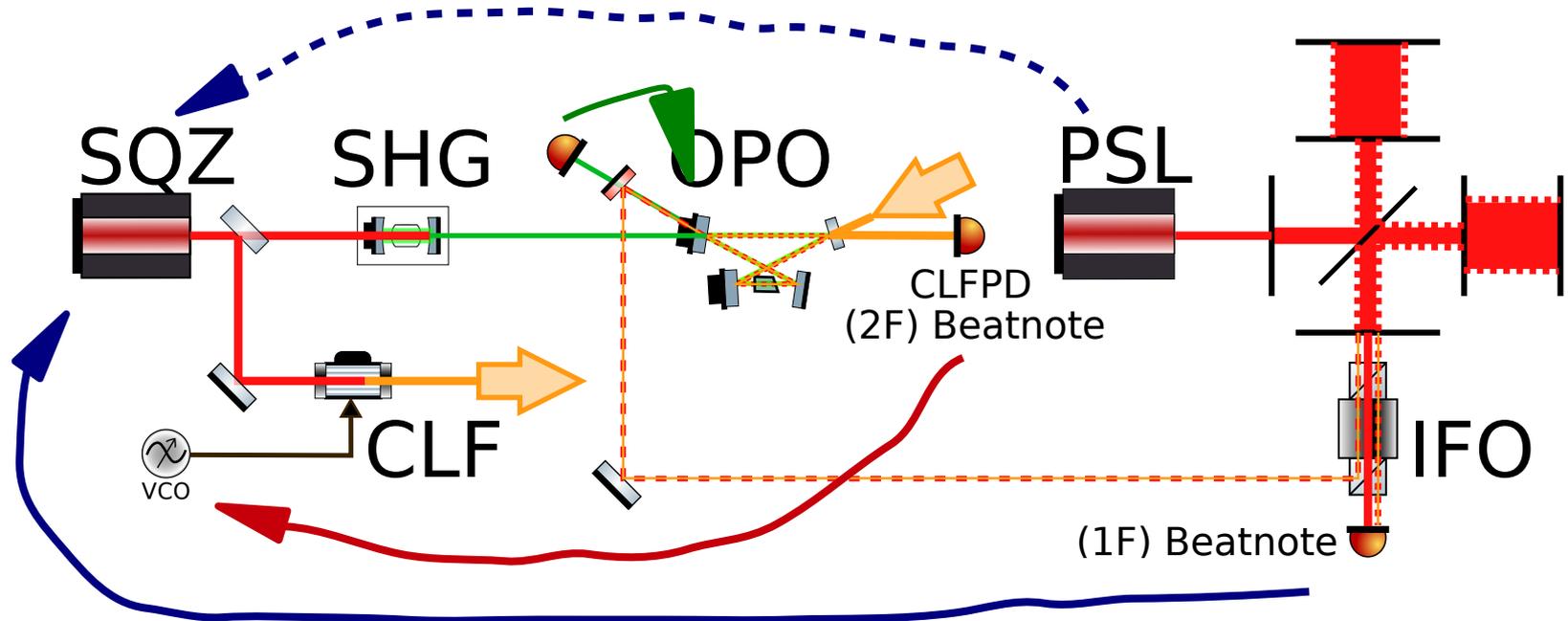


The IFO PD or homodyne measures the beatnote of the CLF with carrier Local Oscillator, senses the difference between the LO phase and the CLF optical phase

Squeeze Control Logic

- If the pump phase is “locked” to the CLF phase
- And the LO phase is “locked” to the CLF phase
- Then the pump phase follows the LO phase
- Implied: the squeezing phase follows the LO phase
- There is freedom to choose which phases actually move to implement “locking” control loops

Control Flow



>100kHz PSL Freq. Servo to SQZ Freq. (has residual noise)

~2-10kHz IFO (CLF 1F beatnote) to SQZ Phase (SQZANGLE)

~2-5kHz CLFPD 2F beatnote to RF Voltage controlled oscillator

~1kHz OPO PDH to OPO PZT (SHG is similar)